

## Interval arithmetic

	function	lower bound	upper bound	scale	
probability	$p$	$w^-$	$w^+$	$\mathbf{P}$	Gaussian
reciprocal	$1/p$	$1/w^+$	$1/w^-$	$\mathbf{P}^{-1}$	inverse Gaussian
alternate	$q = 1 - p$	$1 - w^+$	$1 - w^-$	$\mathbf{P}$	
weighted	$kp$	$kw^-$	$kw^+$	$\mathbf{P} \times k$	weighted Gaussian
square	$p^2$	$(w^-)^2$	$(w^+)^2$	$\mathbf{P}^2$	squared Gaussian
logit	$\text{logit}(p)$	$\text{logit}(w^-)$	$\text{logit}(w^+)$	$\mathfrak{R}$	Gaussian – (0 or 1)
increasing	$fn(p)$	$fn(w^-)$	$fn(w^+)$		
decreasing		$fn(w^+)$	$fn(w^-)$		
non-monotonic		$\min(fn(w^- \dots w^+))$	$\max(fn(w^- \dots w^+))$		
independent proportions					– applicable to Gaussian, same scale only
difference	$p_1 - p_2$	$p_1 - p_2 - \sqrt{(w_1^+ - p_1)^2 + (p_2 - w_2^-)^2}$	$p_1 - p_2 + \sqrt{(p_1 - w_1^-)^2 + (w_2^+ - p_2)^2}$		
sum	$p_1 + p_2$	$p_1 + p_2 - \sqrt{(p_1 - w_1^-)^2 + (p_2 - w_2^-)^2}$	$p_1 + p_2 + \sqrt{(w_1^+ - p_1)^2 + (w_2^+ - p_2)^2}$		
sum	$\Sigma p_i$	$\Sigma p_i - \sqrt{\sum (p_i - w_i^-)^2}$	$\Sigma p_i + \sqrt{\sum (w_i^+ - p_i)^2}$		
dependent proportions					– where $p_2 = fn(p_1)$
difference	$p_1 - p_2$	$w_1^- - w_2^+$	$w_1^+ - w_2^-$		
sum	$p_1 + p_2$	$w_1^- + w_2^-$	$w_1^+ + w_2^+$		
product	$p_1 \times p_2$	$w_1^- \times w_2^-$	$w_1^+ \times w_2^+$		