



Empirical rovibrational energy levels for methane

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ABSTRACT

A MARVEL (Measured Active Rotational Vibrational Energy Levels) analysis of the available spectroscopic data on methane ($^{12}\text{C}^1\text{H}_4$) is performed. A total of 82173 measured rovibrational transitions were gathered from 96 literature sources and put through the MARVEL procedure which led to the determination of 23292 empirical energy levels with uncertainties, up to 9900 cm^{-1} covering the lowest eight polyads. A comparison with Effective Hamiltonian evaluated levels, variational calculations by the TheoReTS project, and the McCaSDa database is performed. The new levels generated will be used to improve the upcoming ExoMol MM line list.

1. Introduction

Methane ($^{12}\text{C}^1\text{H}_4$) is the simplest stable hydrocarbon molecule, with wide-ranging implications in atmospheric and astrophysical chemistry. Methane on Earth has, natural, biological, and geological origins. It is produced by methanogenic microorganisms on wetlands as a metabolic byproduct. A natural reservoir of methane exists under permafrost regions and underneath the oceans in the form of methane hydrates [1]. Methane is central in atmospheric chemistry and its presence in the atmosphere affects the planet's temperature and climate system. Methane's concentration in the troposphere is increasing after a decade of constant value [2,3] making it an important global warming species. It has been identified as the second anthropogenic greenhouse gas after carbon dioxide [4,5]. Methane's atmospheric lifetime is notably shorter than that of carbon dioxide, primarily due to its reactivity with hydroxyl radicals (OH). Despite its shorter lifespan, methane is a more potent greenhouse gas, contributing significantly to heat-trapping in the atmosphere [4]. Consequently, precise measurement and monitoring of methane concentrations are of paramount importance for researchers dedicated to combating climate change [6]. Global methane emissions stem from a variety of human activities, surpassing those originating from natural processes. These anthropogenic sources include emissions from agriculture, biomass burning, the gas and oil industry, large-scale deforestation, industrial processes, combustion, and wastewater treatment, among others. In contrast, the number of natural methane sinks remains limited [7].

Methane's role in atmospheric chemistry and climate impact is not limited to Earth; methane is notably abundant within our Solar System [8]. Primarily found on the outer planets, methane is prevalent in the atmospheres of Jupiter [9], Saturn [10], Uranus [11], and

Neptune [12]. It has also been detected on Venus [13] and several moons, including Titan [14–16] and Triton [17–20], which renders it invaluable for atmospheric analysis and modeling. In addition to these celestial bodies, methane has sparked extensive debates regarding its presence and significance on Mars [21–26], as well as its origin on the Martian surface [27]. Moreover, methane has been detected in some distant objects like comets [28,29] by flyby missions and ground observations, as well as Pluto [30]. Infrared absorption spectra of Type T class of brown dwarfs also reveal the presence of methane [31,32] and are even referred to as “methane dwarfs” [33].

Our primary focus in this study is the significance of methane in the investigation of extrasolar planets. High-resolution infrared spectroscopy is very important in order to understand the chemical composition of the atmosphere of such planets [34]. The substantial advancements in exoplanet discovery have ignited a strong interest within the scientific community to identify exoplanets that may be inhabited or possess habitable conditions. Therefore, recognizing and detecting biosignatures is one of the main goals of researchers in this field. Methane is considered a biosignature for terrestrial planets [35,36], which means it can be a very good indicator of the presence of life beyond Earth, and maybe a sign of early Earth-like environments. Interestingly, it is the sole detectable biosignature by the James Webb Telescope, in contrast to oxygen [37].

In the context of exoplanets, gas giants known as hot Jupiters are expected to contain methane, alongside other molecules such as water and carbon monoxide [38]. Indeed, methane has been observed in the atmospheres of hot, gaseous exoplanets, including HD 189733b, HD 209458b, and XO-1b [34,39–41]. Furthermore, warm Neptunes like GJ 436b and GJ 3470b are expected to exhibit methane-rich atmospheres,

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although its abundance on these planets has occasionally been a subject of debate [42–45]. Consequently, accurately determining the methane content is essential for characterizing exoplanets [46,47].

The importance of methane has led to the construction of numerous line lists [48–55], and plenty of experimental works aimed at accurately characterizing methane's spectral properties. A large number of such works have been utilized in the current analysis. In this work, we compiled all the available experimental spectroscopic data up until July 2023 and put them through the MARVEL procedure in order to determine a dataset of empirical rovibrational energy levels with experimental accuracy. The goal is to improve the upcoming ExoMol MM methane line list [56] by using empirical energy levels in place of the computed values with the variational program TROVE [57].

2. Theoretical background

2.1. MARVEL

Furtenbacher et al. developed the Measured Active Rotation Vibration Energy Level (MARVEL) algorithm [58–61] that we use here to determine accurate empirical energy levels of $^{12}\text{C}^1\text{H}_4$. The MARVEL procedure starts with the creation of a dataset of measured high-resolution spectroscopic transition frequencies (line positions). It is essential that the transitions are assigned with a consistent set of quantum numbers for their upper and lower states and have uncertainties. Each transition is labeled uniquely with a tag that shows the source it originates from, as well as a number identifying it within the source.

MARVEL employs a methodology of transition inversion to derive a set of empirical energy levels accompanied by their respective uncertainties via a weighted linear least-squares inversion protocol. This process involves a meticulous evaluation of the self-consistency of experimental transition frequencies, followed by iterative adjustments of uncertainty values. The goal is to attain a cohesive network of energy levels, referred to as a spectroscopic network. In this network, vertices represent discrete energy levels, and edges represent the transitions connecting these levels [62–64]. Specifically, MARVEL computes optimal uncertainty values for each energy level to ensure their internal consistency within the spectroscopic network.

The MARVEL 4 Online version [65] offers enhanced flexibility in handling transition energy units. Unlike previous versions that exclusively used cm^{-1} , MARVEL 4 Online can accommodate various units (cm^{-1} , Hz, kHz, MHz, GHz, and THz). To support this expanded functionality, a segment file is included as an input, containing a list of source names paired with their respective units.

MARVEL helps enhance significantly the quality of the database by identifying outliers, often resulting from inaccurately assigned wavenumbers or during the transcription of the measured data into the transition list. Transitions are flagged as invalid if the ratio between the optimal uncertainty and the original uncertainty exceeds a threshold of 100. These invalidated transitions are either corrected or annotated with a negative sign applied to their wavenumber values, to exclude them from further analysis by MARVEL.

By iteratively applying this procedure, we systematically improve the transition uncertainties while simultaneously removing incorrect lines from the database. This process results in the compilation of a catalog of uniquely labeled and internally consistent transitions, which subsequently serves as the foundation for generating the MARVEL energy levels.

It is challenging to find the optimal set of transition uncertainties since they are experimental, and we usually need to increase them manually in order to create a self-consistent network. However, MARVEL offers a feature known as the bootstrap method, which iteratively performs calculations to determine the optimal energy level uncertainties [65]. With the bootstrap method, however, the uncertainties of the final set of MARVEL uncertainties are determined to be suitable and reasonable. In this work, we performed the analysis both with and without the bootstrap method.

2.2. Quantum numbers and selection rules

Methane is a spherical top molecule with tetrahedral symmetry and belongs to the symmetry group T_d with five irreducible representations A_1 , A_2 , E , F_1 , and F_2 [66]. It has nine vibrational degrees of freedom and four normal modes of vibration: The non-degenerate symmetric C–H stretching vibration ν_1 (A_1 symmetry), the doubly degenerate C–H bending vibration (E symmetry) known as the ν_2 mode, and two triply degenerate modes (F_2 symmetry); the ν_3 mode corresponds to the C–H stretching vibration, while the ν_4 mode is associated with the C–H bending vibration. Each vibrational level is identified by a set of nine normal quantum numbers: ν_1, ν_2, ν_3 and ν_4 describing the corresponding excitations of the four normal modes ν_1, ν_2, ν_3 and ν_4 , and l_2, l_3 and l_4 , describing the vibrational angular momenta of ν_2, ν_3 and ν_4 , as well as the associated multiplicity indices m_3 and m_4 [50]. The fundamental frequency wavenumbers are $\bar{\nu}_1(A_1) = 2916.481 \text{ cm}^{-1}$, $\bar{\nu}_2(E) = 1533.333 \text{ cm}^{-1}$, $\bar{\nu}_3(F_2) = 3019.493 \text{ cm}^{-1}$, $\bar{\nu}_4(F_2) = 1310.761 \text{ cm}^{-1}$ [67].

