

# BrainPiglet

Full model details

## Contents

1	Settable Parameters	1
2	Derived Parameters	8
3	Model Variables	15
4	Temporary Variables	18
5	Reactions	23

## 1 Settable Parameters

Name	Model Name	Value	Units	Description
$CV_{inh}$	<b>CVinh</b>	1	none	a control parameter representing the action of complex V inhibitors
$C_{im}$	<b>C_im</b>	0.00675	mMmV <sup>-1</sup>	Capacitance of mitochondrial inner membrane
$C_v$	<b>C_v</b>	0.047	mmHg <sup>-1</sup>	Compliance of the veins (normalised)
$F$	<b>Fdy</b>	96.48	Cmmol <sup>-1</sup>	Faraday constant
$G_{VArat,n}$	<b>G_VAratn</b>	4	none	Normal ratio of conductances between arteries and veins $G_v/G_n$ (determines venous pressure) [16].

Name	Model Name	Value	Units	Description
$I$	Inh_glucN	50	none	the parameter which describes how strongly the AMP/ATP ratio inhibits the conversion of glucose to pyruvate
$K_\sigma$	K_sigma	10	none	parameter controlling sensitivity of $\sigma_e$ to radius
$L_{CV,0}$	L_CV0	0.4	none	normal complex V flux as a fraction of maximum possible flux
$L_{lk,frac}$	L_lkfrac	0.25	none	normal fraction of proton entry into mitochondria which is via leak channels
$P_a$	P_a	50	mmHg	arterial blood pressure
$P_a\text{CO}_2$	Pa_CO2	40	mmHg	arterial partial pressure of CO2
$P_a\text{CO}_{2,n}$	Pa_CO2n	40	mmHg	normal arterial partial pressure of CO2
$P_{a,n}$	P_an	50	mmHg	Normal value of ABP
$P_{ic,n}$	P_icn	4.5	mmHg	normal intracranial blood pressure
$P_{ic}$	P_ic	4.5	mmHg	intracranial blood pressure
$P_{vs}$	P_vs	1.5	mmHg	Pressure in the venous sinuses [12].
$R_C$	R_autc	2.2	none	parameter controlling sensitivity of $\eta$ to $P_a\text{CO}_2$
$R_O$	R_auto	1.5	none	parameter controlling sensitivity of $\eta$ to $[\text{O}_{2,c}]$
$R_P$	R_autp	4	none	parameter controlling sensitivity of $\eta$ to $P_a$
$R_u$	R_autu	0	none	parameter controlling sensitivity of $\eta$ to $u$

Name	Model Name	Value	Units	Description
$V_{\text{blood},n}$	blood_frac	0.0325	none	normal blood volume as a fraction of brain tissue volume
$V_{\text{mit}}$	Vol_mit	0.067	none	fraction of brain water which is mitochondria
$V_{t,n}$	Vol_totn	1	none	normal total blood volume
$Z$	Z	59.03	mV	$2.303*RT/F$
$\Delta\Psi_n$	Dpsi_n	145	mV	normal mitochondrial inner membrane potential
$\mathcal{E}_0(\text{Cu}_A)$	E_c0	247	mV	$\text{Cu}_A$ standard redox potential
$\mathcal{E}_0(\text{NADH})$	E_N0	-320	mV	NADH standard redox potential
$\mathcal{E}_0(\text{cyt } a_3)$	E_a30	350	mV	cyt a3 standard redox potential
$\text{CBF}_n$	CBFn	0.008	$\text{ml ml}^{-1} \text{s}^{-1}$	normal cerebral blood flow
$\text{CBF}_{\text{scale}}$	CBFscale	5000	cm	Ratio between $V_{\text{mca}}$ and CBF
$\text{CMRO}_{2,n}$	CMR02_n	0.02	$\text{mM s}^{-1}$	The resting CMRO2.
$\text{CMR}_{\text{gluc},n}$	CMRglucn	0.0044	$\text{mM s}^{-1}$	Normal rate of glucose metabolism for the brain [8].
$C_{\text{buffi}}$	C_buffi	0.022	none	buffering capacity for protons in mitochondria
$\text{Cu}_{A,\text{frac},n}$	a_frac_n	0.67	none	normal oxidised fraction of $\text{Cu}_A$
$K_{\text{eq,PCr}}^*$	k_PCcrATP_eq_ef	166	none	Effective equilibrium constant for the reaction in which phosphocreatine combines with ADP to give creatine and ATP [11]
$N_t$	NADpool	3	mM	total mitochondrial NAD + NADH concentration

