Water flow through sediments and at the ice-sediment interface beneath Sermeq Kujalleq (Store Glacier), Greenland

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Abstract

Subglacial hydrology modulates basal motion but remains poorly constrained, particularly for soft-bedded Greenlandic outlet glaciers. Here, we report detailed measurements of the response of subglacial water pressure to the connection and drainage of adjacent water-filled boreholes drilled through kilometre-thick ice on Sermeq Kujalleq (Store Glacier). These measurements provide evidence for gap opening at the ice-sediment interface, Darcian flow through the sediment layer, and the forcing of water pressure in hydraulically-isolated cavities by stress transfer. We observed a small pressure drop followed by a large pressure rise in response to the connection of an adjacent borehole, consistent with the propagation of a flexural wave within the ice and underlying deformable sediment. We interpret the delayed pressure rise as evidence of no pre-existing conduit and the progressive decrease in hydraulic transmissivity as the closure of a narrow (~1.5 mm) gap opened at the ice-sediment interface, and a reversion to Darcian flow through the sediment layer with a hydraulic conductivity of ≤ 10⁻⁶ m s⁻¹. We suggest that gap opening at the ice-sediment interface deserves further attention as it will occur naturally in response to the rapid pressurisation of water at the bed.

1. Introduction

A list of symbols is presented in Appendix A.

The nature of subglacial hydrology and basal motion on ice masses underlain by soft sediments are central questions in ice dynamics (e.g., Clarke, 1987; Murray, 1997; Tulaczyk and others, 2000). However, despite abundant evidence for subglacial sediments beneath fast-moving outlet glaciers and ice streams draining the Greenland and Antarctic ice sheets (e.g., Alley and others, 1986; Blankenship and others, 1986; Christianson and others, 2014) and mountain glaciers (e.g., Humphrey and others, 1993; Iverson and others, 1995), soft-bedded processes remain poorly constrained (Walter and others, 2014; Alley and others, 2019). Water flow in a soft-bedded subglacial environment has been hypothesised to occur via: Darcian flow through permeable sediments (Clarke, 1987); sheet flow at the ice-sediment interface (e.g., Weertman, 1970; Alley and others, 1986; Flowers and Clarke, 2002; Creyts and Schoof, 2009); and concentrated flow in channels cut into the ice, and canals eroded into the sediment (Walder and Fowler, 1994; Ng, 2000). Drainage through gaps opened and closed dynamically at the ice-sediment interface by turbulent water flow at high pressure has also been proposed as an explanation for the rapid drainage of boreholes (Engelhardt and Kamb, 1997; Kamb, 2001) and both supra- and pro-glacial lakes (Sugiyama and others, 2008; Tsai and Rice, 2010, 2012; Hewitt and others, 2018). Direct evidence for gap-opening at the ice-sediment interface is limited to three observational studies (Engelhardt and Kamb, 1997; Lüthi, 1999; Iverson and others, 2007). However, despite support from detailed analytical modellling (Schoof and others, 2012; Rada and Schoof, 2018) dynamic gap opening has yet to be fully developed for larger-scale numerical models of subglacial hydrology.

The water-saturated sediment layer beneath a soft-bedded ice mass can be approximated as an aquifer confined by an overlying ice aquiclude (e.g., Lingle and Brown, 1987; Stone and Clarke, 1993). And, with careful adaptation, standard hydrogeological techniques can be used to estimate subglacial aquifer properties such as transmissivity, conductivity, diffusivity and storativity. These include slug tests, where the borehole water level is perturbed by the insertion and sudden removal of a sealed pipe of known volume (Hodge, 1979; Stone and Clarke, 1993; Iken and others, 1996; Kulessa and Hubbard, 1997; Stone and others, 1997; Kulessa and Murray, 2003; Kulessa and others, 2005); packer tests where the borehole is sealed near the surface and subsequently rapidly pressurised with air (Stone and Clarke, 1993; Stone and others, 1997), and pumping tests where the borehole hydraulic head is monitored in
response to water injection or extraction (e.g., Engelhardt, 1978; Engelhardt and Kamb, 1997; Iken and Bindschadler, 1986; Lüthi, 1999). Borehole drainage on connection with the bed (hereafter ‘breakthrough’), and the recovery to equilibrium water levels have also been used to determine subglacial aquifer properties (e.g., Stone and Clarke, 1993; Engelhardt and Kamb, 1997; Stone and others, 1997; Lüthi, 1999). During breakthrough events the water level in the initially water-full borehole either: (i) drops rapidly to a new equilibrium level some tens of metres below the surface, (ii) does not drop at all, or (iii) drops slowly, or rapidly, to a new equilibrium level after a delay of minutes to days, with the variability in response usually explained in terms of the connectivity of the subglacial drainage system (e.g., Smart, 1996; Gordon and others, 2001). The hydraulic conductivity of a subglacial sediment layer has also been derived from the propagation and attenuation of diurnal subglacial water pressure waves (e.g., Hubbard and others, 1995), and from numerical modelling of the pressure peaks induced when pressure sensors freeze in (Waddington and Clarke, 1995). To date, the application of borehole response tests to marine-terminating glaciers in Greenland is limited to a single study (Lüthi, 1999), presumably due to the challenges of adapting groundwater techniques to the ice-sheet setting.

The application of hydrogeological techniques requires a number of simplifying assumptions. Many techniques are fundamentally based on Darcian flow and inherently assume that the aquifer is isotropic and homogeneous; conditions that may rarely be met in the subglacial environment. Water in ground-water investigations is typically slow and assumed to be Darcian. While this may hold for low-velocity water flow through subglacial sediments, the discharge rates during borehole breakthrough events mean turbulent flow is likely in the vicinity of the borehole base (e.g., Stone and Clarke, 1993). Further complications arise due to the greater density of water than ice, overpressurising the ice at the base of water-filled glacier boreholes with the potential to raise the ice from its substrate permitting water to flow through the gap created. (Overpressure here being water pressure in excess of the ice overburden pressure). Previous studies have attempted to determine the widths of such gaps (Weertman, 1970; Engelhardt and Kamb, 1997; Lüthi, 1999; Iverson and others, 2007).

Ice boreholes provide direct access to the subglacial environment allowing sensor installation and borehole response tests. Here, we analyse borehole response tests conducted on Sermeq Kujalleq (Store Glacier) in West Greenland during summer 2019. The response tests included breakthrough events, which occurred consistently when boreholes intersected the ice-sediment interface, constant-rate pumping tests undertaken as water was pumped into the borehole as the drill stem was raised to the surface, and recovery tests following removal of the stem. The results provide insights into subglacial hydrological conditions and permit estimation of the hydraulic transmissivity and conductivity of the subglacial drainage system.

2. Methods

2.1 Field site

Sermeq Kujalleq (Store Glacier) is a major fast-moving outlet glacier of the Greenland Ice Sheet draining an ∼34,000 km² catchment area (Rignot and others, 2008) into Ikerasak Fjord – a tributary of Uummannaq Fjord. (Note that as several glaciers share the same name – and for continuity with previous literature – we give the English glacier name in brackets after the official Greenlandic name.) In summer 2019, we used pressurised hot water to drill seven boreholes on Sermeq Kujalleq (Store Glacier) at site R30 (N70° 34.0’, W050° 5.2’) located in the centre of the drained bed of supraglacial lake L028 (Fig. 1a; Table S1).

R30 lies 30 km from the calving front at 863 m a.s.l. and is within the ablation area; there was no winter snow or firn present during the drilling campaign. Ice flow measured by a Global Navigation Satellite System (GNSS) receiver averaged 521 m a⁻¹ in the SSW direction (217° True) between 9 July and 16 September 2019. The surface slope was calculated as 1.0° from linear regression of the ArcticDEM digital elevation model (Porter and others, 2018) over a distance of ten ice thicknesses (10 km). Lake L028 drained via hydraulic fracture on 31 May 2019 (Chadley and others, 2019b) forming two major moulins (each of diameter ∼6 m) located within 200 m of the drill site (Fig. 1b). Borehole-based Distributed Acoustic Sensing (DAS) in BH19c provides evidence for up to 37 m of consolidated subglacial sediment at R30 (Booth and others, 2020), while seismic reflection surveys at site S30 (8 km to the south-east of R30; Fig. 1a) revealed up to 45 m of unconsolidated sediment overlying consolidated sediment (Hofstede and others, 2018). Borehole-based investigations of englacial and basal conditions at S30 reported low effective pressures (180 – 280 kPa), an absent or thin (< 10 m) basal temperate ice layer, and internal deformation concentrated within the lowermost 100 m of ice, below the transition between interglacial (Holocene) and last-glacial (Wisconsin) ice (LGIT; Doyle and others, 2018; Young and others, 2019). At R30, Distributed Temperature Sensing (DTS) reveals a 70 m-thick basal temperate ice layer, the LGIT at 889 m depth and a steeply curving temperature profile with a minimum ice temperature of ∼21.1°C near the centre of the ice column (Law and others, 2021).

2.2 Hot water drilling

Boreholes were drilled using a hot water drill system similar to that described in Makinson and Anker (2014). Pressurised, hot water (110.0 MPa; ~80°C) was provided by five pressure-heater units (Kärcher HDS1000DE) at a regulated flow rate of 751 min⁻¹, through a 1,350 m long, 19.3 mm (0.75”) bore hose. A load cell and rotary encoder recorded the load on the drill tower and the hose length below the surface at 0.5 Hz with a resolution of 1 kg and 0.1 m, respectively (Figs S1–S3). Borehole logging to a depth of 325 m indicates that the hot water drilling system consistently drills boreholes that are within 1° of vertical (Hubbard and others, 2021).

Boreholes (BH) were named by year and by letter in chronological order of drilling, with BH19a the first borehole drilled in 2019 (Table S1). Boreholes were drilled in two clusters with the first (BH19a, b, c and d) separated from the second (BH19e, f and g) by 70 m (Fig. 1b). Seven boreholes were drilled in 2019 with three reaching the ice-sediment interface at depths of 1,043 m (BH19c), 1,022 m (BH19e) and 1,039 m (BH19g), giving a mean ice thickness of 1,035 m and a mean elevation of the glacier sole of ∼172 m a.s.l. (Table 1). Four boreholes were terminated above the ice-sediment interface (see Table S1). Prior to breakthrough boreholes were water-filled to the bare ice surface, with excess water supplied by the pressure-heater units overflowing from the top of the borehole.

To reduce overall drilling duration and produce a more uniform borehole radius (0.06 m four hours after termination of drilling), we optimised drilling speed using the numerical borehole model of Greenler and others (2014). The borehole model was constrained by ice temperature from site R29, 1.1 km distant (Hubbard and others, 2021, Fig. 1a), and a hose thermal conductivity of 0.24 W m⁻¹ K⁻¹. Borehole radius at the time of breakthrough was then estimated by re-running the model with the recorded drill speeds and the equilibrated ice temperature profile measured in BH19c at site R30 (Law and others, 2021). The mean borehole radius for BH19c, BH19e and BH19g output by the model at the time of borehole breakthrough was 0.07 m, with

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larger radii (mean of 0.10 m) in the lowermost 100 m of the ice column (Table A1) due to intentionally slower drilling as the drill approached the ice-sediment interface, together with the presence of temperate ice that was unaccounted for during initial model runs. The borehole model underestimated the near-surface (i.e. 0−100 m) borehole radius (r_s), possibly due to turbulent heat exchange that is not included in the model, so we use the radius at the water line calculated for BH19g (0.14 m) as r_s for all the borehole response tests (see Appendix B).

Analysis of the temperature time series recorded by DTS in BH19c (Law and others, 2021) shows that the boreholes rapidly froze shut. At 580 m depth, where the undisturbed ice temperature was −21.1°C, the temperature fell below the pressure-dependent melting temperature 3 h after drilling. Within warmer ice, refreezing was slower: at 920 m depth in BH19c, the ice temperature was −3°C and refreezing was complete after 5 d.

### Table 1. Key data for the boreholes that reached the bed. Variables h_0, p_w, and N were calculated for the reference period 36–60 h after each respective breakthrough, which was deemed representative of subglacial water pressure. A list of symbols is presented in Appendix A.