The four normal mode wavenumbers $\bar{\nu}_i$ exhibit the following approximate relation:

$$\bar{\nu}_1 \approx \bar{\nu}_3 \approx 2\bar{\nu}_2 \approx 2\bar{\nu}_4 \approx 3000 \text{ cm}^{-1}. \quad (1)$$

This leads to the vibration energies of methane being grouped in a polyad structure [68,69]. The integer polyad number P is defined as $P = 2(\nu_1 + \nu_3) + \nu_2 + \nu_4$ and is numbered with increasing energy starting with $n = 0$ for the Monad, $n = 1$ for the Dyad, $P = 2$ for the Pentad, $P = 3$ for the Octad, etc. Fig. 1 shows schematically the first eight polyads of methane with the number of levels and sublevels within each one. Each polyad is labeled with a Greek prefix for the number of the levels. Here a vibrational level is defined simply by the quantum numbers $(\nu_1, \nu_2, \nu_3, \nu_4)$ while the sublevels comprise all the vibrational angular momentum or symmetry products that are allowed for this vibrational level. Thus, the vibrational level $(\nu_1, \nu_2, \nu_3, \nu_4)$ is split into several sublevels as soon as it is not just one fundamental level. For instance, “ $2\nu_3$ ” or level $(0, 0, 2, 0)$ has three sublevels A_1 , E and F_2 . The degeneracy exhibited by three of the normal modes results in an increasing number of vibrational sublevels as the molecule is excited.

In addition to the vibrational quantum numbers, the total angular momentum of the molecule is denoted J . Methane is classified into three nuclear spin isomers: meta ($I = 2$, A_1 , A_2), ortho ($I = 1$, F_1 , F_2) and para ($I = 0$, E). In the case of higher polyads, the number of sublevels m within a particular symmetry species tend to closely approximate a regular representation, with a ratio of $m(A_1) : m(A_2) : m(E) : m(F_1) : m(F_2)$ equal to 1:1:2:3:3 [67].

The full assignment using the normal mode quantum numbers albeit being theoretically most appropriate gets quickly very complicated with the vibrational excitations. As a practical alternative, the following set of four rotation-vibration quantum numbers is used: the polyad number P , the total angular momentum J , the total symmetry C , the counting number α , which counts the levels with the same (C, J) within a polyad from lower to higher energy.

The electric dipole transitions follow specific selection rules determined by their symmetry:

$$A_1 \leftrightarrow A_2, E \leftrightarrow E, F_1 \leftrightarrow F_2$$

with the standard rotational angular momentum selection rules:

$$\Delta J = -1, 0, 1, \quad J' + J'' \neq 0,$$

leading to the three well-known P , Q and R branches, respectively.

The symmetric ν_1 stretching (A_1) and the asymmetric ν_2 bending (E) modes lead to no change in the dipole moment and as such, are infrared inactive. Only the two F_2 modes ν_3, ν_4 (and more generally, all F_2 vibrational sublevels) are infrared active for transitions starting in the ground vibrational state, as a first approximation. The ro-vibrational transitions of the IR non-active bands get intensities through ro-vibrational interactions with IR active states.

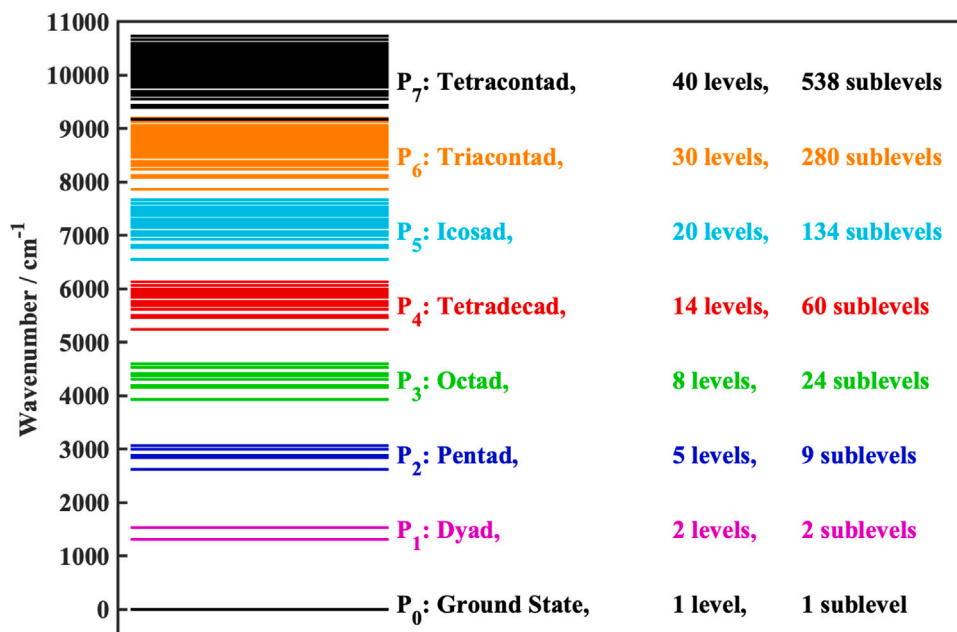


Fig. 1. The first eight vibrational polyads of methane and the number of vibrational levels and sublevels in each one [70].

Table 1

Information on the number of experimental sources and transitions per vibrational band included in our input line list. Average uncertainty is given in cm^{-1} . A/V: total number of available transitions/number of validated transitions.

Bands	A/V	Sources	Av. Unc. cm^{-1}
P0–P0	153/153	10 ^a	0.002262
P1–P0	3452/3433	12	0.008287
P1–P1	140/140	4	0.002144
P2–P0	3406/3397	29	0.003453
P2–P1	5932/5931	6	0.003850
P2–P2	16/16	2	0.000001
P3–P0	32369/32308	13	0.006160
P3–P1	1699/1699	1	0.002000
P3–P2	149/149	2	0.001907
P4–P0	21154/21028	21	0.002323
P4–P1	7316/7275	3	0.007303
P4–P2	31/17	3	0.015161
P4–P3	44/34	1	0.002000
P5–P0	5953/5927	8	0.001381
P5–P1	22/22	1	0.001000
P6–P0	329/329	1	0.005000
P6–P2	26/26	2	0.003492
P7–P3	4/2	1	0.005000

^a One of them is “magic” numbers explained in Section 4.1.

In this analysis, we have used transitions both from Raman and infrared spectra. The selection rules for the Raman spectrum of methane follows: all four vibrational modes are active and the rotational selection rules in the general case are:

$$\Delta J = -2, -1, 0, 1, 2,$$

leading to the five *O*, *P*, *Q*, *R* and *S* branches. One should notice however that for the *A*₁ vibrational sublevels, such as ν_1 fundamental band, there is only a *Q* Raman branch ($\Delta J = 0$).

3. Overview of experimental sources

A comprehensive collection of high-resolution spectra of $^{12}\text{C}^1\text{H}_4$ has been assembled for this study. A total of 279 research articles were reviewed, and from this pool, 96 were selected for inclusion in our current research. A summary of these selected sources, along with details regarding their observational data, is presented in Tables 1 and

3. Additionally, Table 4 provides information about the sources that were considered but ultimately excluded from our analysis. Comments related to Table 3, especially referring to the assignment of unassigned lines and the treatment of the uncertainties are found in Section 3.1.

We built the dataset of the observational spectra from lower to higher polyads testing with MARVEL at each step. In particular, for our final runs, we used the MARVEL 4 Online version [65].

3.1. Comments on the data sources

During the MARVEL process, we increased some initial uncertainties to create a self-consistent network. We also estimated uncertainties when they were missing in the original papers. Regarding the line assignments, many sources had fully assigned lines, while others did not. For those without assignments, we either assigned them ourselves or excluded them. This subsection provides detailed notes and comments on sources for which full assignments were unavailable in the source data.

76Pine [71]: The transitions were assigned in the paper using a different counting numbers convention. We reassigned them using the Effective Hamiltonian fit by 16AmLoPi [72].

79DaPiRo [73]: We assigned the counting numbers using transitions from other sources.