Name	Model Name	Value	Units	Description
SaO <sub>2n</sub>	SaO2_n	0.96	none	normal saturation of the arterial haemoglobin
SaO <sub>2</sub>	SaO2sup	0.96	none	saturation of the arterial haemoglobin
VArat <sub>n</sub>	VArat_n	3	none	The normal ratio of the volume of the veins to the volume of the arteries
[ADP] <sub>n</sub>	_ADPn	0.012	mM	the normal concentration of ADP in the cytoplasm [14]
[ATP] <sub>n</sub>	_ATPn	2.2	mM	the normal concentration of ATP in the cytoplasm [5]
[CCO] <sub>tis</sub>	cytox_tot_tis	0.0022	mM	concentration of cytochrome c oxidase in tissue
[Hbtot] <sub>n</sub>	Xtot_n	5.4	mM	Normal total haemoglobin concentration in the arteries and veins.
[NAD] <sub>n</sub> /[NADH] <sub>n</sub>	NADNADHratn	1.5	none	normal NAD/NADH ratio
[O <sub>2</sub> ] <sub>n</sub>	O2_n	0.024	mM	normal oxygen concentration in mitochondria.
[PCr] <sub>n</sub>	_PCrn	2.6	mM	normal concentration of phosphocreatine in cell cytoplasm [5]
[PCr] <sub>n</sub> /[P <sub>i</sub> ] <sub>n</sub>	PCrPn	2.73	none	Normal Pcr/Pi concentration in the cytoplasm. Set this way because this is often measured by MRS (although mitochondria/cytoplasm differences are ignored).
[Py] <sub>n</sub>	_Py0n	0.1	mM	Normal concentration of pyruvate ions in the cytoplasm [7].
[gluc] <sub>n</sub>	_glucn	1.2	mM	Normal cellular concentration of glucose [1].
[gluc] <sub>c</sub>	gluc_c	5.3	mM	Concentration of glucose in the blood [15].
[lac] <sub>n</sub>	_L0n	3	mM	Normal concentration of lactate in the cytoplasm [13].

Name	Model Name	Value	Units	Description
[lac <sub>c</sub> ]	lac_c	2	mM	Capillary lactate concentration [15].
$\Delta G^\circ$	Gp0	-3.05e+04	J mol <sup>-1</sup>	Standard Gibbs free energy of ATP hydrolysis
$\Delta\text{HHb}_{\text{offset}}$	DHHb_offset	0	μM	an arbitrary baseline offset to the HHb signal (NIRS)
$\Delta\text{HbO}_2_{\text{offset}}$	DHbO2_offset	0	μM	an arbitrary baseline offset to the HbO <sub>2</sub> signal (NIRS)
$\Delta\text{HbT}_{\text{offset}}$	DHbT_offset	0	μM	an arbitrary baseline offset to the HbT signal (NIRS)
$\Delta\text{Hbdiff}_{\text{offset}}$	DHbdiff_offset	0	μM	an arbitrary baseline offset to the HHb signal (NIRS)
$\Delta\text{oxCCO}_{\text{offset}}$	CCO_offset	0	μM	an arbitrary baseline offset to the CCO signal (NIRS)
$\Delta p_{3,\text{corr}}$	Dp3_corr	-25	mV	$\Delta p_{30}$ minus normal PMF
dpH	dpH	0.001	none	a constant in the buffering relationship
$k_{\text{H},\text{O}_2}$	henry_02	0.0014	mMmmHg <sup>-1</sup>	constant setting relationship between oxygen saturation and oxygen concentration in artery
pH <sub>o</sub>	pH_o	7	none	extra-mitochondrial pH
pH <sub>m,n</sub>	pH_mn	7.4	none	normal mitochondrial pH
pH <sub>o,n</sub>	pH_on	7	none	normal extra-mitochondrial pH
$\mu_{\text{max}}$	mu_max	1	none	maximum value of mu
$\mu_{\text{min}}$	mu_min	-1	none	minimum value of mu
$\mu_n$	mu_n	0	none	normal value of mu