<table>
<thead>
<tr>
<th></th>
<th>BH19c</th>
<th>BH19e</th>
<th>BH19g</th>
<th>Mean</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ice thickness (m)</td>
<td>1,043.0</td>
<td>1,022.3</td>
<td>1,039.2</td>
<td>1,034.8</td>
</tr>
<tr>
<td>Piezometer offset (m)</td>
<td>0.05</td>
<td>0.1</td>
<td>0.4</td>
<td>0.18</td>
</tr>
<tr>
<td>Piezometer orthometric height (m a.s.l.)</td>
<td>−180.5</td>
<td>−159.6</td>
<td>−175.1</td>
<td>−171.7</td>
</tr>
<tr>
<td>Water-full overpressure (kPa)</td>
<td>921 ± 102</td>
<td>902 ± 100</td>
<td>917 ± 102</td>
<td>913 ± 101</td>
</tr>
<tr>
<td>Breakthrough time (UTC)</td>
<td>5 July 2019 02:54:36</td>
<td>12 July 2019 03:39:35</td>
<td>22 July 2019 08:07:23</td>
<td>n/a</td>
</tr>
<tr>
<td>Breakthrough volume (m³)</td>
<td>4.83</td>
<td>4.50</td>
<td>4.93</td>
<td>4.75</td>
</tr>
<tr>
<td>Peak load (kg)</td>
<td>199</td>
<td>180</td>
<td>214</td>
<td>198</td>
</tr>
<tr>
<td>Drill-indicated breakthrough depthc (m)</td>
<td>1031.0</td>
<td>1010.5</td>
<td>1017.3</td>
<td>1019.6</td>
</tr>
<tr>
<td>Drill-indicated maximum depthc (m)</td>
<td>1031.0</td>
<td>1013.3</td>
<td>1017.4</td>
<td>1020.6</td>
</tr>
<tr>
<td>Pump rate (l min⁻¹)</td>
<td>75</td>
<td>75</td>
<td>75</td>
<td>75</td>
</tr>
<tr>
<td>Pumping duration during raise (min)</td>
<td>140</td>
<td>140</td>
<td>118</td>
<td>133</td>
</tr>
<tr>
<td>Volume of water pumped during raise (m³)</td>
<td>5.0</td>
<td>5.0</td>
<td>4.5</td>
<td>4.8</td>
</tr>
<tr>
<td>Recovery time (h)</td>
<td>36.4</td>
<td>49.7</td>
<td>45.4</td>
<td>43.8</td>
</tr>
<tr>
<td>Initial water level depth (m)</td>
<td>78.1</td>
<td>72.9</td>
<td>79.8</td>
<td>76.9</td>
</tr>
<tr>
<td>h_0 (m)</td>
<td>773.0</td>
<td>771.1</td>
<td>775.9a</td>
<td>775.3</td>
</tr>
<tr>
<td>p_i (MPa)</td>
<td>9.310 ± 0.1</td>
<td>9.125 ± 0.1</td>
<td>9.276 ± 0.1</td>
<td>9.237 ± 0.1</td>
</tr>
<tr>
<td>p_w (% of p_i)</td>
<td>100.5 ± 1.1</td>
<td>100.6 ± 1.1</td>
<td>100.5 ± 1.1</td>
<td>100.5 ± 1.1</td>
</tr>
<tr>
<td>N (kPa)</td>
<td>−43 ± 102</td>
<td>−54 ± 102</td>
<td>−42 ± 102a</td>
<td>−46 ± 102</td>
</tr>
</tbody>
</table>

a Drill-indicated depths do not account for the elastic extension of the hose under load.
b Recorded in BH19e due to freeze-in of pressure transducer in BH19g.

### 2.3 Pressure measurements

Basal water pressures were recorded by vibrating wire piezometers (Geokon 4500SH) installed at the base of BH19c and BH19e and a current loop transducer (Omega Engineering Ltd. PX3319) installed at the base of BH19g. Pressure records from the Geokon 4500SH were zeroed with atmospheric pressure at the surface, temperature compensated using a high-accuracy thermistor in contact with the piezometer body, and calibrated using the manufacturer’s second-order polynomial to an accuracy of ±3 kPa, equivalent to ±0.3 m of hydraulic head. The pressure record
from the PXM319 current loop transducer (accuracy = ± 35 kPa, equivalent to ± 3.6 m of head) was calibrated using the manufacturer’s linear calibration and zeroed with atmospheric pressure at the surface. A pressure spike indicates that the ice surrounding the transducer installed in BH19g froze at 13.7 h post-breakthrough.

All pressure sensors were lowered until contact with the ice-bed interface was confirmed by the pressure ceasing to increase. The sensor was then raised slightly (piezometer offset: 0.05 – 0.4 m; Table 1) to prevent the piezometer from being dragged through the substrate. The borehole water level below the surface (that is the length of the uppermost air-filled section of the borehole) at installation was measured with a well depth meter, and by reference to distance markers on the piezometer cable. The final installation depth was determined by adding this water level to the depth recorded by the piezometer. The ice thickness \(H_i\) was calculated by adding the piezometer offset to the final installation depth. Borehole positions were surveyed on 22 July 2019 using a Trimble R9s GNSS receiver with 8 min long observations post-processed using the precise point positioning service provided by Natural Resources Canada (CSRS-PPP). Borehole surface elevation was converted to orthometric EGM96 geoid heights. To allow inter-comparison of pressure records from sensors installed at different depths below the surface, water pressure was expressed as hydraulic head \(h\), which represents the theoretical orthometric height of the borehole water level,

\[
h = \frac{P_w \rho_w g}{\rho_i g} + z,
\]

where \(\rho_w = 999.8 \text{ kg m}^{-3}\) is water density at \(0^\circ\text{C}\), \(g = 9.81 \text{ m s}^{-2}\) is gravitational acceleration and \(z\) is the orthometric height of the piezometer determined by subtracting the piezometer depth below the surface from the orthometric height of the borehole at the surface. Pressure was also expressed as the effective pressure \(N = p_i - p_w\) and the overpressure \(p_{o,i} = p_i - p_w\), the latter in respect of the excess pressure exerted at the base of water-filled boreholes due to the greater density of water than ice (Table 1). The ice-overburden pressure \(p_i\) was approximated for an inclined, parallel-sided slab of ice as

\[
p_i = \rho_i g H_i \cos \alpha,
\]

where \(\rho_i\) is the density of ice, \(H_i\) is the height of the overlying ice column, \(\alpha = 1.0^\circ\) is the mean surface and bed slope (see Section 2.1), and ice density was taken as \(\rho_i = 910 \pm 10 \text{ kg m}^{-3}\).

### 2.4 Temperature measurements

Temperature was measured using high-accuracy (± 0.05°C) thermistors (Littelfuse: PR502J2) at ~0, 1, 3, 5 and 10 m above the bed in BH19c and BH19e and also throughout the full ice column in BH19c using fibre-optic DTS (Law and others, 2021). Here we present temperature measurements recorded by the lowestmost thermistor in BH19c, which was mounted with the Geokon 4500SH piezometer. We calculated the pressure-dependent melting temperature

\[
T_m = T_{tp} - \gamma (p_i - p_w),
\]

where \(\gamma = 9.14 \times 10^{-8} \text{ K Pa}^{-1}\) is the Clausius–Clapeyron gradient determined from the basal temperature gradient (Law and others, 2021), and \(T_{tp} = 273.16 \text{ K}\) and \(p_w = 611.73 \text{ Pa}\) are the triple point temperature and pressure of water, respectively.

### 2.5 GNSS measurements of ice motion

Time series of horizontal and vertical ice motion were determined from dual frequency (L1 + L2) GNSS data recorded by a Trimble R7 receiver at 0.1 Hz and post-processed kinematically using Precise Point Positioning with Ambiguity Resolution (CSRS PPP-AB). The GNSS antenna was mounted on a 5 m long pole drilled 4 m into the ice surface at a location between the two clusters of boreholes (Fig. 1b). Rapid refreezing of the hole ensured effective coupling of the antenna pole with the ice. Small gaps (< 5 min) in the position record were interpolated linearly before a 6 h low pass Butterworth filter was applied. The filtered position record was differentiated to calculate velocity. The time series was then resampled to 10 min medians and a further 6 h moving average was applied to the velocity record. To prevent a shift in phase, phase-preserving filters and differentiation were used.

### 3. Borehole response tests

We analysed the response of borehole water pressure to the perturbations induced at breakthrough, during the continued pumping of water into the borehole while the drill stem and hose were raised to the surface, and also during the recovery phase after which borehole water pressure was in equilibrium with the pressure in the subglacial drainage system. These tests were conducted at different times since breakthrough, allowing us to investigate whether hydraulic transmissivity changed as water pressure returned to equilibrium. Rapid borehole refreezing precluded slug testing. Below we describe the borehole response test results alongside the methods.

For the majority of tests the monitoring borehole was the same as the injection borehole and these are referred to simply by the borehole name. To distinguish response tests where the injection and monitoring boreholes were different, we give the injection borehole in full followed by the monitoring borehole’s letter code in brackets. A conceptual illustration of our borehole response tests is presented in Figure 2.

All data loggers, including that of the drill, were synchronised precisely with Global Positioning System Time (GPST) immediately prior to drilling. Water pressure data were logged by separate Campbell Scientific CR1000X data loggers for each cluster of boreholes. The sampling frequency was increased to 0.2 Hz prior to borehole breakthrough, necessitating temporary suspension of thermistor measurements. Hence, no measurements of basal water temperature were made when drilling was taking place.

As it is difficult to measure the background hydraulic head without disturbing the subglacial environment it is necessary to define a reference head \(h_0\). The head in BH19e averaged from 36 – 60 h after BH19g breakthrough had recovered to within 0.1 m of the mean head over the 24 h period preceding BH19g breakthrough (Fig. 3b). On this basis, we define \(h_0\) as the mean head from 36 – 60 h post-breakthrough for all tests. No corrections for background trends in hydraulic head were made but such trends are small relative to the perturbations induced (Fig. 3a).

#### 3.1 Breakthrough tests

##### 3.1.1 Observations

All three boreholes drilled to the bed in 2019 drained rapidly upon intersecting the basal interface. During breakthrough, water levels dropped to an initial level measured during pressure transducer installation of 78, 73 and 80 m below the surface in BH19c, BH19e and BH19g (Table 1). The frictional drag of water flowing past the hose during breakthrough events caused
transient \( \sim 2 \text{kN} \) magnitude peak forces, as recorded on the drill tower (Figs 4, S1–S3). Following the peak, force on the drill tower became constant at \( \sim 200 \text{s} \) post-breakthrough but at a higher level than recorded prior to breakthrough. The offset in pre- and post-breakthrough force on the drill tower represents the difference between the weight of the hose in a water-filled and part-filled borehole.

As the drill stem was raised to the surface over \( \sim 2 \text{h} \) water continued to be pumped into the borehole, supplying an additional \( \sim 10 \text{m}^3 \) of water (Table 1). The volume of water drained during the breakthrough events was determined from the initial water level and annular cross-sectional area of the borehole of near surface radius \( r_s \) containing the hose of external radius \( r_d \), yielding a mean volume for the three breakthrough events of \( 4.70 \text{m}^3 \) (Table 1). Taking the duration of rapid drainage as the duration of the peak in force of \( \sim 200 \text{s} \) gives a mean discharge for the three breakthrough events of \( 2.3 \times 10^{-2} \text{m}^3 \text{s}^{-1} \) supplied from the borehole, with an additional flux supplied by the pumps \( Q_i = 75 \text{l min}^{-1} (1.25 \times 10^{-3} \text{m}^3 \text{s}^{-1}) \) bringing the total discharge to \( Q_o = 2.5 \times 10^{-2} \text{m}^3 \text{s}^{-1} \), and the total volume over the \( \sim 200 \text{s} \) duration to \( 4.95 \text{m}^3 \). The Reynolds number for outflow from the base of the borehole can be approximated as flow through a uniform cylindrical pipe, with a radius equal to that at the borehole base, the mean of which was \( r_0 = 0.10 \text{m} \) for the three boreholes (Table A1),

\[
Re = \frac{U_w 2n\rho_w}{\eta_w} = \frac{2Q_o\rho_w}{\pi r_0^2},
\]

where \( \eta_w = 0.0018 \text{Pa s} \) is the water viscosity at 0°C. Water flow through the boreholes near the base was turbulent with a high \( Re \approx 87,500 \) greatly exceeding the threshold for laminar flow of 2,000 (de Marsily, 1986).

3.1.2 Determining the BH19g breakthrough flux

To avoid sensor cables becoming tangled around the drill hose, pressure transducers were installed after the drill stem and hose had been recovered to the surface. Hence, no measurements of pressure were made within boreholes being drilled including during breakthrough. As the pressure response to BH19g breakthrough was captured by transducers already installed in BH19c and BH19e (Fig. 4) we now focus on the BH19g breakthrough.

We determined the time varying flux of water into the subglacial drainage system during the breakthrough of BH19g by inverting the recorded force on the drill tower from the hose, which is a combination of its weight, both in air and in water, and the...
frictional drag on the hose when the water drains through the borehole,

\[
F(t) = \pi r_d^2 \rho_g (H_{w0} - H_w) + \pi r_d^2 \Delta \rho g H_w + \frac{\pi r_d^4}{4} \rho_a F_d U_d^2 H_w + F_s, \tag{5}
\]

where \(r_d\) is the radius of the drill, \(\rho_g\) is the mean density of the drill (including the water core), \(\Delta \rho = \rho_d - \rho_w\), \(F_d\) is the coefficient of frictional drag exerted on the outside of the hose by the down-rushing water in the borehole, \(H_d(t)\) is the height of water in the borehole, \(F_s\) is the force exerted by the weight of the drill stem in water, and the bulk velocity of water in the borehole during the drainage event is \(U_w(t) = dH_w/dt\).