79PiDu [74]: The ν_4 transitions are assigned using a different convention for the counting numbers in the original paper, and we reassigned them using lines from [75] and the set of calculated energy levels provided by 16AmLoPi [72].

82JeRo [76]: The ν_4 transitions are partly assigned in the original paper without the upper state's counting numbers. We were able to assign them using the Effective Hamiltonian fit by 16AmLoPi [72].

16AmLoPi [72]: We used the P_1-P_0 and P_2-P_1 lines but not the P_3-P_2 , P_4-P_3 lines because they were inconsistent with the rest of the network.

83DeFrPr and 83DeFrPrb [77,78]: The lines were taken as published and assigned by 97MaBeSa [79].

85ChKlNi [80], 79DoKoTa [81], and 81DoKoTa [82]: Measurements of one F -symmetry line at 88 THz were published by 85ChKlNi [80]. The original papers 79DoKoTa [81] and 81DoKoTa [82] (references 6 and 8 of [80] respectively) were not found. Other measurements of the same transition were published by 82ChGoKl [83], 76BlEdJo [84], 80KnEdPe [85], 80ClDaRu [86], 72EvDaWe [87], and 92KrLiWe [88] and we assigned them fully using lines by 09AlBaBo [70].

88Brown [89]: 12 of the 235 published observed transitions were identified as $3\nu_4$ R0-R4 lines. We assigned the quantum numbers for these lines using the Effective Hamiltonian fit by 16AmLoPi [72].

92PuWe [90]: We assigned the counting numbers for the pure rotational transitions in the ν_3 band with the use of the calculated energies from the Effective Hamiltonian fit by 16AmLoPi [72].

98BrKaRu [91]: We used the more recent assignments from [72].

98ErTyKr [92]: One E -line is measured, which we assigned fully using [70].

00FeChJo [93]: The upper state's counting numbers were assigned using 09AlBaBoBr [70] lines.

02HiQu [94]: The full assignments were taken from 12TaQu [95].

05Brown [96]: The full assignments of 27 of the published lines were taken from 12TaQu [95].

05PrBrMa [97]: We reassigned the following transitions:
 4286.949 cm^{-1} from ($P' = 3, J' = 4, C' = F_2, \alpha' = 41; P'' = 0, J'' = 5, C'' = F_1, \alpha'' = 1$) to ($3, 4, F_2, 41; 0, 5, F_1, 2$),
 4509.857 cm^{-1} from ($3, 10, A_1, 37; 0, 9, A_2, 1$) to ($3, 10, A_2, 35; 0, 9, A_1, 1$),
 4492.216 cm^{-1} from ($3, 4, F_2, 52; 0, 3, F_1, 1$) to ($3, 4, F_2, 58; 0, 5, F_1, 1$),
 4522.050 from ($3, 11, F_1, 117; 0, 10, F_2, 3$) to ($3, 11, F_2, 114; 0, 10, F_1, 2$).

09ScKaGa [98]: Full assignments of 27 of the published lines were taken from 12TaQu [95].

10NiLyMi [99]: We assigned the upper state's counting numbers of 2551 lines using lines from 15NiLyMi [51] as well as lines from other sources in this range.

12CaWaMo [100]: The transitions were published unassigned, and we used the assignments provided in the HITRAN database [101].

12TaQu [95]: We attributed the counting numbers using HITRAN lines [102], and lines from [103], and [94].

13AbIwOk [104]: The full assignments were taken from 18AmBo [105].

13CaLeWa [106]: The transitions were published unassigned, but have been assigned in other works; we used 3436 lines assigned by

17NiChRe [107], and 2445 lines by 16NiReTa [108]. In addition, 16ReNiCa [109] published 10034 partly assigned lines in the range 6539–6800 cm^{-1} without counting numbers. We assigned counting numbers for 1906 of these lines using other sources. We also reassigned the following lines after evaluating them with MARVEL:

5931.350 cm^{-1} from ($4, 8, F_1, 207; 0, 7, F_2, 1$) to ($4, 8, F_1, 208; 0, 7, F_2, 1$),

6102.645 cm^{-1} from ($4, 10, F_2, 325; 0, 9, F_1, 3$) to ($4, 10, F_2, 326; 0, 9, F_1, 3$),

5998.240 cm^{-1} from ($4, 10, F_2, 325; 0, 10, F_1, 2$) to ($4, 10, F_2, 326; 0, 10, F_1, 2$).

13NiBoWe [110]: We reassigned the following transition: 5782.556 cm^{-1} from ($4, 8, F_2, 180; 0, 8, F_1, 1$) to ($4, 8, F_2, 181; 0, 8, F_1, 1$).

13ZoGiBa [111]: 1153 assigned lines were published with no counting number for the upper state. We assigned 348 of them using the Effective Hamiltonian fit by 16AmLoPi [72].

16DeMaRe [112]: 307 assigned lines were published without the upper state's counting numbers. We attributed the counting numbers using the Effective Hamiltonian fit by 16AmLoPi [72].

17HaPrNi [113]: We reassigned the following transitions:

4417.888 cm^{-1} from ($3, 7, F_1, 66; 0, 6, F_2, 1$) to ($3, 7, F_1, 66; 0, 6, F_2, 2$),

4489.943 cm^{-1} from ($3, 4, F_2, 56, 0, 5, F_1, 1$) to ($3, 4, F_2, 56; 0, 5, F_1, 2$),

4469.327 cm^{-1} from ($3, 6, F_2, 80, 0, 7, F_1, 1$) to ($3, 6, F_2, 80; 0, 7, F_1, 2$),

4432.663 cm^{-1} from ($3, 8, F_2, 76; 0, 7, F_1, 1$) to ($3, 8, F_2, 76; 0, 7, F_1, 2$),

4427.818 cm^{-1} from ($3, 8, F_2, 75; 0, 7, F_1, 1$) to ($3, 8, F_2, 75; 0, 7, F_1, 2$).

18GhMoKa [114]: We reassigned the transition 5753.757 cm^{-1} from ($4, 8, F_1, 207; 0, 9, F_2, 1$) to ($4, 8, F_1, 208; 0, 9, F_2, 1$).

18GoPrKa [115]: The counting numbers were attributed using the lines by 16DeMaRe [112].

18KoMaEs [116]: We assigned counting numbers using lines by 13TyTaRe [117].

18YaLiFe [118]: Lines from several other sources were used to attribute counting numbers.

19LiYaFe [119]: We attributed full assignments using HITRAN lines [102] or the Effective Hamiltonian fit by 16AmLoPi [72].

19YaLiFe [120]: One measured transition is published in this work and assigned as an $R(1) 2\nu_1 + \nu_3$ line. We reassigned this line to an $R(0)$ line and assigned counting numbers using the HITRAN database [102], and the sources 13ZoGiBa [111] and 13CaLeWa [121].

20YaLiPl [122]: We assigned 6 of the published lines using transitions from several other sources.

21OkInOk [123]: The counting numbers for the transitions were found using lines from other sources and the Effective Hamiltonian fit by 16AmLoPi [72].

21FoRuSi [124]: The full assignments for the transitions were attributed using other lines from our line list, as well as calculated energies from 16AmLoPi [72].

3.2. Raman spectra

The following data sources provided Raman spectra we evaluated and considered in our analysis.

Table 2

Magic numbers. Wavenumber values were selected from the effective Hamiltonian energy values by 16AmLoPi [72].

Wavenumber cm^{-1}	Unc cm^{-1}	Upper state				Lower state				Label
		P'	J'	C'	α'	P''	J''	C''	α''	
10.481641	0.000001	0	1	F_1	1	0	0	A_1	1	MAGIC.1
31.442100	0.000001	0	2	E	1	0	0	A_1	1	MAGIC.2
31.442366	0.000001	0	2	F_2	1	0	0	A_1	1	MAGIC.3
62.878129	0.000001	0	3	A_2	1	0	0	A_1	1	MAGIC.4
104.772781	0.000001	0	4	A_1	1	0	0	A_1	1	MAGIC.5
62.875738	0.000001	0	3	F_1	1	0	0	A_1	1	MAGIC.6
2179.816	0.030	0	20	E	1	0	0	A_1	1	MAGIC.7
2620.967	0.010	0	22	E	1	0	0	A_1	1	MAGIC.8
3104.763	0.010	0	24	A_2	1	0	0	A_1	1	MAGIC.9
3104.752	0.010	0	24	F_2	2	0	0	A_1	1	MAGIC.10

We included 379 Raman transitions in total. The sources we used are the following:

75ChBe [125] reported 196 ν_2 Raman transitions in the range 1360–1770 cm^{-1} belonging to the O , P , R , and S branches which were assigned by 76GrRo [126] and 77Champion [127].