Name	Model Name	Value	Units	Description
$\phi$	phi	0.036	mM	value of O2 at half maximal saturation
$\sigma_{coll}$	sigma_coll	62.79	mmHg	value of pressure at which vessels collapse
$\sigma_{e0}$	sigma_e0	0.1425	mmHg	parameter in relationship determining $\sigma_e$
$\tau_{P_a}$	t_p	5	s	the time constant associated with $v_{P_a}$
$\tau_{CO_2}$	t_c	5	s	the time constant associated with $v_{CO_2}$
$\tau_{O_2}$	t_o	20	s	the time constant associated with $v_{O_2}$
$\tau_u$	t_u	0.5	s	the time constant associated with $v_u$
$c_3$	c3	0.11	$mV^{-1}$	parameter controlling the sensitivity of reaction 3 to PMF
$c_{k1}$	ck1	0.01	$mV^{-1}$	parameter controlling sensitivity of k1 to PMF
$c_{k2}$	ck2	0.02	$mV^{-1}$	parameter controlling sensitivity of k2 to PMF
$h_0$	h_0	0.003	cm	vascular wall thickness when radius is $r_0$
$k_{AK}^-$	k_nADPATP	379	$mM^{-1} s^{-1}$	the backward rate constant for the conversion of two molecules of ADP to one of ATP and one of AMP [10, 3].
$k_{MCT}$	k_lac_trans	2	mM	$k_m$ for the transport of lactate in and out of the cell. This is an average of the different types of MCT and the different cell types [1].
$k_{glut}$	k_gluc_trans	6.2	mM	$k_m$ for the transport of glucose in and out of the cell [9].
$k_{3,0}$	k30	2.5e+05	$mM^{-1} s^{-1}$	an apparent second-order rate constant for reaction 3 at zero PMF

Name	Model Name	Value	Units	Description
$k_{AK}$	k_ADPATP	1055	$\text{mM}^{-1} \text{s}^{-1}$	the forward rate constant for the conversion of two molecules of ADP to one of ATP and one of AMP [10, 3].
$k_{aut}$	k_aut	0.5	none	control parameter allowing destruction of autoregulation
$k_{lk2}$	k_lk2	0.038	$\text{mV}^{-1}$	Second constant controlling rate of $L_{lk}$ of $\Delta p$ .
$k_{m,ATP}$	km	0.025	none	Km for ATP use as a fraction of normal ATP concentration [10].
$k_{m,glucA,f}$	Km_glucNAf	0.2	none	Km for ADP in glycolysis as a fraction of normal ADP concentration [3].
$k_{m,glucG}$	Km_glucNg1	0.05	mM	Km for glucose in the caricature of glycolysis [6].
$k_{m,glucP,f}$	Km_glucNPf	0.2	none	Km for inorganic phosphate in glycolysis as a fraction of normal phosphate concentration [3].
$k_{m,tcaN,f}$	Km_NADf	0.6	none	$k_m$ for NAD in the TCA cycle as a fraction of normal NAD concentration
$k_{m,tcaP,f}$	Km_Pyf	0.005	none	$k_m$ for pyruvate in the TCA cycle as a fraction of normal pyruvate concentration
$k_{unc}$	k_unc	1	none	a parameter representing the action of uncouplers
$n_a$	na	4.33	none	number of protons passing through Complex V for each ATP synthesised [4]
$n_h$	n_h	2.5	none	Hill coefficient for haemoglobin saturation
$n_m$	n_m	1.83	none	exponent in the muscular tension relationship
$p_2$	p2	4	none	total protons pumped by reaction 2