The force on the drill hose is initially set by the water height, which for a borehole full to the surface is equal to the ice thickness, therefore \(H_{w0}(t = 0) = H_{w0} = H_i = 1039\, m\) (Table 1). Since the initial force just before breakthrough \(F_0 = 893\, N\) the density difference between the hose and water is

\[
\Delta \rho = \frac{F_0 - F_s}{\rho_d g H_{w0}} = 96\, kg\, m^{-3}. \tag{6}
\]

Taking \(\rho_d = 999.8\, kg\, m^{-3}\) gives a mean density of the hose filled with water \(\rho_d = 1096\, kg\, m^{-3}\). Note that the composite density of the hose is

\[
\rho_d = \rho_d - (\rho_d - \rho_w)(r_d/r_i)^2, \tag{7}
\]

where \(r_d\) is the density of the hose material, and \(r_i = 9.7\, mm\) is the internal bore radius of the hose. Using the calculated value of \(\rho_d = 1096\, kg\, m^{-3}\) gives an estimate of the hose material density of \(\rho_d = 1166\, kg\, m^{-3}\), which is slightly larger than the nominal manufacturer’s specification of 1149 kg m\(^{-3}\). This apparent extra density corresponds to an extra force measured on the drill after the initial rapid breakthrough (\(t \to \infty\)) on the drill tower after the initial rapid breakthrough on the drill tower prior to breakthrough of 65 N, which we interpret as a drag of 0.0625 N per metre of hose from the pumped water flowing down the centre of the hose.

Neglecting minor residual oscillations, the force \(F_{\infty} = F\) \((t \to \infty)\) on the drill tower after the initial rapid breakthrough was again approximately constant and is given by

\[
F_{\infty} = 1470 \pm 10\, N = \pi r_d^2 \rho_g (H_{w0} - H_{w\infty}) + \Delta \rho \rho g H_{w\infty}. \tag{8}
\]

From this we can infer that the final height of the water level \(H_{w\infty} = 954 \pm 1\, m\). That is, during BH19g breakthrough the water in BH19g transiently drops \(H_{w0} - H_{w\infty} \approx 85\, m\) below the surface.

Following BH19g breakthrough a portion of the water in the borehole is rapidly evacuated into the subglacial environment. We know that the water level in the borehole decreases monotonically from an initial height \(H_0\) to a final height \(H_w\) and so fit the transient response with a modified exponential solution of the form

\[
H_w = H_{w\infty} + (H_{w0} - H_{w\infty})e^{-y(t)}, \tag{9}
\]

where

\[
y(t) = c_1 t^2 + c_1 t^3 + c_1 t^4. \tag{10}
\]

A fourth order polynomial was found to be the lowest order of polynomial to accurately represent the data. The flux of water from the borehole into the subglacial environment \((Q_w)\) can then be given by

\[
Q_w(t) = \pi r_d^2 U_w(t) + Q_i = \pi r_d^2 \frac{dH_w}{dt} + Q_i, \tag{11}
\]

where \(Q_i = 1.25 \times 10^{-3}\, m^3\, s^{-1}\) is the input flux from the drill. The three constants in the polynomial \(y(t), c_i\) where \(i = 1, \ldots, 3\), along with the drag coefficient \(F_d\) were estimated using non-linear regression (MATLAB: fitnlm). The resulting constants, with error estimation, are given in Table S2. From this fit \(R^2 = 0.996\) of the force on the drill hose the height of water, and therefore hydraulic head, in BH19g can be calculated, together with the flux into the subglacial hydrological network (Fig. 4b). This reveals that the discharge peaked at \(4.5 \pm 0.1 \times 10^{-3}\, m^3\, s^{-1}\) at 38 s after breakthrough.

3.1.3 Modelling the pressure response to BH19g breakthrough

Distinct pressure perturbations, here expressed as hydraulic head, occurred in BH19c and BH19e following the breakthrough of BH19g (Fig. 4a). In BH19e, located 4.1 m from BH19g, head instantaneously decreased by 0.93 m over a 20 ± 5 s period before rising rapidly and peaking at 14.0 m above its pre-breakthrough level 130 ± 5 s post-breakthrough. Synchronously with the drop in head observed in BH19c, a 0.11 m drop in head began in BH19c.

To analyse these pressure perturbations further we modelled the propagation of water at the contact between elastic ice and poroelastic sediment during BH19g breakthrough following Hewitt and others (2018). The Maxwell time for the basal temperate ice at site R30 is 10–25 min, and it is therefore reasonable to assume an elastic ice rheology for the short duration (< 4 min) of breakthrough events (Appendix C). This model accounts for pressure diffusion, flexure of the ice and deformation of the sediment, and was originally developed to describe the subglacial response to a rapidly draining supraglacial lake. The original model, which is based on Darcy’s law, allowed for the formation of a subglacial cavity as well as seepage through the sediment or established subglacial networks. However, for simplicity, here we do not include cavity formation and instead assume a single effective hydraulic transmissivity for subglacial water transport; and that the fluid is incompressible. The model allows the poroelastic sediment layer to deform in response to fluid flow and pressure gradients, which allows the overlying ice to flex and bend slightly as reflected in the small (0.93 m) transient head decrease preceding the large (14.0 m) head increase recorded in BH19c following BH19g breakthrough (Fig. 4a). With these features included, the model shows how an injected fluid diffuses through the subglacial environment and how this drives a propagating flexural wave in the overlying ice.

The linearised form of the model reduces to an evolution equation for the subglacial water pressure, which for consistency is here expressed as hydraulic head \(h\)

\[
\frac{\partial h}{\partial t} = A_1 \nabla^2 h + A_2 \nabla^3 h. \tag{12}
\]

Here \(A_1 = T M/lb\) and \(A_2 = T B\), in terms of transmissivity \(T\), till stiffness (p-wave modulus) \(M\), bending modulus of the ice \(B\), and sediment thickness \(b\). Here \(b\) is a fitting parameter, unconstrained by measurements of the actual sediment thickness, that represents the thickness of sediment affected by pressure diffusion. Assuming radial flow,

\[
\nabla^2 \equiv \frac{1}{r} \frac{\partial}{\partial r} \left( \frac{r}{\partial r} \right). \tag{13}
\]

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the associated flux of water $q$ at radius $r$ is

$$q(r) = -2\pi T \frac{dh}{dr},$$

(14)

and $q(r) = Q_i(r)$ is the injection flux into the subglacial environment.

This problem can be solved numerically for any injection flux $Q_i(r)$. By entering the time-varying injection flux for BH19g breakthrough (Section 3.1.2) into Eqn (14), we predicted the response of hydraulic head at BH19e (4.1 m from the injection point of BH19g). An automated non-linear optimisation procedure (MATLAB: fitnlm) was used to determine the best-fit model parameters, yielding $B = 2.75 \times 10^9$ Pa m$^{-3}$, $M/b = 1 \times 10^4$ Pa m$^{-3}$, and $T = 1.46 \times 10^{-3}$ m$^3$ s$^{-1}$. The prediction initially follows the data closely and it captures the initial decrease in BH19e hydraulic head as the flexural wave passes through (Fig. 4a). However, the model does not capture the subsequent development of the pressure recorded in BH19e; instead it predicts that the pressure drops off too rapidly after the first two minutes. We discuss this discrepancy further in Section 4.1.

### 3.2 Pumping Tests

#### 3.2.1 Observations

Following each breakthrough event, the hose was raised back to the surface over ~2 h (Table 1; Figs S1–S3), with the continued supply of water into the borehole functioning as a pumping test. We captured the pressure response at the base of BH19e to such a pumping test following the breakthrough of BH19g (Fig. 5). Although water was pumped down the hose while it was raised to the surface for all boreholes that reached the bed, no other pumping tests were useful as they occurred prior to the installation of pressure sensors. During the BH19g(e) pumping test the water pressure was measured in BH19e, 4.1 m distant (Fig. 5).

Starting 28 min after the breakthrough of BH19g the head in BH19e increased at a steady rate of $1.24$ m h$^{-1}$ (Fig. 5). This period of steady increase was interrupted by the temporary shutdown of the water supply when pressure-heater units were refuelled, with the linear increase in head resuming at the slightly higher rate of $1.36$ m h$^{-1}$. The rate of change of hydraulic head increased again to $7.40$ m h$^{-1}$ when the drill stem and hose rose above the borehole water level, indicating that, while the stem was below the water line, part of the water pumped into the borehole was replacing the reducing volume displaced by the hose as it was raised to the surface. We refer to these three periods of linearly increasing head as PT1, PT2 and PT3, respectively.

Discharge from the base of BH19g ($Q_d$) was calculated by correcting the input flux $Q_i (1.25 \times 10^{-3}$ m$^3$ s$^{-1}$) for storage within BH19g ($Q_s$), and for the flux offsetting the decreasing water displacement caused by the hose as it was raised to the surface ($Q_d$)

$$Q_o = Q_i - Q_d - Q_s$$

(15)

The pumping test was undertaken 9 d after the breakthrough of BH19e. Hence, we assume that storage within BH19e was negligible due to rapid borehole refreezing within cold ice that was present above a 70 m thick basal temperate layer (Law and others, 2021). We also consider storage within temperate ice to be negligible within the time span of our experiments due to its low permeability (e.g., $10^{-12} - 10^{-8}$ m$^2$; Haseloff and others, 2019). $Q_o$ was calculated as

$$Q_s = \pi r_i^2 \bar{U}_d,$$

(16)

where $r_i = 0.015$ m is the hose radius and $\bar{U}_d$ is the mean drill speed. For PT3, $Q_s = 0$ as the drill stem and hose were above the borehole water level. $Q_d$ is the flux lost to storage in the injection borehole calculated from the rate of change in head $dh/dt$ and the cross-sectional area of the borehole, which for PT1 and PT2 is annular as the hose was below the borehole water level

$$Q_o = (\pi r_i^2 - \pi r_s^2) \frac{dh}{dt},$$

(17)

where $r_s = 0.14$ m is the radius of BH19g at the surface (see Appendix B). For PT3

$$Q_s = \pi r_s^2 \frac{dh}{dt},$$

(18)

As the measurement of hydraulic head in BH19g did not start until after the pumping test, we assume that the rate of change of hydraulic head was the same in BH19g and BH19e.

These calculations reveal that during the pumping test the vast majority (90%) of water pumped into the borehole was discharged from the base (Table 2). Furthermore, this discharge from the borehole base ($Q_o$) was remarkably steady, averaging $1.12 \times 10^{-3}$ m$^3$ s$^{-1}$ with a standard deviation of $1.1 \times 10^{-6}$ m$^3$ s$^{-1}$. It follows that the bulk velocity of the water ($U_w = Q_o/\pi r_s^2$) through the borehole near the base during all periods was also steady, averaging $3.2 \times 10^{-2}$ m s$^{-1}$ with a standard deviation of $3.1 \times 10^{-3}$ m s$^{-1}$.

To test whether the outflow of borehole water during the pumping test was laminar or turbulent we calculated the Reynolds number ($Re$) using Eqn (4). During all periods, $Re \approx 3750$, indicating that flow of water in the bottom of the borehole was turbulent during the pumping tests. If, however, we assume that water leaves the borehole through a gap of width $\delta$ the Reynolds number for flow through this gap is

$$Re = \frac{Q_o \bar{D}_h \bar{U}_w}{2 \phi \pi \tau \delta \eta_w},$$

(19)

where $\bar{D}_h$ is the hydraulic diameter of the water film, $r$ is the distance from the borehole, and $\phi$ is the areal fraction of the bed occupied by the gap (de Marsily, 1986; Iken and others, 1996).
For thin films with a large lateral extent $D_h$ can be approximated as $28$ (de Marsily, 1986) and the equation can be simplified to

$$Re = \frac{Q_o\rho_w}{\eta_p \eta_{wc}}. \quad (20)$$

Using Eqn (20) and following the approach of Lüthi (1999), the transition from turbulent to laminar flow occurs at a distance of $\sim 1$ m from the borehole base for even the low value of $\phi = 0.1$. Hence, water flow beyond this point can be treated as laminar allowing the application of standard hydrogeological techniques.

### 3.2.2 Hydraulic transmissivity according to the Thiem method

The hydraulic transmissivity ($T_h$) of a subglacial sediment layer can be calculated by applying the Thiem (1906) method to the pumping test data. The Thiem method assumes that a steady state has been reached within a vertically-confined, homogeneous, isotropic and incompressible aquifer with Darcian flow. In these limits the hydraulic transmissivity

$$T_h = \frac{Q_o}{2\pi m^2} \ln \frac{R}{r_p}. \quad (21)$$

where $r = 4.1$ m is the horizontal distance between the injection borehole (BH19g) and the monitoring borehole (BH19e), and $s = h - h_0$, is the mean hydraulic head ($h$) during the pumping test above the reference head ($h_0$). The radius of influence ($R$) is the distance to the theoretical point at which the hydraulic head remains unchanged at the equilibrium level (i.e. at radial distance $R$, $h = h_0$, $s = 0$, Fig. 2). (Note that the subscript in $T_h$ indicates that the method used assumes Darcian flow through sediment rather than through a gap at the ice-sediment interface, later denoted $T_{ge}$ or some combination of the two, for which we use $T_h$ to represent the effective transmissivity.) The strong response of hydraulic head in BH19e to breakthrough in BH19g and the close agreement between head in these boreholes during the recovery phase (Fig. 3) indicates that the radius of influence is greater than the distance between BH19e and BH19g, which is 4.1 m at the surface. On the other hand, assuming a homogeneous, isotropic aquifer, the lack of a positive pressure peak in BH19g suggests the radius of influence is $<70$ m. Using the Thiem (1906) Eqn 21, and reasonable $R$ values of 10 and 70 m gives hydraulic transmissivity from $(1.31 - 4.75) \times 10^{-5}$ m$^2$s$^{-1}$ (Table 2).