92BeSaCa [128] reported 83 ν_1 and $\nu_2 + \nu_4$ Raman lines in the range 2911–2921 cm^{-1} belonging to the Q branch.

91MiLaSt [129] reported 13 ν_2 Raman lines in the range 3063–3066 cm^{-1} belonging to the Q Branch.

94HiChTo [130] reported 37 $2\nu_2$ Raman lines in the Q branch and the range 3063–3070 cm^{-1} from a thesis by J.M. Jouvard, University of Bourgogne (1991).

97MaBeSa [79] measured 21 $2\nu_1 - \nu_1$ Raman lines in the Q branch. In addition, they reported 4 Raman lines in the $2\nu_3 - \nu_3$ band in the R and P branches and the 2800–6000 cm^{-1} range that are originally from 83DeFrPr [77], as well as 6 lines from 83DeFrPrb [78]. The 83DeFrPrb lines were not validated by MARVEL.

92SaCaDo [131] reported 45 ν_1 Raman lines that have also been published and assigned by 92BeSaCa [128], as well as 13 lines by 79KoPrSm [132] and 6 lines by 85GrLa [133]. The assignments of these lines were also done using lines by 92BeSaCa [128].

The following Raman sources were not used:

85ThFaKo [134]: The Raman lines reported were not used because of low accuracy.

78OwPaDo [135]: 32 ν_1 Raman lines were measured in the 2916–2918 cm^{-1} range with assignments without counting numbers.

70ClSt [136]: No measured wavenumbers.

75Champion [137]: Only calculated values were provided.

78MaHeBy [138]: No measured wavenumbers.

15MaKcVa [139]: Measured Raman spectra were reported at temperatures ranging from 300 K to 860 K covering the 882 – 1791 cm^{-1} and 2548 – 3434 cm^{-1} regions without assignments.

77Berger [140]: Raman ν_3 lines were reported ranging from 2850 cm^{-1} to 3100 cm^{-1} . The lines were assigned in this source as well as by [141] but the counting numbers follow a different convention that we could not use.

83FrIlFi [142]: ν_1 Raman Q branch lines were reported from 2916 to 2917 cm^{-1} assigned with a different convention for the counting numbers.

06JoChSa [143]: No measured wavenumbers.

82LoBrRo [144]: Measurements of $2\nu_4$ Raman transitions in the 2460–2675 cm^{-1} region were published. The assignments were different and due to low accuracy, we were not able to include them in the analysis at this stage.

07JoGaCh [145]: No measured wavenumbers.

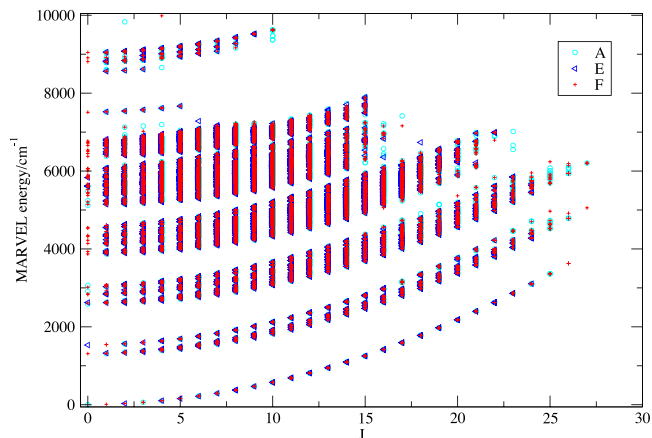


Fig. 2. The $^{12}\text{C}^1\text{H}_4$ MARVEL energy levels for the first eight polyads obtained in this work. The symbols denote the different symmetries; A: A_1 , A_2 , E: E , F: F_1 , F_2 .

4. The MARVEL networks

Out of a total of 82173 transition frequencies assessed by the MARVEL procedure, 308 were not validated and were assigned a negative wavenumber in the input line list. At this stage, six artificial transitions were included called “magic” numbers (the first six in Table 2). Three of them to connect the different nuclear spin isomers, and three to improve the network connectivity as explained below in Section 4.1. This resulted in a spectroscopic network comprising 81865 lines, separated into 305 components. The largest component consisted of 80598 transitions connecting 23060 energy levels, with 109 of these components containing one single transition linking two levels.

The next four components were two E symmetry, one A_1/A_2 , and one F_1/F_2 symmetry networks which consisted of 103, 57, 48, and 44 transitions respectively. To establish connections between them and the largest component four new magic numbers were added (the last four in Table 2). We connected only these four to the largest network because the next was a much smaller one consisting of only 29 transitions. As a result, we ended up with 81872 validated transitions in total separated into 301 components, the largest one of which includes 80854 transitions that link 23292 energy levels.

The distribution of energy levels according to their symmetries is as follows: 21.4% are of A_1/A_2 symmetry, 18.4% are of E symmetry, and 60.2% are of F_1/F_2 symmetry. The energy distribution with respect to J are illustrated in Fig. 2 and relevant details are given in Table 5.

We compared our empirical rovibrational energy levels to the Effective Hamiltonian results of 16AmLoPi [72], variational energies from the TheoReTS project [53], and calculated levels from the MeCaSDa database [146]. Figs. 3 and 4 show the differences between the MARVEL levels and levels from the TheoReTS project. For the comparison with the MeCaSDa database see the Supplementary Material,

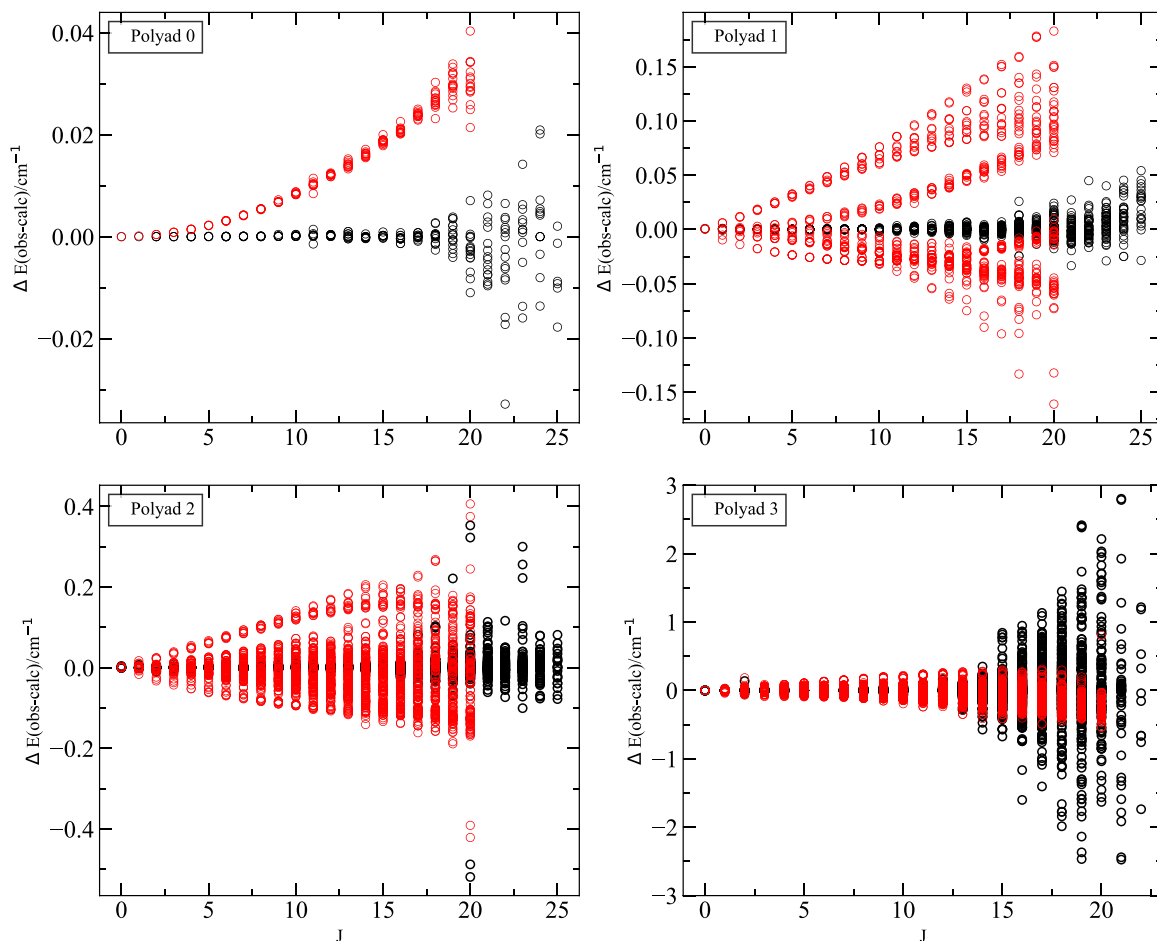


Fig. 3. Difference between the MARVEL energies (obs) and the a. Effective Hamiltonian by [72] (black) b. Variational calculations (red) by [53].

which also provides the full comparison with the TheoReTS variational calculations.