$\infty$ 

Name	Model Name	Value	Units	Description
$p_{23}$	p23	8	none	total protons pumped by reactions 2 and 3
$p_{tot}$	p_tot	18.4	none	total protons pumped by reactions 1, 2 and 3
$r_0$	r_0	0.0126	cm	a special radius in the elastic tension relationship
$r_m$	r_m	0.027	cm	value of vessel radius giving maximum muscular tension
$r_n$	r_n	0.0187	cm	normal radius of blood vessels
$r_t$	r_t	0.018	cm	parameter in the muscular tension relationship
$r_{CV}$	r_CV	5	none	a parameter controlling the ratio of maximal to minimal rates of oxidative phosphorylation
$t_{1/2,pl}$	k_PytoLac_ht	10	s <sup>-1</sup>	Time constant for pyruvate to lactate interconversion
$t_{1/2,PCr}$	k_PCrATP_ht	2e-05	s	halftime for the reaction in which phosphocreatine combines with ADP to give creatine and ATP
$u$	u	1	none	The representation of "demand" in the model.
$u_n$	u_n	1	none	Resting "demand"

## 2 Derived Parameters

Name	Model Name	Expression	Value	Units
$C_{NADH,n}$	C_NADH_n	$\frac{Z}{2} \log \left( \frac{1}{[\text{NAD}]_n / [\text{NADH}]_n} \right)$	-5.197	mV



Name	Model Name	Expression	Value	Units
$D_{O_2}$	D_02	$\frac{J_{O_2,n}}{[O_{2,c}]_n - [O_2]_n}$	0.6796	$s^{-1}$
$E_2$	E_2	$\mathcal{E}_0(\text{cyt } a_3) - \mathcal{E}_0(\text{Cu}_A)$	103	mV
$E_{1,NADH,n}$	E1NADH_n	$\mathcal{E}_0(\text{Cu}_A) - \mathcal{E}_0(\text{NADH}) + C_{\text{NADH},n}$	561.8	mV
$E_{1,n}$	E_1n	$E_{1,NADH,n}$	561.8	mV
$G_n$	Gn	$\frac{\text{CBF}_n(1+G_{\text{VArat},n})}{G_{\text{VArat},n}(P_{a,n}-P_{vs})}$	0.0002062	$\text{mmHg}^{-1} s^{-1}$
$G_v$	G_v	$G_{\text{VArat},n} G_n$	0.0008247	$\text{mmHg}^{-1} s^{-1}$
$J_{O_2,n}$	J_02n	$\text{CMRO}_{2,n}$	0.02	$\text{mM s}^{-1}$
$K_G$	K_G	$\frac{G_n}{r_n^4}$	1686	$\text{mmHg}^{-1} s^{-1} \text{cm}^{-4}$
$L_n$	L_n	$p_{\text{tot}} f_n$	5.492	$\text{mM s}^{-1}$
$L_{CV,\text{frac}}$	L_CVfrac	$1 - L_{lk,\text{frac}}$	0.75	none
$L_{CV,\text{max}}$	L_CVmax	$\frac{L_{CV,n}}{L_{CV,0}}$	10.3	$\text{mM s}^{-1}$
$L_{CV,n}$	L_CVn	$L_n L_{CV,\text{frac}}$	4.119	$\text{mM s}^{-1}$
$L_{lk,n}$	L_lkn	$L_n L_{lk,\text{frac}}$	1.373	$\text{mM s}^{-1}$
$L_{lk0}$	L_lk0	$\frac{L_{lk,n}}{\exp(\Delta p_n k_{lk2}) - 1}$	0.002269	$\text{mM s}^{-1}$
$P_{1,n}$	P_1n	$\frac{P_{a,n} + P_{v,n}}{2}$	30.6	mmHg
$P_{v,n}$	P_vn	$\frac{G_v P_{vs} + G_n P_{a,n}}{G_n + G_v}$	11.2	mmHg