Although the Thiem (1906) method is well established, it has limitations. The first is that the radius of influence $R$ is difficult to interpret physically. The second is the requirement that a steady state has been reached. A third limitation in our application is that to calculate the flux of water leaving the base of the injection borehole (BH19g) we assume that the rate of change in hydraulic head is the same in BH19g as that recorded in BH19e.

### 3.2.3 Hydraulic transmissivity according to the Hewitt model

An alternative method to calculate the transmissivity from the pumping test data is through the application of an analytical solution to the simplified Hewitt and others (2018) model. During the pumping test $Q_o$ is steady, thereby permitting an asymptotic solution of Eqn (12) that, based on the monitoring borehole at radius $r$ being sufficiently near to the injection borehole, gives

$$h(r) \to -\frac{Q_o}{2\pi T} \ln \left( \frac{r \sqrt{P R}}{A_{1T}} \right). \quad (22)$$

Hence, the predicted rate of change in hydraulic head at the nearby monitoring borehole is:

$$\frac{\partial h}{\partial t} \to \frac{Q_o}{4\pi T} T = \frac{Q_o}{4\pi T} \left( \frac{\partial h}{\partial t} \right)^{-1} \quad \text{(23a,b)}$$

This expression is independent of parameters $B$, $M$ and $b$ and is sensitive only to the transmissivity. In principle this provides an alternative means of predicting $T$ from the measured rate of change in hydraulic head during the pumping test, which avoids the limitations of the Thiem (1906) method outlined in Section 3.2.2. This method (Eqn (23b)) gives estimates of $T$ decreasing from $7.96 \times 10^{-5}$ m$^2$s$^{-1}$ during PT1, to $3.93 \times 10^{-5}$ m$^2$s$^{-1}$ during PT2, to $0.62 \times 10^{-5}$ m$^2$s$^{-1}$ during PT3 (Table 2).

### 3.3 Recovery tests

#### 3.3.1 Observations

After water input to the borehole ceased, the borehole water pressure recovered to the reference head ($h_{0}$) over ~36 – 50 h (Fig. 3b; Table 1). The range in recovery times can be explained by the variable timing and magnitude of the diurnal cycle in subglacial water pressure (Fig. 3). The observed recovery curves were similar (Fig. 3b) suggesting spatially uniform subglacial hydrological conditions between boreholes. We analysed the early phase of the recovery by fitting an exponential decay curve (Weertman, 1970, 1972; Engelhardt and Kamb, 1997) and the late phase using the Cooper and Jacob (1946) recovery test method. This provides two further estimates of hydraulic transmissivity: the first at 4 – 5 h post-breakthrough (early-phase), and the second at 14 – 27 h post-breakthrough (late-phase).

#### 3.3.2 Exponential decay curve

The early phase of the recovery curve can be approximated as an exponential decay using the water-film model of Weertman (1970, 1972):

$$s(t) = s_0 \exp \left(-\frac{t}{D}\right) \quad \text{(24)}$$

where $s_0$ is the initial recharge at the time the pumps stopped, $t$ is the time since the pumps stopped, and $D$ is a time constant determined by log-linear fitting (Figs 6a–c). The water-film model, which is referred to as the gap-conduit model in Engelhardt and Kamb (1997), is based on the Hagen–Poiseuille equation and assumes laminar flow through a constant-width gap at the interface between the ice and a level, impermeable bed.

---

### Table 2. Statistics for the BH19g(e) pumping test. $V_o$ is the volume of water discharged from the borehole base during the period. All other symbols are defined in the text.

<table>
<thead>
<tr>
<th>Period</th>
<th>PT1</th>
<th>PT2</th>
<th>PT3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Time since breakthrough (h)</td>
<td>0.9</td>
<td>1.7</td>
<td>1.9</td>
</tr>
<tr>
<td>Duration (min)</td>
<td>54</td>
<td>24</td>
<td>6</td>
</tr>
<tr>
<td>$s$ (m)</td>
<td>11.2</td>
<td>12.1</td>
<td>12.8</td>
</tr>
<tr>
<td>$dV/dr$ (m h$^{-1}$)</td>
<td>1.24</td>
<td>1.36</td>
<td>7.40</td>
</tr>
<tr>
<td>$Q_o$ (m$^3$ s$^{-1}$)</td>
<td>8.80</td>
<td>8.82</td>
<td>8.75</td>
</tr>
<tr>
<td>$Q_o$ (10$^{-4}$ m$^3$ s$^{-1}$)</td>
<td>12.5</td>
<td>12.5</td>
<td>12.5</td>
</tr>
<tr>
<td>$Q_o$ (10$^{-6}$ m$^3$ s$^{-1}$)</td>
<td>1.04</td>
<td>1.04</td>
<td>0</td>
</tr>
<tr>
<td>$Q_o$ (10$^{-5}$ m$^3$ s$^{-1}$)</td>
<td>0.231</td>
<td>0.231</td>
<td>1.27</td>
</tr>
<tr>
<td>$Q_o$ (% of $Q$)</td>
<td>90.0</td>
<td>89.8</td>
<td>89.8</td>
</tr>
<tr>
<td>$V_o$ (m$^3$)</td>
<td>3.65</td>
<td>1.62</td>
<td>0.41</td>
</tr>
<tr>
<td>$T_h$ (10$^{-3}$ m$^3$ s$^{-1}$)</td>
<td>1.51 – 4.75</td>
<td>1.39 – 4.37</td>
<td>1.11 – 4.13</td>
</tr>
<tr>
<td>$T$ (10$^{-5}$ m$^3$ s$^{-1}$)</td>
<td>7.96</td>
<td>3.93</td>
<td>0.62</td>
</tr>
</tbody>
</table>

$\dagger$ Calculated using the analytical solution to the simplified Hewitt and others (2018) model (Eqn (23b)).

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In the recovery curves of tests BH19c and BH19e the first part of the curve is missing due to the time taken to lower the pressure transducer to the bed after the drill stem was raised to the surface (Fig. 3a). Hence, \( s_0 \) was also treated as an unknown. In the BH19g(e) test the monitoring borehole was different from the injection borehole and the first part of the recovery curve was recorded. The initial BH19g(e) recovery curve was not, however, exponential and linear-log fitting was delayed for 5,000 s (83 min; Fig. 6c). After this delay the trend for BH19g(e) was quasi-exponential, in common with the other tests, and \( s_0 \) was again treated as an unknown for this test (Figs 6a–c). Hence, measured \( s_0 \) for BH19g(e) is 12.7 m and that calculated by fitting Eqn (24) is 10.1 m. The resulting time constant \( D \) was 18,200 s for BH19c, 25,000 s for BH19e and 23,000 s for BH19g(e).

Rearranging Eqn (9) of Engelhardt and Kamb (1997) allows the gap width \( \delta \) to be calculated from the time constant as

\[
\delta = \left( \frac{6 \eta w r_s^2}{D p_s g \phi} \ln \frac{R}{r_0} \right)^{1/3}
\]  

(25)

Furthermore, if we make the reasonable assumption of laminar flow at distances > 1 m from the borehole (Section 3.2), the transmissivity \( T_g \) of a continuous porous medium equivalent to a gap of width \( \delta \) is given by de Marsily (1986) as

\[
T_g = \delta^2 \frac{\phi g p_s w}{12 \eta w}
\]  

(26)

Combining Eqns (25) and (26) (see Appendix D) allows \( T_g \) to be calculated directly from the time constant \( D \)

\[
T_g = \frac{r_s^2}{2D} \ln \frac{R}{r_0}
\]  

(27)

For each test, two values of transmissivity were calculated, bracketing the radius of influence \( R \) to 10 – 70 m.

The results show that hydraulic transmissivity was an order of magnitude lower during the early recovery phase than during the pumping test, with hydraulic transmissivity spanning the range \((1.8 - 3.5) \times 10^{-6} \text{ m s}^{-1}\) equivalent to gap widths of 0.16 – 0.20 mm for gaps covering the whole of the glacier bed (\( \phi = 1 \); Table 3).

### 3.3.3 Cooper and Jacob recovery tests

Hydraulic transmissivity can also be derived from the later stages of the recovery curve using the Cooper and Jacob (1946) recovery test method, providing information about the nature of the subglacial hydrological system as it returns to its original state. This method is based on the observation that, after a certain period of time, drawdown (or in our case drawup) within an aquifer at a given distance from a borehole decreases approximately in proportion to the logarithm of the time since the discharge (or in our case recharge) began. The method assumes a non-leaky, vertically-confined aquifer of infinite lateral extent. Although the Theis (1935) method – on which the Cooper and Jacob (1946) method is based – requires a constant pumping rate, the method can be applied to a recovery test (i.e. after the pumps have ceased) using the principle of superposition of drawdown (e.g. de Marsily, 1986; Hiscock and Bense, 2014). Under this principle, pumping is assumed to continue uninterrupted while a hypothetical drawdown well is superimposed on the monitoring well from the time pumping stopped to exactly counteract the recharge from the pump. The residual drawup \( s' \) is

\[
s' = h - h_0 = \frac{Q}{4 \pi T} [W(u) - W(u')]
\]  

(28)

where \( h, h_0, Q \) and \( T \) are as previously defined, and \( W(u) \) and \( W(u') \) are well functions for the real and hypothetical boreholes.
Table 3. Results from the gap-conduit model (exponential fit). Gap width and the apparent hydraulic transmissivity were calculated for two values of the radius of influence ($R = 10$ and $70$ m). Gap widths were additionally calculated for two areal fractions of the bed covered by the gap ($\phi = 0.1$ and 1.0). The apparent gap transmissivity is independent of $\phi$ because gap cross-sectional area is a product of $\delta$ and $\phi$.

<table>
<thead>
<tr>
<th>Test</th>
<th>$s_0$ (m)</th>
<th>$D$ (s)</th>
<th>$\delta$ (mm)</th>
<th>$T_s$ ($10^{-5}$ m$^2$ s$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>BH19c</td>
<td>16</td>
<td>18,200</td>
<td>0.18 − 0.20</td>
<td>0.38 − 0.43 0.25 − 0.35</td>
</tr>
<tr>
<td>BH19e</td>
<td>14.8</td>
<td>25,000</td>
<td>0.16 − 0.18</td>
<td>0.34 − 0.38 0.18 − 0.26</td>
</tr>
<tr>
<td>BH19g(e)</td>
<td>10.1</td>
<td>23,000</td>
<td>0.16 − 0.18</td>
<td>0.35 − 0.39 0.19 − 0.28</td>
</tr>
</tbody>
</table>

where

$$u = \frac{r^2 S}{4Tt}, \quad u' = \frac{r^2 S}{4TF},$$

and $S$ is the storage coefficient, which cannot be determined using this method. In the previous two equations, $t$ is time since the start of pumping, which for our tests is at breakthrough, and $t'$ is the time since the pumps stopped. As per the standard Cooper and Jacob (1946) method for pumping tests, for small values of $u'$ and large values of $t'$, the well functions can be approximated so that residual drawdown can be estimated from the simplified equation

$$s' = \frac{2.303Q}{4\pi T_0} \log_{10} \frac{t}{t'},$$

Hence, linear-log fitting allows hydraulic transmissivity ($T_s$) to be calculated,

$$T_s = \frac{2.303Q}{4\pi s'},$$

where $\Delta s'$ is the rate of change of residual drawdown with respect to the logarithmic time ratio. The Cooper and Jacob (1946) recovery test method described above has the advantage that the rate of recharge can be assumed to be constant, in contrast to that during an actual pumping test, which may vary (Hiscock and Bense, 2014).

During the recovery phase, the sampling interval was increased from 5 to 300 s. Prior to application of the Cooper and Jacob (1946) recovery test method, the data were resampled to a constant 5 s interval and interpolated linearly. The data presented in Figures 6d-f extend from the time of pressure transducer installation at the bed (or in the case of BH19g the earlier time at which the pumps were stopped), to when diurnal pressure variations began. Fitting was applied to the later stages of the recovery curve where the trend in recharge versus the logarithmic time ratio was linear, as is required for this method to be appropriate. Accordingly, hydraulic transmissivity was calculated to be $3.0 \times 10^{-6}$ m$^2$ s$^{-1}$, $2.2 \times 10^{-6}$ m$^2$ s$^{-1}$ and $2.8 \times 10^{-6}$ m$^2$ s$^{-1}$ for BH19c, BH19e and BH19g respectively.