For the first two polyads the agreement with the Effective Hamiltonian energies by 16AmLoPi [72] is very good for $J \leq 17$ with a maximum difference of less than 0.007 cm^{-1} . For the next two polyads, the agreement with the Effective Hamiltonian energies is very good for $J \leq 15$ with a maximum difference of less than 0.014 cm^{-1} . Regarding the comparison with the TheoReTS variational energies, the agreement is always within 1 cm^{-1} for the first five polyads. Additionally, in polyad 3 the TheoReTS energies exhibit better agreement with the MARVEL energies than the Effective Hamiltonian energies in high J values. The comparison with the MeCaSDa database follows a similar trend to the one with the Effective Hamiltonian results. The differences grow with J and polyad P in all cases and grow more in the cases of polyad 5 and polyad 6 where our data are limited.

For polyad 2 Fig. 3 shows a difference of $\approx 0.4 \text{ cm}^{-1}$ between MARVEL and the Effective Hamiltonian energies, as well as the TheoReTS energies for four $J = 20$ levels. These differences are much smaller when compared with MeCaSDa (see Supplementary Material). These four levels, comprising two E levels and two A_2 levels, are part of two weakly coupled components within the network. Their connections to the broader network are limited, leading to less accurate definitions: the Supplementary Material gives details of these states and linked levels. Additionally, the single transition defining the states (2,20, A_2 ,14) and (2,20, E ,28) is given three different assignments in the original source [72]; it is assigned as an F line, an E line, and an A line. We note that F states are generally better defined, as they are characterized by more transitions. More experimental data are required to resolve the above problem and enhance the accuracy of the A and E networks.

4.1. Magic numbers

To interconnect previously unlinked networks, including the ortho, para, and meta networks, we use artificial transitions that we call ‘magic numbers’. In addition, some extra magic numbers were used. Specifically, the first three (MAGIC.1, MAGIC.2, MAGIC.3) were used to link the ortho, para, and meta networks, the next three (MAGIC.4, MAGIC.5, MAGIC.6) were used to improve the connection between unlinked networks, and the last four (MAGIC.7 to MAGIC.10) connected the first four larger energy components. For this work, the Effective Hamiltonian wavenumber values by 16AmLoPi [72] were utilized as magic numbers, which are listed in Table 2.

4.2. MARVEL energy uncertainties

MARVEL calculates energy uncertainties using the input transition uncertainties. In addition to this, when utilized without the bootstrap method, MARVEL yielded an average energy uncertainty of 0.0036 cm^{-1} based purely on the stated input uncertainties. However, when the bootstrap method is applied, the average energy uncertainty increases slightly to 0.0049 cm^{-1} suggesting that the input uncertainties are too low for the cases of polyad 0, 1, and 2. This is shown in Fig. 5 and the mean energy uncertainty per polyad is presented in Table 5.

5. Conclusions and future work

In this paper, we endeavored to compile a thorough database of published experimental methane spectra up to July 2023 which we

Table 3

Experimental data for $^{12}\text{C}^1\text{H}_4$ used in our analysis. Wavelength range and mean line position uncertainty are given in cm^{-1} , A/V: number of available transitions/number of validated transitions, given: an uncertainty is given in the source, CD: an uncertainty is not given in the paper and we used an uncertainty based on combination differences, increased: we increased the uncertainty given in the source. See Section 3.1 for comments on individual sources.

Source	Polyad band	Wavenumber range cm^{-1}	A/V	Mean Unc cm^{-1}	Unc Origin
80ItOz [147]	P_0-P_0	0.00027	1/1	6.00E-13	given
73Curl [148]	P_0-P_0	0.01–0.04	2/2	6.60E-07	given
85Dreizler ^a [70]	P_0-P_0	0.16–0.76	7/7	1.00E-03	CD
85OlAnBa.CH4 [149]	P_0-P_0	0.26–0.51	27/27	2.10E-06	given
73HoGeOz [150]	P_0-P_0	0.3–0.5	3/3	3.30E-06	given
92PuWe [90]	P_0-P_0, P_2-P_2	0.3–0.6	18/18	9.30E-07	given
87OlBaHi [151]	P_1-P_1	0.4–0.6	6/6	1.50E-05	given
73TaUeSh [152]	P_2-P_2	0.5	1/1	3.30E-07	given
75HoGeOz [153]	P_0-P_0	0.6–0.64	3/3	6.60E-06	given
87HiLoCh [154]	P_1-P_1	4–9	14/14	2.80E-06	given
MAGIC ^d	P_0-P_0	10.48–3104.76	10/10	6.00E-03	
17BrCuHi [155]	P_0-P_0, P_1-P_1	37.5–84.5	10/10	8.90E-06	given
10BoPiRo [156]	P_0-P_0, P_1-P_1	59–276.3	193/193	3.00E-03	CD
09AlBaBoBrDyadGs [70]	P_1-P_0	1088.3–1751.8	1189/1182	5.00E-03	increased
16AmLoPi [72]	P_1-P_0, P_2-P_1	1100.4–1488	5062/3846	2.70E-03	given
10SmBePr [157]	P_1-P_0	1159.3–1494.6	435/434	7.20E-04	increased
82JeRo [76]	P_1-P_0	1170.4–1316.9	49/49	1.00E-02	CD
09AlBaBoBrPentDyad [70]	P_2-P_1	1189.3–1930.4	1046/1046	1.00E-03	increased
22GeHjBo [158]	P_1-P_0, P_2-P_1	1250.4–1378.5	712/712	1.90E-02	given
79PiDu [74]	P_1-P_0	1259.5–1306.6	134/128	1.20E-02	increased
98BrKaRu [91]	$P_1-P_0, P_2-P_1, P_3-P_2, P_4-P_3$	1260–1333.2	295/287	2.00E-03	increased
93HiBaBr [159]	$P_2-P_1, P_3-P_2, P_1-P_0$	1262.1–1275.5	40/40	1.50E-03	given
79ReCa [160]	P_1-P_0	1292.5–1306.8	89/81	1.00E-02	increased
75ChBe ^c [125]	P_1-P_0	1359.2–1770.2	196/193	6.10E-02	increased
92HiLoBr [161]	P_3-P_0, P_2-P_1	1382.8–4652.2	434/431	7.00E-03	increased
21LiDiLi [162]	P_1-P_0	1396.5–1397.1	10/10	1.00E-03	CD
14SmBePr [163]	P_1-P_0	1398.5–1645	154/150	5.40E-05	given
09AlBaBoBrOctadDyad [70]	P_3-P_1	2334.1–3298.4	1707/1707	2.00E-03	increased
09AlBaBoBrPentadGs [70]	P_2-P_0	2466.5–3274.2	2246/2246	5.00E-03	increased
97MaBeSa ^c [79]	P_4-P_2, P_4-P_0	2868.3–6057.2	76/60	8.70E-03	given
00FeChJoBr [93]	P_2-P_0	2884.3–3149.04	258/257	2.00E-04	given
18KoMaEs [116]	P_2-P_0	2885–3122.8	36/36	1.10E-05	given
13AbIwOk [104]	P_2-P_0	2894.9–3104.6	150/150	1.40E-07	given
11BaGiSw [164]	P_2-P_0	2905.6–3048.2	132/132	9.20E-06	given
92BeSaCa ^c [128]	P_2-P_0	2910.6–2920.7	83/81	1.00E-03	given
76Pine [71]	P_2-P_0	2916.2–3122.8	155/149	5.00E-04	given
79DaPiRo [73]	P_2-P_0	2937.2–3067.3	30/30	5.00E-04	CD
11OkNaIw [165]	P_2-P_0	2943.2–3018.9	54/54	7.70E-08	given
09TaKoSa [166]	P_2-P_0	2947.6–2958.7	12/12	3.60E-07	given
85ChKlNi [80]	P_2-P_0	2947.8–2947.9	3/3	1.50E-07	given
98ErTyKr [92]	P_2-P_0	2947.8	1/1	6.60E-09	given
72EvDaWe [80]	P_2-P_0	2947.9	1/1	1.60E-06	given
76BlEdJo [84]	P_2-P_0	2947.9	1/1	1.40E-06	given
79DoKoTa [80]	P_2-P_0	2947.9	1/1	3.30E-07	given
80ClDaRu [80]	P_2-P_0	2947.9	1/1	4.60E-07	given
80KnEdPe [85]	P_2-P_0	2947.9	1/1	1.00E-07	given
81DoKoTa [80]	P_2-P_0	2947.9	1/1	4.60E-08	given
82ChGoKl [80]	P_2-P_0	2947.9	1/1	1.00E-07	given
92KrLiWe [88]	P_2-P_0	2947.9	1/1	6.60E-09	given
23RiTeJo [167]	P_2-P_0	3009.6–3014.8	12/12	4.70E-04	given
19Pine [168]	P_2-P_0	3012.5–3018.9	66/66	3.90E-05	increased
21OkInOk [123]	P_4-P_2	3017.7–3018.9	10/10	7.10E-08	given
21FoRuSi (pump) [124]	P_2-P_0	3028.75	1/1	5.00E-04	CD
83DeFrPr [77]	P_4-P_2	3034.6–3068.0	4/1	1.00E-01	given
91Jouvard [130]	P_2-P_0	3063.6–3070.2	37/37	1.00E-03	CD
91MiLaSt ^c [129]	P_2-P_0	3063.6–3066.9	13/13	5.70E-04	given
02GrFiTo [169]	P_2-P_0	3182.9–3224.6	100/85	4.20E-04	given
09AlBaBoBrOctadGs [70]	P_3-P_0	3518.8–4746.6	7910/7907	5.00E-03	increased
19RoNiTh [170]	P_3-P_0, P_4-P_1	3760.2–4100	6847/6798	5.00E-03	CD
01HiRoLoTo ^b [171]	P_3-P_0	3797–4099.7	206/205	1.00E-04	CD
01HiRoLoToa [171]	P_3-P_0	3848.6–3871.8	96/90	7.00E-04	given
88Brown [89]	P_3-P_0	3876.7–3890.9	12/10	1.10E-04	given
22RoNiMa [172]	P_3-P_0, P_4-P_1	4100–4300	11341/11304	7.50E-03	CD
05PrBrMa [97]	P_3-P_0	4100.4–4634.9	1432/1401	2.80E-04	increased
17HaPrNi [113]	P_3-P_0	4300–4491.1	59/55	1.00E-04	CD
17HaPrNi(2) [113]	P_3-P_0	4300–4481.1	102/102	6.20E-04	given
20NiRoTh [173]	P_3-P_0, P_4-P_1	4300–4600	9749/9734	9.00E-03	increased
15DeBeSm [174]	P_3-P_0	4499.5–4628.9	307/305	3.90E-04	given
13DaNiTh [175]	P_2-P_0	4600.4–4868.8	1570/1560	1.00E-03	CD
14NiThRe [176]	P_4-P_0	4801.2–5299.9	2725/2715	3.00E-03	CD
13NiBoWe [110]	P_1-P_0	4885.7–6204.6	1194/1170	1.00E-03	given
01RoHiLo [177]	P_4-P_0	4909.4–5271.8	189/184	1.00E-03	CD

