Spectral theory of differential operators: what's it all about and what is its use Part III

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Spectral theory for systems

There are two main types of systems.

Type 1 Self-adjoint and semi-bounded system of m PDEs, each of even order 2n, on a compact d-dimensional manifold M with boundary ∂M . Requires mn boundary conditions.

Type 2 Self-adjoint system of *m* PDEs, each of odd order 2n - 1, on a compact *d*-dimensional manifold *M* without boundary. No requirement for system to be semi-bounded. In fact, the most interesting and physically meaningful examples are when the system is not semi-bounded. Think particle/antiparticle.

For type 1: second Weyl coefficient comes from the boundary ∂M .

For type 2: second Weyl coefficient comes from M itself.

For both types of systems the principal symbol is an $m \times m$ Hermitian matrix-function on $T^*M \setminus \{0\}$.

I will always assume that the eigenvalues of the principal symbol have constant multiplicity.

Moreover, for type 2 systems I will assume that the eigenvalues of the principal symbol are simple.