4. Discussion

4.1 Hydraulic ice-sediment separation

The average drop in borehole water level during breakthrough indicates that the subglacial environment accommodated 4.70 m$^3$ of water within 200 s. For all three boreholes that reached the bed, the delayed recovery to background levels over 36 − 50 h suggests that this breakthrough water and an additional ~10 m$^3$ of water injected during the raise, could not be efficiently drained away from the immediate vicinity of the borehole’s base. For example, recovery to the reference head took 45 h following the input of 13.6 m$^3$ of water injected into BH19g at breakthrough and during the drill stem raise (Table 1; Fig. 3b) yielding a mean discharge of $8.4 \times 10^{-5}$ m$^3$ s$^{-1}$. If the boreholes had intercepted a conduit with the capacity to drain the water away efficiently then the mean discharge rate would have been higher and the recovery time would have been shorter. Hence, it follows that at least some of this water must have been temporarily stored locally. We hypothesise that water was predominantly stored within a gap opened at the ice-surface interface facilitated by the overpressure (913 ± 101 kPa; Table 1) exerted at the base of water-filled boreholes due to the greater density of water than ice. In the following analysis we constrain the geometry of this gap and investigate how the gap width changed through time.

An approximate calculation of the plausible range in gap width can be made for the BH19g breakthrough by assuming a uniform cylindrical subglacial water sheet with a radius ranging from 10 − 70 m (that is just greater than the distance to BH19e where a positive peak in pressure was observed and just less than the distance to BH19c where there was no positive peak in pressure). Under these assumptions, a gap width of 0.3 − 16.5 mm could accommodate the 5.17 m$^3$ of water injected in 200 s after BH19g breakthrough. This range is consistent with a lack of discernible ice surface uplift in data collected by a GNSS receiver at R30, confirming that surface uplift was below the precision of the GNSS data of ± 50 mm (Fig. S4). Assuming a straight-sided cylinder with a volume equal to that injected during BH19g of 5.17 m$^3$ the upper bound on the surface uplift of 50 mm provides a lower bound on the radius of the uplift of ~ 5.7 m.

Further estimates of gap widths can be determined from the hydraulic transmissivity measurements. If we assume laminar flow, which is reasonable at distances > 1 m from the borehole (see Section 3.2), the gap width ($\delta$), equivalent to a continuous porous medium with an effective hydraulic transmissivity ($T_g$), is given by rearranging Eqn (26)

$$\delta = \left( \frac{12T_g \eta_w}{\phi \rho_w g} \right)^{1/3}.$$
opened at the ice-sediment interface. The delayed arrival of the pressure increase demonstrates that no efficient hydraulic connection existed between BH19e and BH19g prior to the breakthrough of BH19g. The 20 ± 5 s delay between the start of the load increase on the drill tower and the start of the pressure increase in BH19e gives a mean velocity of the pressure pulse of 0.20 ± 0.04 m s\(^{-1}\). Similar pressure pulse propagation velocities of 0.08 – 0.18 m s\(^{-1}\) were observed on Whillans Ice Stream (Engelhardt and Kamb, 1997). If a conduit existed between BH19g and BH19e prior to breakthrough, the pressure pulse would be transmitted at the speed of sound (1440 m s\(^{-1}\)) and attenuated in amplitude by the viscosity of water at a rate proportional to the gap width (Engelhardt and Kamb, 1997). The observed delay of 20 ± 5 s is four orders of magnitude longer than the expected delay of a sound wave through 4.1 m of water of 0.003 s, which confirms that no conduit existed between BH19g and BH19e prior to breakthrough. Instead, we infer that the delay represents the propagation velocity of the gap tip outwards from BH19g.

On the other hand, the disturbance in hydraulic head in BH19e caused by attempts to free a piezometer snagged at 394 m depth in BH19g, demonstrates that a hydraulic connection between the two boreholes was present at this time 2.4 h after breakthrough (Fig. 5). The piezometer in BH19g was freed after repeated pulling on the cable, which caused the hydraulic head to fluctuate in BH19e, with disturbance continuing as the piezometer was lowered to the bed. We infer that this inter-borehole transmission of pressure perturbations indicates an open gap at the ice-sediment interface at this time.

The performance of the simplified Hewitt and others (2018) model in predicting the pressure response to borehole breakthrough provides further evidence for gap opening. The simplified model makes a reasonable prediction of the initial pressure response in BH19e to BH19g breakthrough (Fig. 4). The model closely reproduces the small (0.93 m) drop in hydraulic head followed by the rapid rise within the first minute. This suggests that the small drop in BH19g head can be explained by the propagation of a flexural wave through the ice that is faster than the spread of water. Furthermore, the initial drop in pressure indicates that the sediment is deformable because such a drop cannot be reproduced by the model if the sediment is rigid (see Fig. 7b of Hewitt and others, 2018). The model, however, predicts that the hydraulic head should reduce much more rapidly after the peak than was observed (Fig. 4a). Furthermore the analytical solution to the model (Eqa (23b)) predicts that \(\frac{d\phi}{dt}\) should decrease non-linearly as 1/t, whereas the measured linear trends in hydraulic head during the pumping test suggest that \(\frac{d\phi}{dt}\) was constant (Fig. 5). Both these disparities can be explained by gap opening.

The response of hydraulic head in BH19e to BH19g breakthrough and pumping (Figs 4 and 5) resembles the idealised pressure response of petroleum reservoirs to hydraulic fracture treatment (cf. Fig. 18a of Hubbert and Willis, 1957). Specifically, the BH19(e) breakthrough curve can be interpreted as a horizontal hydraulic fracture induced from a relatively smooth borehole, which is consistent with our interpretation of gap-opening at the ice-sediment interface induced by borehole breakthrough. We can therefore apply hydraulic fracture treatment theory to interpret the response to BH19g(e) breakthrough, as follows. After the initial drop in head, the arrival of water in BH19e is marked by a steep rise (labelled A in Figs 4a and 5), and the gradient of this increase indicates compression of the water and subglacial sediment prior to the initiation of gap opening beyond BH19e. As gap opening begins the energy stored within the compressed water and sediment is transferred to gap propagation outwards from BH19e resulting in more space for the water to occupy, and therefore lower pressure and a decrease in the gradient (dh/dt; label B). The peak in head after 130 s represents the transition from stable to unstable gap opening at the so-called ‘breakdown pressure’. The ensuing transient head decrease (label C) can be explained by the gap opening rate transiently exceeding the water input rate, and by the diffusion of unevenly distributed pressure within the immature gap. With continued water input, a steady state of gap opening was reached resulting in the linear trend in hydraulic head (label D). In our pump tests, the recharge from the pump exceeded the discharge through the gap and the borehole filled with water at a linear rate determined by the supply rate from the pumps and the extraction rate of the drill hose. That water input exceeded water output during the pumping test despite discharge rates being much lower than during breakthrough provides evidence for partial gap closure in response to reduced water pressure. When the pumps ceased, head briefly stayed constant before dropping rapidly and then transitioning into a logarithmic decay representing gap closure and reversion to Darcian flow. In petroleum engineering, the pressure at the onset of the rapid drop (label E) has been interpreted to approximate the fracture propagation pressure. For BH19g(e) this occurs at 9.290 MPa, which is comparable to the ice overburden pressure (Table 1), and is thus consistent with hydraulic ice-sediment separation. This interpretation suggests that the application of hydraulic fracture models to borehole breakthrough and pumping tests would be an improvement over hydrogeological techniques such as the Thiem (1906) method, which inherently assume Darcian flow through an incompressible, isotropic aquifer. Such assumptions are unlikely to be valid if gap opening is taking place and this

### Table 4. Summary of borehole response test results.

<table>
<thead>
<tr>
<th>Test Type</th>
<th>Method</th>
<th>(t) (h)</th>
<th>(\phi = 1)</th>
<th>(\phi = 0.1)</th>
<th>(T) (10(^{-3}) m(^2) s(^{-1}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>BH19g(e)</td>
<td>Breakthrough</td>
<td>Hewitt and others (2018)(^a)</td>
<td>0</td>
<td>0.69</td>
<td>1.48</td>
</tr>
<tr>
<td>BH19g(e)</td>
<td>Pumping (PT1)</td>
<td>Hewitt and others (2018)(^b)</td>
<td>0.9</td>
<td>0.56</td>
<td>1.21</td>
</tr>
<tr>
<td>BH19g(e)</td>
<td>Pumping (PT2)</td>
<td>Hewitt and others (2018)(^b)</td>
<td>1.7</td>
<td>0.44</td>
<td>0.95</td>
</tr>
<tr>
<td>BH19g(e)</td>
<td>Pumping (PT3)</td>
<td>Hewitt and others (2018)(^b)</td>
<td>1.9</td>
<td>0.24</td>
<td>0.51</td>
</tr>
<tr>
<td>BH19g(e)</td>
<td>Pumping (PT3)</td>
<td>Thiem (1906)</td>
<td>0.9</td>
<td>0.32 – 0.47</td>
<td>0.69 – 1.01</td>
</tr>
<tr>
<td>BH19g(e)</td>
<td>Pumping (PT3)</td>
<td>Thiem (1906)</td>
<td>1.7</td>
<td>0.31 – 0.46</td>
<td>0.67 – 0.99</td>
</tr>
<tr>
<td>BH19g(e)</td>
<td>Pumping (PT3)</td>
<td>Thiem (1906)</td>
<td>1.9</td>
<td>0.31 – 0.45</td>
<td>0.66 – 0.97</td>
</tr>
<tr>
<td>BH19e</td>
<td>Recovery (early)</td>
<td>Weertman (1970) exponential fit</td>
<td>4.9</td>
<td>0.18 – 0.20</td>
<td>0.38 – 0.43</td>
</tr>
<tr>
<td>BH19e</td>
<td>Recovery (early)</td>
<td>Weertman (1970) exponential fit</td>
<td>4.4</td>
<td>0.16 – 0.18</td>
<td>0.34 – 0.38</td>
</tr>
<tr>
<td>BH19e</td>
<td>Recovery (early)</td>
<td>Weertman (1970) exponential fit</td>
<td>4.4</td>
<td>0.16 – 0.18</td>
<td>0.35 – 0.39</td>
</tr>
<tr>
<td>BH19e</td>
<td>Recovery (late)</td>
<td>Cooper and Jacob (1946)</td>
<td>14.1</td>
<td>0.19</td>
<td>0.40</td>
</tr>
<tr>
<td>BH19e</td>
<td>Recovery (late)</td>
<td>Cooper and Jacob (1946)</td>
<td>27.2</td>
<td>0.17</td>
<td>0.36</td>
</tr>
<tr>
<td>BH19g(e)</td>
<td>Recovery (late)</td>
<td>Cooper and Jacob (1946)</td>
<td>23.0</td>
<td>0.18</td>
<td>0.39</td>
</tr>
</tbody>
</table>

\(^a\) Simplified model (Eqn (14)).
\(^b\) Analytical solution (Eqn (23b)).
may explain the difference between the Thiem (1906) and (analytical) Hewitt and others (2018) estimates of transmissivity during the pumping test (Table 4; Fig. 7).

The observation of an instantaneous drop in hydraulic head of 0.11 m in BH19c in response to BH19g breakthrough without a subsequent increase in head (Fig. 4a) also cannot be reproduced by the simplified Hewitt and others (2018) model; the model predicts a flexural wave that would be apparent at any fixed radius as a small pressure drop followed by a large pressure rise. We hypothesise that the drop in pressure in BH19c is caused by uplift at the BH19g injection site increasing the volume of a hydraulically-isolated cavity at BH19c, and that cavity expansion without an increase in water mass leads to a reduction in water density and pressure – that is a rarefaction. The simplified Hewitt and others (2018) model cannot reproduce rarefactions caused by stress transfer through the ice because it assumes that water compressibility is zero and, more fundamentally, it directly couples vertical displacement of the ice to the pressure in the subglacial environment, so that cavity expansion cannot occur without an increase in pressure (and vice versa). Further evidence for hydraulic isolation of the BH19c cavity is provided by diurnal water pressure variations that are anti-correlated with those in BH19e and ice velocity (Figs 8a,b; e.g., Murray and Clarke, 1995; Meierbachtol and others, 2016). The inference of BH19c cavity isolation is also supported by the observation that diurnal pressure variations in BH19c are manifested as small (~0.05°C peak-to-peak) temperature cycles recorded at the base of BH19c (Fig. 8). This demonstrates that the water temperature quickly equilibrates with the pressure-dependent ice temperature, which would occur within an isolated cavity but not in a connected conduit. We would expect that within a connected conduit a throughput of water from different regions of the bed at variable pressures and temperatures would mask the small pressure-driven diurnal variations in temperature.