(continued on next page)

Table 3 (continued).

Source	Polyad band	Wavenumber range cm ⁻¹	A/V	Mean Unc cm ⁻¹	Unc Origin
18MaZnCa [178]	P_4-P_0	4975.8–4984.6	32/32	2.00E–03	increased
17NiThDa [179]	P_4-P_0	300.1–5549.9	2847/2845	1.50E–03	CD
18NiThDa [180]	P_4-P_0, P_3-P_2	5550–5814.3	3467/3446	1.00E–03	CD
10NiLyMi [99]	P_4-P_0	5550.8–6204.6	2550/2549	5.00E–03	given
15NiLyMi [51]	P_4-P_0	5550.8–6204.6	2069/2067	5.00E–03	given
09LyNiPe [181]	P_4-P_0	5556.3–6180.7	452/443	1.00E–03	CD
98GeHeHi [182]	P_4-P_0	5577.4–6076.1	22/15	1.00E–03	CD
18GhMoKa [114]	P_4-P_0	5695.3–5849.9	2079/2049	1.50E–03	given
13CaLeWa [106]	P_4-P_0	5855–6243.4	3436/3414	1.50E–03	CD
13ZoGiBa [111]	P_4-P_0	5870.6–6137.6	348/341	1.20E–03	given
23DuViGa [183]	P_3-P_2, P_7-P_3	5909.9–6215.9	22/19	5.00E–03	CD
21FoRuSi [124]	P_6-P_2	5910.8–6056.5	8/8	1.00E–04	given
21FoRuSiVtype [124]	P_4-P_0	5972–6047	24/24	4.90E–05	given
19YaLiFe [120]	P_4-P_0	6076.1	1/1	1.20E–06	given
16DeMaRe [112]	P_4-P_0	6076.9–6078	12/12	3.80E–05	given
18GoPrKa [115]	P_4-P_0	6076.9–6077.1	6/6	1.80E–07	given
20YaLiPl [122]	P_4-P_0	6076.9–6077.1	6/6	6.30E–05	given
18YaLiFe [118]	P_4-P_0	6077–6077.2	2/2	9.80E–07	given
19LiYaFe [119]	P_4-P_0	6105.6–6107.2	11/11	1.70E–07	given
11NiThRe [184]	P_5-P_0	6256.3–6788.9	717/717	2.40E–03	CD
12CaWaMo [100]	P_3-P_0	6256.3–6788.9	2514/2497	1.50E–03	given
16ReNiCa [109]	P_5-P_0	6294–6780.4	376/376	1.00E–03	CD
16NiReTa [108]	P_3-P_0	6539.4–6799.9	2445/2445	1.00E–03	CD
02HiQu [94]	P_3-P_0	7478.6–7552.9	23/22	1.00E–03	given
05Brown [96]	P_3-P_0	7478.6–7563.9	26/25	1.00E–03	increased
09ScKaGa [98]	P_3-P_0	7478.6–7564	27/26	1.00E–03	CD
12TaQu [95]	P_5-P_0	7509.5–7564	21/21	1.00E–03	given
19NiPrRe [185]	P_6-P_0	8736.2–9159.1	329/329	5.00E–03	increased

^a Published in [70] from private communication.

^b Lines assigned by [170].

^c Raman lines.

^d Refer to Section 4.1.

used to extract precise empirical rovibrational energy levels. Our primary objective moving forward is to employ this set of energy levels in order to improve the upcoming MM ExoMol line list for methane [56], and generate a high-resolution line list for $^{12}\text{C}^{14}\text{H}_4$ that can be used for high-resolution exoplanetary and other studies.

The 82173 measured transitions we assembled from 96 articles yielded 23292 energy levels through the MARVEL procedure. With the bootstrap method, 66.8% of MARVEL energy levels have an uncertainty lower than or equal to 0.005 cm⁻¹.

We gathered a plethora of observational unassigned spectra, as well as assigned spectra with a different convention. As mentioned in Section 3.1 we were able to attribute assignments to a large number of such transitions but we still have a large number of experimental sources with transitions that we aim to assign with our final line list. Many of the sources we used successfully also contain a significant number of unassigned lines. In addition, the following sources reported unassigned transitions that we aim to assign as a next step.

12HaBeMi [49] published 324406 unassigned measured lines ranging from 1067 to 3350 cm⁻¹ belonging to the dyad, pentad, and octad bands, as well as in hot bands.