Rearranging the equation of state for water assuming mass is conserved and that temperature is constant, allows the pressure change to be related to the change in cavity volume

$$\frac{V}{V_0} = \exp[\beta_w(p_w - p_{w0})],$$

where $V_0$ and $p_{w0}$ are the reference volume and pressure and $\beta_w = 5.1 \times 10^{-10} \text{ Pa}^{-1}$ is the compressibility of water. We can constrain the initial cavity geometry in two situations. First, the observation of no prior hydraulic connection between BH19e and BH19g, which were separated at the surface by 4.1 m, indicates the BH19c cavity was smaller than this distance. Second, the volume of water drained during BH19c breakthrough and the hose raise of 15.6 m$^3$ provides an approximate maximum constraint on the BH19c cavity volume. These constraints are consistent with measurements of dye dilution in boreholes drilled on Isunnguata Sermia, which indicated cavity volumes of 7.6 ± 6.7 m$^3$ (Meierbachtol and others, 2016). Assuming the initial BH19c cavity volume was within the reasonable range of 0.5 – 15 m$^3$, the small 0.11 m decrease in hydraulic head measured in BH19c located ~70 m distant can be explained by the contraction of the BH19c cavity of 0.3 – 8.2 × 10$^{-6}$ m$^3$. This demonstrates that, due to the low compressibility of water, the 0.11 m head decrease can be explained by a small cavity contraction of 5.5 × 10$^{-6}$ m$^3$.

Hence, we hypothesise that hydraulic ice-sediment separation caused by the overpressure at the base of BH19g caused elastic uplift of the BH19c cavity roof. The 0.11 m drop in BH19c head in response to BH19g breakthrough therefore provides direct evidence for the hypothesis of Murray and Clarke (1995) that pressure variations in hydraulically-isolated cavities occur due to elastic displacement of the ice roof driven by perturbations in hydraulically-connected regions of the bed. We discuss this further in Section 4.3.

4.2 Hydraulic conductivity of subglacial sediments

We interpret the decrease in hydraulic transmissivity with time since breakthrough (Table 4; Fig. 7) as evidence for the closure...
of a gap at the ice-sediment interface that was opened by the over-pressure at borehole breakthrough. It is notable that hydraulic transmissivity estimates derived using the Cooper and Jacob (1946) recovery tests were relatively constant (that is within $8 \times 10^{-7}$ m$^2$ s$^{-1}$), despite the tests occurring over a wide range in time since breakthrough (14.1–27.2 h; Table 4; Fig. 7). Hence, these tests may be representative of Darcian flow through the sediment layer after gap closure. This suggestion is supported by the observation that the drawdown decreased logarithmically through time (Figs 6d–f) as is expected under Darcian flow, which is unlikely to be the case if gap closure was incomplete. Darcian flow through subglacial sediments was also inferred at site S30 from the initially logarithmic recovery in subglacial water electrical conductivity (EC) observed over 12 h following the dilution effect caused by drilling with low EC surface waters (Doyle and others, 2018).

When there is no flow through a gap at the ice-sediment interface, hydraulic transmissivity ($T$) is the hydraulic conductivity ($K$) integrated over the sediment thickness $b$

$$T = bK. \quad (34)$$

The sediment thickness at the borehole location has been estimated at $20.7 \pm 1$ m by fibre-optic distributed acoustic seismics in BH19c (Booth and others, 2020). The full sediment thickness represents an upper limit for the calculation of hydraulic conductivity due to an increase in sediment compaction with depth, and the pressure-dependent depth limit to the diffusion of water from the ice-sediment interface (Tulaczyk and others, 2000). For the range of hydraulic transmissivity from the Cooper and Jacob (1946) recovery tests of $(2.2 - 3.0) \times 10^{-6}$ m$^2$ s$^{-1}$ (Table 4), and a range of reasonable 'hydraulically-active' sediment thicknesses of $2 - 20$ m, the hydraulic conductivity is $(0.1 - 1.5) \times 10^{-6}$ m s$^{-1}$. This estimate is reasonable and within the range of hydraulic conductivities of glacial tills found in a range of settings by previous studies (Table 5). The Cooper and Jacob (1946) recovery test for BH19c was performed several hours earlier with respect to the time of breakthrough than those in BH19e and BH19g (Fig. 7) due to the earlier establishment of diurnal pressure variations in BH19c (Fig. 3b). If gap closure was still taking place, this earlier timing could explain the slightly higher transmissivity derived for BH19c. We also cannot exclude the possibility that water flow during breakthrough and pumping tests – or from previous natural subglacial water flow – winnowed fine particles from the upper layer of sediment, increasing the hydraulic conductivity of this layer (Iverson and others, 2007; Fischer and others, 1998). As we cannot exclude winnowing, or be certain that the gap was fully closed, we interpret our estimates to represent an upper bound on the hydraulic conductivity of the sediment beneath this site.

Our inferred sediment hydraulic conductivity is two orders of magnitude higher than that determined from laboratory analysis of sediment retrieved from beneath Whillans Ice Stream (Engelhardt and others, 1990) and Trapridge Glacier in Canada (Murray and Clarke, 1995), see Table 5. A hydraulic conductivity of $10^{-6} - 10^{-7}$ m s$^{-1}$ is, however, broadly consistent with the type of glacigenic sediment within core samples taken from Uummannaq Fjord. These core samples comprise glaciomarine sediments deposited during the last glacial maxima including matrix supported diamict with angular to sub-angular clasts of basalt and granitic gneiss dispersed throughout a sandy mud matrix (Ó’Cofaigh and others, 2013).

Laboratory measurements of the hydraulic conductivity of glacial sediments, which inherently measure only Darcian flow, are typically a few orders of magnitude lower than field measurements (Table 5; Hubbard and Maltman, 2000), a disparity that could, at least partly, be explained by residual gap opening at the ice-sediment interface during borehole response tests (e.g., Fountain, 1994; Stone and others, 1997). While in situ measurement of hydraulic conductivity of subglacial sediments appears to overestimate hydraulic conductivity under strict Darcian flow conditions, laboratory measurements provide little insight into the complexity of subglacial hydrological processes such as ice-sediment separation. Furthermore, as glacial sediment is by nature poorly sorted, with grain sizes ranging from boulders to clays, analysing samples that are large enough to be representative in laboratory experiments conducted at the scale necessary is more difficult than conducting in situ measurements (Clarke, 1987; Hubbard and Maltman, 2000). True subglacial water flow at this site may neither occur as entirely Darcian (laminar) flow through subglacial sediment nor exclusively through a gap at the ice-sediment interface, but rather a combination of the two. In any case, our in situ measurements represent a constraint on the effective hydraulic transmissivity that is independent of the process of water flow.

### 4.3 Implications for subglacial hydrology and basal motion

Subglacial water flow at glaciers underlain by porous sediment will naturally occur as laminar Darcian flow through interconnected pore spaces, although only insofar as the hydraulic transmissivity of the sediment is sufficient to accommodate the input of meltwater. With sustained inputs of water to the bed of many glaciers, from surface melt, for example, it may also be natural for a portion of that input to be stored temporarily in gaps opened at the ice-sediment interface, when water is delivered faster than it can permeate into the sediment below. The evidence presented herein demonstrates that the overpressure of a water-filled borehole can open a gap at the ice-sediment interface and need not directly intersect an active subglacial drainage system in order to drain. The delayed arrival of the pressure pulse in BH19e rules out the existence of sheet flow (Weertman, 1970; Alley and others, 1986; Creyts and Schoof, 2009), efficient conduits such as R-channels or canals (e.g., Röthlisberger, 1972; Walder and Fowler, 1994; Ng, 2000), and linked cavities (e.g., Kamb, 1987) prior to BH19g breakthrough, but supports the gap-opening theory of Engelhardt and Kamb (1997). We infer that prior to the breakthrough of BH19g, subglacial drainage at this location consisted exclusively of Darcian flow through subglacial sediments with a hydraulic conductivity $K \leq 10^{-6}$ m s$^{-1}$.

Borehole drainage at the ice-sediment interface may be physically similar, but of lower magnitude, to that which occurs during the subglacial drainage of proglacial (Sugiyama and others, 2008), subglacial (e.g., Johannesson, 2002) and supraglacial lakes (Tsai and Rice, 2010, 2012; Doyle and others, 2013; Dow and others, 2015; Stevens and others, 2015; Hewitt and others, 2018) via a broad, turbulent and transient sheet. We note that gap opening at the ice-sediment or ice-bedrock interface is conceptually the same as horizontal hydraulic fracture at this interface as envisaged by previous studies (Tsai and Rice, 2010, 2012; Hewitt and others, 2018). Rapid water flow into this narrow gap is likely to be turbulent (Section 3.1.1); however, flow must become laminar near the gap tip as the width of the gap decreases to zero, and flow velocity will also decrease with distance from the injection point (Hewitt and others, 2018). Continued sheet flow through a uniform gap would be unstable as irregularities in flow would theoretically favour the formation of conduits through preferential sediment erosion and concentrated ice melt from frictional heat (Röthlisberger, 1972; Walder and Fowler, 1994; Ng, 2000). Conduit development beneath kilometre-thick ice is, however, anticipated to require continuous water supply at high pressure over prolonged periods, which may only occur if there is...
continued water input from the surface (e.g., Dow and others, 2014, 2015). Hence, our inference of complete, or at least partial, gap closure in response to declining pressure is consistent with existing theory as the water volumes provided by borehole drainage and subsequent pumping (~15 m$^3$) are likely insufficient to establish an efficient conduit beneath kilometre-thick ice. The development of efficient conduits in response to borehole breakthrough can also be excluded by the low discharge rate of $8.4 \times 10^{-5}$ m$^3$ s$^{-1}$ calculated from the 45 h required for hydraulic head to recover to the equilibrium level following the injection of 13.6 m$^3$ of water at BH19g breakthrough and during the drill stem raise. Although we cannot rule out the persistence of stable sheet flow following borehole drainage facilitated by clasts partially supporting the ice overburden pressure (Creys and Schoof, 2009), our observations of a progressive decrease in hydraulic transmissivity can be entirely explained by gap closure and a reversion to Darcian flow through the sediment layer. For simplicity, this and previous studies (Tsai and Rice, 2010, 2012; Hewitt and others, 2018) make the reasonable assumption that initial gap opening is elastic; however, where temperate ice is present, as it is at R30, viscous deformation cannot be neglected during the longer time scales of pumping tests or lake drainage events (Appendix C). The application of a viscoelastic model (e.g., Reeh and others, 2003) to borehole response tests (and lake drainage events) would therefore represent an improvement over the analysis presented herein (and previously).

The instantaneous 0.11 m drop in BH19c head in response to BH19g breakthrough (Fig. 4a) provides direct evidence for the hypothesis of Murray and Clarke (1995) that pressure variations can be transmitted to unconnected cavities through elastic displacement of the ice roof. Murray and Clarke (1995) theorised that uplift caused by high water pressure relieves the pressure in adjacent hydrologically-isolated cavities. This hypothesis is one of three hypotheses of mechanical forcing of water pressure that have been proposed to explain the observed diurnal variation of water pressure in hydrologically-isolated cavities that is out of phase with both ice velocity and water pressure in boreholes and moulins deemed to be connected to efficient subglacial conduits (Murray and Clarke, 1995; Engellhardt and Kamb, 1997; Gordon and others, 1998; Dow and others, 2011; Andrews and others, 2014; Ryser and others, 2014; Lefeuvre and others, 2015; Meierbachtol and others, 2016; Rada and Schoof, 2018). While we cannot rule out the possibility that such anti-correlated diurnal pressure and velocity variations in BH19c (Fig. 8) can be attributed to the alternative hypotheses of cavity expansion and contraction caused by longitudinal strain (Ryser and others, 2014) or basal sliding (Iken and Truffer, 1997; Bartholomaus and others, 2011; Hoffman and Price, 2014), displacement of the ice roof due to elastic uplift during gap-opening at BH19g breakthrough can entirely explain the 0.11 m instantaneous drop in BH19c head. It is therefore plausible that elastic displacement of the ice roof by diurnal pressure variations within a nearby conduit also explains the anti-correlated diurnal variations in BH19c pressure. This assertion is supported by three-dimensional full-Stokes modelling (Lefevre and others, 2018) that reproduced anti-correlated pressure variations between connected and unconnected components of the subglacial drainage system without invoking cavity expansion caused by sliding.

Similar to borehole breakthrough events, we argue that water flow at the ice-sediment interface may also occur at times of naturally high subglacial water pressures. It is important to note that the gap widths we report are probably larger than would have occurred naturally for the same volume of cold glacial water because warm drilling water would have enlarged the gaps through ice melt. The greater variability in meltwater supply means that gap opening at the ice-sediment interface is more likely to occur naturally on the Greenland Ice Sheet, and on mountain glaciers, than on the West Antarctic ice streams where the process was originally inferred (Engellhardt and Kamb, 1997). Hence, gap opening at the ice-sediment interface has important implications for our understanding of subglacial hydrological systems that extends beyond its ability to explain the drainage of boreholes. Subglacial hydrology in ice-sheet models may for instance include exchanges of water flowing partly at the interface and partly within subglacial sediment, which has proven efficient in reproducing day-to-day variations in ice flow as observed at the land-terminating southwest ice margin (Bougainmont and others, 2014). Darcian flow and gap-opening therefore provide a physical explanation for the partitioning of water flowing at the interface and within subglacial sediment.

Gap-opening may also play a role in the formation and growth of subglacial drainage systems. Within the framework of existing theory, gap opening provides the initial conduit that may later develop into an inefficient narrow orifice in a distributed (i.e. linked cavity) drainage system (Kamb, 1987), which may ultimately develop into an efficient channel or canal (Rothlisberger, 1972; Walder and Fowler, 1994; Ng, 2000). That the overpressure of a water-filled vertical conduit stretching from the surface to the

### Table 5. Selected hydraulic conductivities of glacial sediments from the literature in ascending order. Sediments at the lower end of the scale ($K \leq 10^{-6}$ m s$^{-1}$) were typically interpreted as unconsolidated sands and gravels, often associated with water flow from subglacial channels winnowing fine particles (Fischer and others, 1998).

<table>
<thead>
<tr>
<th>$K$ (m s$^{-1}$)</th>
<th>Location (method)</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>$10^{-12}$ – $10^{-6}$</td>
<td>Literature review of glacial tills</td>
<td>Freeze and Cherry (1979)</td>
</tr>
<tr>
<td>$10^{-12}$ – $10^{-9}$</td>
<td>Haut Glacier d’Arolla, Switzerland (laboratory measurement)</td>
<td>Hubbard and Maltman (2000)</td>
</tr>
<tr>
<td>$10^{-11}$ – $10^{-9}$</td>
<td>Coastal exposure of glacial till, Traeth y Mwnt, Wales (laboratory measurement)</td>
<td>Hubbard and Maltman (2000)</td>
</tr>
<tr>
<td>$10^{-9}$</td>
<td>Willans Ice Stream, Antarctica (laboratory measurement)</td>
<td>Engelhardt and others (1990)</td>
</tr>
<tr>
<td>$10^{-9}$</td>
<td>Trarpiglacier, Canada (analysis of pressure freezing curves)</td>
<td>Waddington and Clarke (1995)</td>
</tr>
<tr>
<td>$10^{-8}$ – $10^{-8}$</td>
<td>Storglaciaren, Sweden (pressure wave propagation)</td>
<td>Fischer and others (1998)</td>
</tr>
<tr>
<td>$10^{-8}$</td>
<td>Storglaciaren, Sweden (laboratory measurement)</td>
<td>Iverson and others (1994)</td>
</tr>
<tr>
<td>$10^{-8}$</td>
<td>Trarpiglacier, Canada (laboratory measurement)</td>
<td>Murray and Clarke (1995)</td>
</tr>
<tr>
<td>$10^{-7}$ – $10^{-6}$</td>
<td>Sermiologyq Kujalleq (Store Glacier), Greenland (boorehole response tests)</td>
<td>This study</td>
</tr>
<tr>
<td>$10^{-7}$ – $10^{-5}$</td>
<td>Surface-exposures of glacial till, Snowy Range, Wyoming (infiltration tests)</td>
<td>Ronayne and others (2012)</td>
</tr>
<tr>
<td>$10^{-7}$ – $10^{-4}$</td>
<td>Haut Glacier d’Arolla, Switzerland (diurnal pressure wave propagation)</td>
<td>Hubbard and others (1995)</td>
</tr>
<tr>
<td>$10^{-7}$ – $10^{-4}$</td>
<td>South Cascade Glacier, USA (diurnal pressure wave propagation)</td>
<td>Fountain (1994)</td>
</tr>
<tr>
<td>$10^{-6}$</td>
<td>Breidamerkurjökull, Iceland (laboratory measurement)</td>
<td>Boulton and Dent (1974)</td>
</tr>
<tr>
<td>$10^{-5}$</td>
<td>Midre Lovenbreen, Svalbard (slug tests)</td>
<td>Kulessa and Murray (2003)</td>
</tr>
<tr>
<td>$10^{-4}$</td>
<td>Trarpiglacier, Canada (breakthrough response tests)</td>
<td>Stone and others (1997)</td>
</tr>
<tr>
<td>$10^{-3}$ – $10^{-2}$</td>
<td>Bakakinbreen, Svalbard (slug tests)</td>
<td>Kulessa and Murray (2003)</td>
</tr>
<tr>
<td>$10^{-2}$</td>
<td>Haut Glacier d’Arolla, Switzerland (slug tests)</td>
<td>Kulessa and others (2005)</td>
</tr>
<tr>
<td>$10^{-1}$</td>
<td>Gornergletscher, Switzerland (slug tests)</td>
<td>Iken and others (1996)</td>
</tr>
</tbody>
</table>
bed (i.e. a borehole) can open a gap at the ice-sediment interface, despite the low volumes of water involved, has implications for the establishment of subglacial drainage of the much larger water volumes supplied via moulins, crevasses and supraglacial lakes. It illustrates the manner in which regions of the basal environment can become hydrologically connected during peaks in water pressure. Hence, gap opening can explain transient periods of borehole water pressure synchrony that abruptly punctuate the often observed long-term pattern of anti-correlated variations in water pressure and velocity measured in hydraulically-isolated cavities during periods of high water pressure (e.g., Murray and Clarke, 1995; Engelhardt and Kamb, 1997; Harper and others, 2007; Andrews and others, 2014; Rada and Schoof, 2018). If areas of the bed that were previously hydraulically isolated experience net drainage as a result of gap opening at the ice-sediment interface, it may also explain the hydro-mechanical regulation of ice flow (e.g., Sole and others, 2013; Tedstone and others, 2015; Davison and others, 2020), which observations suggest cannot be entirely explained by water pressures within efficient channels (Andrews and others, 2014). It follows that drainage at the ice-sediment interface and Darcian flow through sediments with a low hydraulic conductivity may be two of potentially multiple processes behind the hypothesised weakly-connected component of the subglacial drainage system (Hoffman and others, 2016).

A drainage system consisting of cavities, which we assume are present at the base of our boreholes, linked via gaps opened at the ice-sediment interface would at first appear similar to the linked cavity theory of glacial drainage, which consists of cavities connected via narrow orifices (e.g., Kamb, 1987). There is, however, an important distinction in that the linked cavity model specifies that orifices are continuously open and water flow is inefficient and turbulent due to the length and narrowness of orifices (Kamb, 1987). Modification of the linked cavity theory to allow transient gap opening between cavities under high water pressure with turbulent flow would explain the same characteristics associated with linked cavity drainage systems: enhanced basal motion, sediment entrainment (as indicated by increased turbidity) and increased connectivity of the bed at times of high water pressure. It would also explain the existence of neighbouring yet behaviourally-independent subglacial drainage subsystems in close proximity (e.g., Murray and Clarke, 1995; Harper and others, 2007; Rada and Schoof, 2018), which the majority of previous models of subglacial drainage cannot reproduce as they inherently allow water to diffuse across the entire glacier bed (e.g., Schoof, 2010; Hewitt, 2013; Werder and others, 2013). This implies a strong link between subglacial hydraulics, stresses within the ice and basal motion that will be challenging to reproduce within numerical models due to the requirement to combine linear-elastic gap opening with a viscous ice rheology.

To date, every borehole drilled on Sermeq Kujalleq (Store Glacier) drained rapidly and immediately upon reaching the bed. This includes three boreholes at R30 in 2019, four boreholes at R29 in 2018 (unpublished), and seven boreholes at S30 in 2014 and 2016 (Doyle and others, 2018). A similar pattern of rapid borehole drainage, with a small number of exceptions, has been reported for Whillans Ice Stream in West Antarctica (Engelhardt and Kamb, 1997) and Sermeq Kujalleq (Jakobshavn Isbrae) in West Greenland (Lüthi, 1999). While the results presented here provide further evidence for gap opening as a mechanism for rapid borehole drainage, it also raises the question of why some boreholes on other ice masses do not drain rapidly upon reaching the bed. Some boreholes appear to never drain (e.g., Smart, 1996), while others drain slowly (e.g., Andrews and others, 2014), and others drain after a delay (e.g., Gordon and others, 2001; Kamb and Engelhardt, 1987; Engelhardt and Kamb, 1997; Fischer and Clarke, 2001). This heterogeneity, which often occurs within the same field site, could be explained by the stress regime, boreholes terminating blind in debris-rich basal ice before they are able to connect to the subglacial drainage system, or by the presence of impermeable barriers such as areas of ice-bedrock contact or cold ice, the latter of which can occur even within predominantly temperate glaciers (Robin, 1976). A detailed discussion of the heterogeneity of borehole drainage is not warranted here (see instead Smart, 1996 and Gordon and others, 2001), but we do seek an explanation for the homogeneity in borehole drainage observed to date on Sermeq Kujalleq (Store Glacier). Hot water drilling is ineffective at penetrating debris-rich basal ice, which is characteristic of many exposed margins of the Greenland Ice Sheet, for example, on Russell Glacier (Knight and others, 2002) and at the base of icebergs discharging from Sermeq Kujalleq (Jakobshavn Isbrae; Lüthi and others, 2009), yet none of the boreholes drilled to date on Sermeq Kujalleq (Store Glacier) terminated above the bed due to an obstruction by englacial clasts. We therefore speculate (while noting the small number of boreholes drilled at a limited number of sites) that debris content within basal ice on Sermeq Kujalleq (Store Glacier) may be low. If so, this could be explained by the removal of debris-rich basal ice formed upstream by basal melt. Furthermore, low (and potentially even negative) effective pressures (e.g. −46 ± 102 kPa at R30; Table 1) are conducive to hydraulic ice-bed separation (e.g., Schoof and others, 2012) and these conditions are found at all the Sermeq Kujalleq (Store Glacier) sites drilled to date. Modelling of subglacial drainage through a poroelastic sediment and cavity suggests that elastic gap opening is enabled by the suction of water from an underlying porous sediment layer without the requirement for a pre-wetted water film (Hewitt and others, 2018). We therefore conclude that rapid borehole drainage on Sermeq Kujalleq (Store Glacier) is facilitated by low effective pressures, subglacial sediment, and a potentially low debris content within basal ice.

Booth and others (2020) used the low basal reflectivity in vertical seismic profiles to infer that the subglacial sediment layer at site R30 has an acoustic impedance similar to that of basal ice, and from this, they suggested that the sediment is consolidated, and neither deforming nor lithified. The inference that the sediment layer is not deforming implies that the fast ice velocity at this site must be accommodated by either enhanced internal deformation of the ice, ice-sediment decoupling under high water pressure (e.g., Iverson and others, 1995, 2007), or deformation of a sediment layer thinner than the 5 – 10 m vertical resolution of the seismic technique. With regard to the last assertion we note that sediment deformation often occurs within an upper layer that is typically only decimetres to a few metres thick (e.g., Clarke, 1987; Murray, 1997; Humphrey and others, 1993; Engelhardt and Kamb, 1998), and that the shape of the pressure pulse during BH19g breakthrough can only be reproduced using the model of Hewitt and others (2018) if the sediment layer is deformable. While the extent of sediment deformation beneath this site remains inconclusive the evidence presented herein supports the hypothesis of ice-sediment decoupling under periods of high water pressure. Indeed, we suggest that the theory of gap opening at the ice-sediment interface (Engelhardt and Kamb, 1997) may involve the same physical process as ice-sediment decoupling envisaged by Iverson and others (1995). To explain the reverse tilt of inclinometers just below the ice-sediment interface, Iverson and others (1995) envisaged that sediment would be squeezed into the zone of uplift at times of high water pressure. The modulation of slip by pressurised water at the ice-sediment interface was confirmed by pump tests on a simulated prism of till on Engabreen (Iverson and others, 2007). Further evidence for gap opening and decoupling at the ice-sediment interface is provided by (as far as we are aware) unreported, direct observation of a cm-wide gap at the ice-sediment interface of Blue
Glacier, USA (Engelhardt and others, 1978). Borehole photog-

3raphy revealed a ~0.1 m thick sediment layer overlying bedrock

that was mechanically and visibly distinct from a 0.1 – 16.0 m

thick debris-laden basal ice layer. Engelhardt and others (1978)

guessed that the gap was opened by the overpressure of the

water-filled borehole and that basal sliding velocities were faster

where gaps were present. They also inferred that interstitial pres-

sure within the sediment must be close to or at the ice overburden

pressure in order to prevent the basal ice merging with the sedi-

ment layer through regelation, an assertion supported by Rempel

(2008). Hence, further in situ observations are required to inves-
tigate whether ice-sediment decoupling occurs via a gap at the ice-

sediment interface or through an increase in the thickness of the

sediment layer as proposed by Iverson and others (1995), or a

combination of both processes as modelled by Hewitt and others

(2018).

5. Conclusions

Detailed measurements of pressure pulses during a borehole
breakthrough event, and a decrease in hydraulic transmissivity
with time since breakthrough, provide evidence for hydraulic
gap opening and closure at the ice-sediment interface, with gaps
opening and closing in response to water pressure. Analysis of
the subsequent recovery of subglacial water pressure indicates
that the hydraulic conductivity of the subglacial sediment layer
3

is on the order of 10^{-7} – 10^{-6} m s^{-1}, which suggests it is coarse-
ground and more permeable than the fine-grained sediments
beneath West Antarctic ice streams. As seismic surveys suggest
that sediment at this site is not deforming, we infer that fast
basal motion may be accommodated by ice-sediment decoupling
and potentially shallow-depth sediment deformation in a layer
thinner than the 5 – 10 m resolution of the seismic technique.