85HiLoBr [282] reported 13 $v_3 - v_4$ assigned lines ranging from 1568 to 1932 cm⁻¹ where a different convention is used for the counting numbers.

03NaBe [283] measured methane spectra in the 2000–6400 cm⁻¹, tetradecad, and octad region. They published a number of very accurate lines around 3038 cm⁻¹ that can be assigned with our final line list.

82HuLoRo [284] published spectra in the pentad region and in the 2930–3250 cm⁻¹ range. Assignments are given for the observed lines without the lower state's counting number.

15HaBeBa [52] reported high-temperature line position measurements and provided 15 lines around 2980 cm⁻¹.

83PiChGu [285] reported 2250–3260 cm⁻¹ lines in the pentad region assigned with a different convention for the quantum numbers.

84MaFrPr [286] and **85MaFrPr** [287] reported partly assigned $3v_3 - 2v_3$ transitions in the range 2940–2995 cm⁻¹ and 2890–2935 cm⁻¹ respectively.

97Pine [288] reported measured lines in the pentad region and the range 3028–3122 cm⁻¹ which are partly assigned, without upper state counting number.

21YoBeDu [289] published partly assigned pentad lines in the range 2750–3200 cm⁻¹.

72HuPoVa [290] reported partly assigned octad transitions in the 4136–4288 cm⁻¹ range.

10CaWaKa [291] reported 12865 unassigned measured icosad transitions.

90Margolis [292] reported partly assigned transitions in the tetradecad region and in the range 5597–5635 cm⁻¹.

18GhVaMo [293] reported unassigned tetradecad lines in the 5693–6257 cm⁻¹ region.

08KaGaRo [294] published unassigned transitions in the 5850–7700 cm⁻¹ region.

12GaChZh [295] reported tetradecad lines in the 6038–6050 cm⁻¹ region.

20YaLiPlb [296] reported one very accurate measured line at around 6077 cm⁻¹ which was not assigned.

98BoRePl [297] published unassigned 5500–6180 cm⁻¹ lines.

13CaLeMo [121] reported unassigned tetradecad lines from 5855 cm⁻¹ to 6183 cm⁻¹.

88Margolis [298] reported unassigned or fully assigned transitions in the tetradecad region and the range 5500–6180 cm⁻¹.

09GaKaCa [299] reported $2v_3$ unassigned transitions in the 5852–6181 cm⁻¹ range.

08FrWaBu [300] reported measured tetradecad lines unassigned or partly assigned in the 5860–6185 cm⁻¹ region.

81BrToHu [301] published unassigned lines in the $v_2 + v_3 - v_2$ band.

22VoKaCa [302] reported lines in the 6015–6115 cm⁻¹ region partly assigned.

23OlSiRu [303] measured and partly assigned transitions in the $3v_3$, v_3 bands.

12WaMoKa [304] reported unassigned icosad lines in the 6717–7589 cm⁻¹ region.

Table 4
Experimental $^{12}\text{C}^1\text{H}_4$ papers not used in MARVEL analysis.

Source	Wavenumber range cm^{-1}	Comments
48NePlBe [186]	5900–6200	old measurements
52BoThWi [187]	2700–3200	low accuracy
55FeRoWe [188]	1300–1800	old measurements
60RaEaSk [189]	5983–6115	not fully assigned
65MoGaMo [190]		no measurements provided
65Moret [191]		theoretical paper
66HeMoGo [192]		low accuracy
66McDowell [193]		low accuracy
70ClSt ^a [136]		no measurements provided
70HeHuAn [194]	2884–3141	different assignments, low accuracy
70OzYiKh [195]		no lines provided
71HuDa [196]	2884–3141	different assignments, low accuracy
71HuPo [197]	1225–1376	different assignments, low accuracy
72BaSuHu [198]	2884–3139	low accuracy
72Bobin [199]	5891–6107	not fully assigned
72Botineau [75]	1225–1400	not accurate enough
72RoOzKu [200]	100–180	no lines provided
73BeFaCh [201]		no lines provided
73BoFo [202]	2840–3167	no new measurements
73CaDe [203]		not accurate J assignments
73CuOkSm [204]		no new measurements
73DaMa [205]		no lines provided
73Susskind [206]		no new measurements
75Berger [207]	1271–1311	different assignments, low accuracy
75BoHi [208]		different assignments, low accuracy
75Champion [137]	1481–1747	theoretical paper
75RoOz [209]		no new measurements
75TaDaPo [210]	3019–3021	different assignments
76GrRo [126]		no new measurements
76HaBoUe [211]		no new measurements
77AlKoSm [212]		no new measurements
77Berger ^a [140]		different assignments
77Champion [127]		calculated lines
77ToBrHu [213]	2862–3000	different assignments
78BoGu [214]	4157–4425	different assignments, low accuracy
78ChHuSc [215]		no new measurements
78HuBrTo [216]	2700–2862	unassigned lines
78MaHeBy ^a [138]		no lines provided
78OwPaDo ^a [135]	2916–2918	not fully assigned
78OzRo [217]	94–145	not accurate enough
79BlGoLu [218]	1120–1800	not accurate enough
79BoBr [219]		no lines provided
79GrRo [220]		no new measurements
79GrRoPi [221]		not fully assigned
79KoPrSm [132]		no measurements provided
80ChPiBe [141]		no new measurements
80HiDeCh [222]		low accuracy
80Jennings [223]		no measurements provided
80OrRo [224]		no new measurements
80VaEsOw [225]		no measurements provided
81GhHeLo [226]	2832–3018	not accurate enough
81HuBrTo [227]		difficult to scan table
81OzGeRo [228]	0.00026–0.64	no new measurements
81Robiette [229]		no new measurements
81ToBrHu [230]	2385–3200	no lines provided
82BrRo [231]		no new measurements
82BrToRo [232]	2700–3000	difficult to scan
82LoBrRo [144]	2460–2675	different assignments
82LuPiPiCh [233]		no line position measurements
82RaCa [234]		no new measurements
82PoPaCh [235]	2250–3250	observed energy levels
83BrMaNo [236]		no new measurements
83FrIFi ^a [142]	2916–2917	different assignments
83VaGiVa.a [237]		unassigned lines
85BrTo [238]		no line position measurements
85GrLa [133]		no lines provided
85ThFaKo ^a [134]		not accurate enough
86KeCoSm [239]		no new measurements
87Kim [240]		intensity measurements
86TyChPi [241]		no new measurements
89BrLoHi [242]		no new measurements
89VaCh [243]	1270–1317	not fully assigned
90VaCh [244]	1332–1350	no new measurements

(continued on next page)

Table 4 (continued).

Source	Wavenumber range cm^{-1}	Comments
91RoCh [245]		no new measurements
92BrMaCh [246]		no new measurements
92Pine [247]	3012–3018	we used the lines from [168]
92SaCaDo ^a [131]	2916–2917	no new measurements
92SmRiDe [248]		no new measurements
96OuHiLo [249]		no new measurements
98WeCh [250]		theoretical paper
00MeDoMe [251]	2942–2982	not fully assigned
01NaMi [252]	3009–3039	not fully assigned
02BrCa [253]	10635–13300	no lines provided
05GhBu [254]		no new line measurements
05JoChSa [143]	1200–5500	no lines provided
05MoChVa [255]	2914–2922	no new line measurements
06BoMeMa [256]	2931–2996	no new line measurements
06BoReLo [69]		theoretical paper
07JoGaCh ^a [145]	2905–2925	no lines provided
07RuWoHa [257]	2990–3070	not fully assigned
07WiOrOz [258]	0.06–0.24	no lines provided
10HoSkSa [259]		not fully assigned
10TrHaTo [260]	6000	no new line measurements
10ZiWh [261]		theoretical paper
12SaAuPi [262]	59–288	no new line measurements
12YuFaYa [263]		no new line measurements
13ThDaAn [3]		no new line measurements
13TyTaRe [117]		theoretical paper
14ReNiTY [264]		theoretical paper
14UlBeAl [67]	1000–12500	no lines provided
15LiWaTa [265]		no new line measurements
15MaKcVa ^a [139]	882–3434	unassigned
15ReNiTy [103]		theoretical paper
17ReNiTy [53]		theoretical paper
18NiPrRe [266]		theoretical paper
18Petrov [267]		no new line measurements
18ReNiBe [268]	0–3400	theoretical paper
19BuAmBe [269]		no lines provided
19DeGhHo [270]		no new line measurements
19GhHeBe [271]		no new line measurements
19KiMaPe [272]		no new line measurements
20GiNaTu [273]		no new line measurements
20HaGoRe [55]		theoretical paper
20PeMaZa [274]		theoretical paper
21CuHiMo [275]		no new line measurements
21FaArVa [276]		no new line measurements
21FoRuSib [277]	3028–6058	no new data
21EsFa [278]	2884–2969	no new line measurements
22ZhXuWa [279]	3225.8–3857.1	no lines provided
23MaThCa [280]		no lines provided
23VaDeKa [281]		no new line measurements

^a Raman lines.