Observations of a pressure drop simultaneous with the break-
through of a borehole 70 m away provides direct evidence for the
hypothesis that anti-correlations between water pressure in con-

cnected and unconnected regions of the bed can be explained

connected via elastic displacement of the ice roof.

We argue that water flow via gaps opened at the ice-sediment
interface is likely to play a critical role in both basal motion and
the development of subglacial hydrology on soft-bedded ice
masses, and that Darcian flow through sediments may explain
the drainage and recharge of areas of the bed that are otherwise
hydrologically isolated.

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Appendix A. List of symbols

\[\begin{align*}
\alpha & \quad \text{Surface and bed slope (°)} \\
\beta_w & \quad \text{Water compressibility (5.1 \times 10^{-10} \text{ Pa}^{-1})} \\
\gamma & \quad \text{Clausius–Clapeyron constant (9.14 \times 10^{-8} \text{ K Pa}^{-1})} \\
\delta & \quad \text{Gap width (m)} \\
\eta_i & \quad \text{Effective ice viscosity (Pa s\(^{-1}\))} \\
\eta_w & \quad \text{Water viscosity at 0°C (0.0018 Pa s)} \\
\rho_i & \quad \text{Ice density (910 ± 10 kg m\(^{-3}\))} \\
\rho_w & \quad \text{Water density at 0°C (999.8 kg m\(^{-3}\))} \\
\rho_d & \quad \text{Densities} \\
\tau_c & \quad \text{Effective stress (Pa)} \\
\phi & \quad \text{Areal fraction of the bed covered by gap} \\
A & \quad \text{Rate factor in Glen’s flow law (Pa s\(^{-1}\))} \\
b & \quad \text{Sediment thickness (m)} \\
B & \quad \text{Bending modulus of the ice (Pa m\(^3\))} \\
D & \quad \text{Time constant (s)} \\
E & \quad \text{Elastic modulus of ice (9.3 GPa)} \\
f & \quad \text{Shape factor} \\
f_D & \quad \text{Frictional drag coefficient} \\
F & \quad \text{Force on the drill tower (N)} \\
g & \quad \text{Gravitational acceleration (9.81 m s\(^{-2}\))} \\
h & \quad \text{Hydraulic head (m)} \\
h_0 & \quad \text{Reference hydraulic head (m)} \\
H_i & \quad \text{Ice thickness (m)} \\
H_w & \quad \text{Water height (m)} \\
K & \quad \text{Hydraulic conductivity (m s\(^{-1}\))} \\
M & \quad \text{Sediment stiffness (p-wave modulus) (Pa)} \\
\eta & \quad \text{Exponent in Glen’s flow law (3)} \\
N & \quad \text{Effective pressure (Pa)} \\
p_i & \quad \text{Ice overburden pressure (Pa)} \\
p_w & \quad \text{Subglacial water pressure (Pa)} \\
P_o & \quad \text{Triple point pressure of water (611.73 Pa)} \\
Q & \quad \text{Volumetric flux (m\(^3\) s\(^{-1}\))} \\
r & \quad \text{Radial distance (m)} \\
r_d & \quad \text{External borehole radius (0.015 m)} \\
r_0 & \quad \text{Borehole radius at base (m)} \\
r_s & \quad \text{Borehole radius at near-surface (m)} \\
R & \quad \text{Radius of influence (m)} \\
Re & \quad \text{Reynolds number} \\
s & \quad \text{Recharge (s = h - h_0) (m)} \\
s_0 & \quad \text{Reference recharge (m)} \\
S & \quad \text{Storage coefficient (m)} \\
t & \quad \text{Time (s)} \\
t_M & \quad \text{Maxwell time (s)} \\
T & \quad \text{Hydraulic transmissivity (m\(^2\) s\(^{-1}\))} \\
T_m & \quad \text{Melting temperature of ice (°C)} \\
T_w & \quad \text{Triple point temperature of water (273.16 K)} \\
U_\beta & \quad \text{Drill velocity (m min\(^{-1}\))} \\
U_w & \quad \text{Water velocity (m s\(^{-1}\))} \\
V & \quad \text{Volume (m\(^3\))} \\
W(u) & \quad \text{Well function} \\
z & \quad \text{Orthometric height (m)}
\end{align*}\]

Appendix B. Borehole radius

As the hose radius (r_d) and speed (U_\beta) are known, the differential rate of change in hydraulic head below and above the water line during the BH19g (e) pumping test allows the borehole radius at the water line (r_e) to be determined as follows. The total volumetric flux of water stored within the borehole when the drill hose was below the water line during PT2 is Q_{b2} = Q_{b2} + Q_{d2} or alternatively

\[Q_{b2} = (r_e^2 - r_d^2) \frac{dh_3}{dt} + r_d^2 U_\beta, \quad (B1)\]

where the numeric subscript indicates the period. Similarly the borehole radius at the time of borehole breakthrough predicted using the model of Greenler et al. (2014) over ten depth intervals ranging from the ice surface to the ice-sediment interface at a depth below the ice surface corresponding to the ice thickness (h_I)

Table B1. Borehole radii at the time of borehole breakthrough predicted using the model of Greenler et al. (2014) over ten depth intervals ranging from the ice surface to the ice-sediment interface at a depth below the ice surface corresponding to the ice thickness (h_I)

<table>
<thead>
<tr>
<th>Depth (m)</th>
<th>BH19c</th>
<th>BH19e</th>
<th>BH19g</th>
</tr>
</thead>
<tbody>
<tr>
<td>0 - 100</td>
<td>0.07</td>
<td>0.07</td>
<td>0.07</td>
</tr>
<tr>
<td>101 - 200</td>
<td>0.05</td>
<td>0.06</td>
<td>0.05</td>
</tr>
<tr>
<td>201 - 300</td>
<td>0.06</td>
<td>0.07</td>
<td>0.06</td>
</tr>
<tr>
<td>301 - 400</td>
<td>0.06</td>
<td>0.07</td>
<td>0.06</td>
</tr>
<tr>
<td>401 - 500</td>
<td>0.07</td>
<td>0.07</td>
<td>0.06</td>
</tr>
<tr>
<td>501 - 600</td>
<td>0.07</td>
<td>0.07</td>
<td>0.06</td>
</tr>
<tr>
<td>601 - 700</td>
<td>0.07</td>
<td>0.07</td>
<td>0.07</td>
</tr>
<tr>
<td>701 - 800</td>
<td>0.08</td>
<td>0.08</td>
<td>0.08</td>
</tr>
<tr>
<td>801 - 900</td>
<td>0.10</td>
<td>0.10</td>
<td>0.11</td>
</tr>
<tr>
<td>901 - h_I</td>
<td>0.10</td>
<td>0.10</td>
<td>0.11</td>
</tr>
<tr>
<td>Mean</td>
<td>0.07</td>
<td>0.08</td>
<td>0.07</td>
</tr>
</tbody>
</table>

storage flux with the drill stem above the water line during PT3 is

\[Q_{b3} = \frac{r_e^2}{2} \left( \frac{dh_3}{dt} \right). \quad (B2)\]

Assuming water input (Q_i) and output (Q_o) were constant at the transition from PT2 to PT3

\[Q_{b2} = Q_{b3}. \quad (B3)\]

Therefore equating fluxes gives

\[ (r_e^2 - r_d^2) \frac{dh_3}{dt} + r_d^2 U_\beta = \frac{r_e^2}{2} \left( \frac{dh_3}{dt} \right). \quad (B4)\]

Expanding on the left-hand side gives

\[r_e^2 \frac{dh_3}{dt} - r_d^2 \frac{dh_3}{dt} + r_d^2 U_\beta = \frac{r_e^2}{2} \frac{dh_3}{dt}. \quad (B5)\]

Rearranging gives

\[r_e^2 \frac{dh_3}{dt} - r_d^2 \frac{dh_3}{dt} = r_d^2 U_\beta - \frac{r_e^2}{2} \frac{dh_3}{dt}. \quad (B6)\]

and factorising gives

\[r_e^2 \left( \frac{dh_3}{dt} \right) = r_d^2 \left( U_\beta - \frac{dh_3}{dt} \right). \quad (B7)\]

which we rearrange to find

\[r_e = \left( \frac{r_d^2 (U_\beta - \frac{dh_3}{dt})}{\frac{dh_3}{dt} - \frac{dh_3}{dt}} \right)^{1/2}. \quad (B8)\]

Using Eqn (B8), the known hose radius (r_d = 0.015 m), the measured mean drill speed during PT2 (U_\beta = 8.82 m min\(^{-1}\)), and the rate of change in hydraulic head during PT2 (dh_3/dt = 1.36 m h\(^{-1}\)) and PT3 (dh_3/dt = 7.40 m h\(^{-1}\)), gives a borehole radius at the water line r_e = 0.14 m. This estimate is double that of the borehole model (r_e = 0.07 m; Table B1), but consistent with the borehole radius measured at the surface.

Measurements were not made of BH19g but BH19e had a radius at the surface of 0.17 m. As the pumping test period was not recorded in BH19c and BH19e we assume that their near-surface radius was the same as BH19g; that is, we assume r_e = 0.14 m for all response tests. Near-surface borehole radii larger than predicted by the Greener and others (2014) model could be explained by turbulent heat exchange from warm upwelling water. Laminar flow is specified in the model. The effect of turbulent heat exchange on borehole radius would decrease with depth so the model should perform better near the base. With no better estimate available, we therefore use the model output for the borehole radius at the base (r_{bg}; Table B1).
Appendix C. Elastic response of ice to borehole breakthrough

Here we consider the relative importance of viscous and elastic deformation in the response of the ice sheet at site R30 to borehole breakthrough forcing by calculating the Maxwell relaxation time

\[ t_M = \frac{\eta}{E}, \quad (C1) \]

where \( E = 9.3 \text{ GPa} \) is the elastic modulus for ice (Sinha, 1978), and \( \eta \) is the effective ice viscosity. The effective viscosity can be given as

\[ \eta = \frac{1}{2A} (r^2)^{\frac{n}{2}}, \quad (C2) \]

where \( A \) and \( n = 3 \) are the rate factor and exponent in Glen’s flow law, and \( \tau_e \) is the effective stress (Hutter, 1983). For simplicity, we estimate the effective stress as

\[ \tau_e = f \rho g H \sin \alpha, \quad (C3) \]

where, for site R30, \( f \approx 0.75 \) is the shape factor representing the proportion of driving stress supported by basal drag (Nye, 1952). Using Eqn (C3), the effective stress at site R30 is 121 kPa. We assume that viscous deformation will be greatest within the basal temperate ice layer and therefore use upper and lower limits of \( A \) for temperate ice of \( 5.5 - 2.4 \times 10^{-24} \text{ Pa}^{-3} \text{ s}^{-1} \) (Cuffey and Paterson, 2010). With these values the effective viscosity is \( 6.2 - 14.2 \times 10^{-12} \text{ Pa s}^{-1} \), and the Maxwell time is 11 – 25 min. Hence, assuming elastic ice rheology at site R30 is reasonable during the initial stages of gap opening. Over the time scales relevant to pumping and recovery tests viscous deformation should not be neglected and a viscoelastic model (e.g., Reeh and others, 2003) would be more appropriate. Note, however, that the rheology of the ice actually drops out of the asymptotic solution of the Hewitt and others (2018) model in Eqn (22), and so incorporating viscous deformation may not have a large effect on the predictions of transmissivity from that model.

Appendix D. Transmissivity from time constant

The hydraulic transmissivity (\( T_g \)) of a porous medium equivalent to a gap of uniform width \( \delta \) is given by de Marsily (1986) as

\[ T_g = \frac{d \phi \rho_s g}{12 \eta_w}. \quad (D1) \]

The time constant \( D \) is given by

\[ D = \frac{6 \eta_w r_i^2}{\delta \rho_s g \ln \frac{R}{r_0}}, \quad (D2) \]

which is Eqn (7a) of Weertman (1970) and Eqn (9) of Engelhardt and Kamb (1997). Combining Eqs (D1) and (D2) as follows allows the hydraulic transmissivity to be approximated from the time constant \( D \). Inserting \( \phi \) and then multiplying both sides of Eqn (D2) by two gives

\[ 2D = \frac{12 \eta_w r_i^2}{\delta \rho_s g \ln \frac{R}{r_0}}. \quad (D3) \]

This permits simplification by inserting the inverse of Eqn (D1) into Eqn (D3)

\[ 2D = \frac{1}{T_g} r_i^2 \ln \frac{R}{r_0}. \quad (D4) \]

Multiplying both sides by \( T_g \) gives

\[ 2D T_g = r_i^2 \ln \frac{R}{r_0}. \quad (D5) \]

And further rearranging gives

\[ T_g = \frac{r_i^2}{2D} \ln \frac{R}{r_0}. \quad (D6) \]

which is Eqn (8.7) of Lüthi (1999) and Eqn (27) of this paper.