Table 5

Summary of the MARVEL energies. MU/MUB: The Mean Energy Uncertainty before (MU) and after bootstrap (MUB).

Polyad	Energy range cm^{-1}	Number of energy levels	Max J	MU/MUB.
P_0	0–3628.25	247	26	0.005/0.01
P_1	1310.7–5054.83	1088	27	0.005/0.01
P_2	2587.04–6239.03	3154	27	0.005/0.009
P_3	3870.48–7017.60	7708	23	0.005/0.006
P_4	5121.72–7417.90	8232	18	0.002/0.002
P_5	6377.52–7903.64	2528	15	0.001/0.001
P_6	8562.46–9629.88	333	10	0.005/0.005
P_7	9832.06–9986.23	2	4	0.005/0.005

21MaYuSu [305] reported unassigned icosad lines in the 6770–7570 cm^{-1} region.

09ScKaGa [98] reported unassigned icosad lines in the 7351–7655 cm^{-1} region.

05Brown [96] published observed lines in the range 6770 to 9111 cm^{-1} .

19WoBeRe [306] published 5200–9200 cm^{-1} unassigned lines belonging to the tetradecad, icosad, and triacodad regions.

13MaPrMo [307] reported 654 icosad transitions in the range 7040–7378 cm^{-1} partly assigned or unassigned.

11MoKaWa [308] published unassigned spectra in the 7541–7919 cm^{-1} range.

19WoBeRe [306] reported unassigned measured transitions in the tetradecad, icosad, and triacodad and in the range 5200–9200 cm^{-1} .

96SiOb [309] provided unassigned spectra from 7128 to 7373 cm^{-1} .

15BeKaCa [310] reported unassigned measured spectra in the range 7908–8345 cm^{-1} .

80PiHiBe [311] reported partly assigned $3\nu_3$ lines in the range 9000–9155 cm^{-1} .

18SeSiLu [312] reported unassigned 9057–9167 cm^{-1} lines.

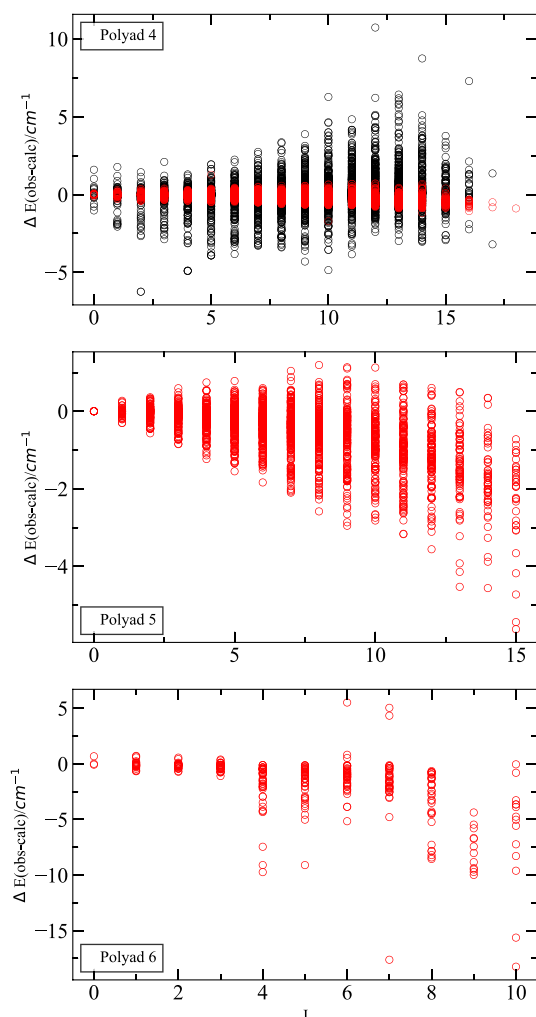


Fig. 4. Difference between the MARVEL energies (obs) and the a. Effective Hamiltonian by [72] (black) b. Variational calculations (red) by [53].

¹⁵BeLiCa [313] reported triad transitions in the 9028–10435 cm^{-1} region.

⁹³BoBoLi [314] reported three partly assigned measured lines in the range 11258–11309 cm^{-1} .

⁰⁷LuGo [315] reported observed transitions at around 11900 cm^{-1} belonging to the $\nu_1 + 3\nu_3$ band.

⁹⁵TsSa [316] reported $3\nu_1 + \nu_3$ unassigned lines.

⁹⁴BoLiRe [317] published $3\nu_1 + \nu_3$ transitions in the range 11220–11313 cm^{-1} mostly unassigned.

⁹⁵CaPeJo [318] published partly assigned transitions in the range 11245–11312 cm^{-1} .

⁹³LuLoGa [319] measured unassigned lines in the 11539–12756 cm^{-1} region.

²²Lucchesini [320] reported 112 unassigned lines in the heptacontad region at around 12700 cm^{-1} .

⁹⁵SiOb [321] reported 13470–14025 cm^{-1} unassigned lines.

⁹¹CaChSt [322] reported $4\nu_1 + \nu_3$ lines in the range 13702–13887 cm^{-1} .

Finally, we note that **²³CaKaVaTu** [323] very recently published an unassigned absorption spectrum in the range 10800–14000 cm^{-1} .

CRedit authorship contribution statement

Kyriaki Kefala: Writing – original draft, Validation, Formal analysis, Data curation. **Vincent Boudon:** Methodology, Formal analysis.

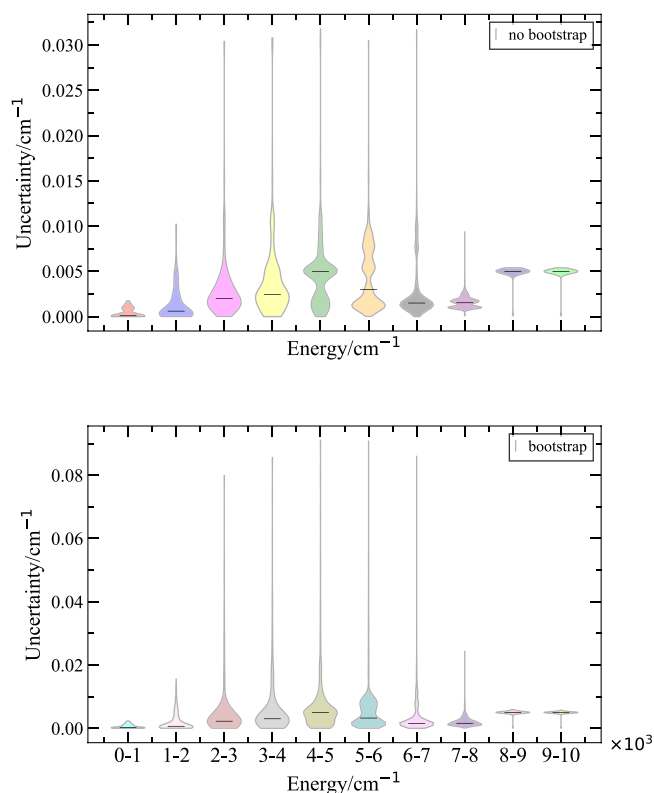


Fig. 5. The MARVEL energy uncertainties with respect to the energy.

Sergei N. Yurchenko: Writing – review & editing, Validation, Methodology. **Jonathan Tennyson:** Writing – review & editing, Supervision, Funding acquisition, Conceptualization.

Declaration of competing interest

The authors declare no competing financial interests.

Data availability

All data given in the supporting material.

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Appendix A. Supplementary material

The MARVEL transition, energy, and segment files are provided as supplementary material as well an analysis of the outlying levels discussed in Section 4.

Supplementary material related to this article can be found online at <https://doi.org/10.1016/j.jqsrt.2024.108897>.

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