Name	Model Name	Expression	Value	Units
$T_{\max,n}$	T_maxn	$\frac{T_{m,n}}{\exp\left(-\left(\frac{r_n-r_m}{r_t-r_m}\right)^{nm}\right)}$	1.383	mmHg cm
$T_{\max 0}$	T_max0	$\frac{T_{\max,n}}{1+k_{aut}\mu_n}$	1.383	mmHg cm
$T_{e,n}$	T_en	$\sigma_{e,n}h_n$	-0.09604	mmHg cm
$T_{m,n}$	T_mn	$(P_{1,n} - P_{ic,n})r_n - T_{e,n}$	0.5841	mmHg cm
$V_{a,n}$	Vol_artn	$\frac{V_{t,n}}{1+VArat_n}$	0.25	none
$V_{v,n}$	Vol_venn	$V_{t,n} \frac{VArat_n}{1+VArat_n}$	0.75	none
[HHb <sub>a</sub> ]	Xa	[Hbtot] (1 - SaO2)	0.216	mM
[O <sub>2,a</sub> ]	O2a	$\phi \left( \frac{SaO2}{1-SaO2} \right)^{\frac{1}{n_h}}$	0.1283	mM
$\Delta G_{1,n}$	DG1_n	$-4 \left( E_{1,n} + Z \log \left( \frac{Cu_{A,o,n}}{Cu_{A,o,n}} \right) \right) + p_1 \Delta p_n$	-566.3	mV
$\Delta G_{2,n}$	DG2_n	$-4 \left( E_2 + Z \left( \log \left( \frac{Cu_{A,o,n}}{Cu_{A,o,n}} \right) - \log \left( \frac{[a3r]_n}{a3_{o,n}} \right) \right) \right) + p_2 \Delta p_n$	-39.7	mV
$\Delta \Psi_{init}$	Dpsi_init	$\Delta \Psi_n$	145	mV
$Cu_{A,o,n}$	ared_n	[CCO] <sub>mit</sub> - Cu <sub>A,o,n</sub>	0.01084	mM
$Cu_{A,o,init}$	a_init	Cu <sub>A,o,n</sub>	0.022	mM
$Cu_{A,o,n}$	a_n	[CCO] <sub>mit</sub> Cu <sub>A,frac,n</sub>	0.022	mM
HHb <sub>n</sub>	HHbn	$1000 \frac{V_{a,n} [HHb_a]_n + V_{v,n} [HHb_v]_n}{4} V_{blood,n}$	16.99	μM
$H_{m,init}^+$	H_init	$H_{m,n}^+$	3.981e-05	mM

Name	Model Name	Expression	Value	Units
$H_{m,n}^+$	H_n	$10^{3-pH_{m,n}}$	3.981e-05	mM
HbO <sub>2n</sub>	HbO2n	$1000 \frac{V_{a,n}[HbO_{2,a}]_n + V_{v,n}[HbO_{2,v}]_n}{4} V_{blood,n}$	26.89	μM
Hbt <sub>n</sub>	HbTn	$1000 \frac{(V_{a,n} + V_{v,n})[Hbtot]_n}{4} V_{blood,n}$	43.88	μM
$K_{eq,PCr}$	k_PCrATP_eq	$\frac{K_{eq,PCr}^*}{[H^+]_n}$	1.66e+06	mM <sup>-1</sup>
$K_{eq1,n}$	Keq1_n	$10^{\frac{-1}{Z} ( \frac{p1 \Delta p_n}{4} - E_{1,n} )}$	123.2	none
$K_{eq2,n}$	Keq2_n	$10^{\frac{-1}{Z} ( \frac{p2 \Delta p_n}{4} - E_2 )}$	0.07735	none
$K_{eqADPATP}$	k_ADPATP_eq	$\frac{k_{AK}}{k_{AK}^-}$	2.784	none
NADH <sub>n</sub>	NADHn	$N_t - [NAD]_n$	1.2	mM
PaO <sub>2</sub>	PaO2	$\frac{[O_{2,a}]}{k_{H,O_2}}$	91.68	mmHg
ScO <sub>2n</sub>	ScO2_n	$\frac{SaO_{2n} + SvO_{2n}}{2}$	0.7285	none
SvO <sub>2n</sub>	SvO2_n	$\frac{[HbO_{2,v}]_n}{[Hbtot]_n}$	0.497	none
$V_{glucosein}$	v_gluc_in	$\frac{[gluc_c]}{k_{glut} + [gluc_c]}$	0.4609	none
$V_{lacin}$	v_lac_in	$\frac{[lac_c]}{k_{MCT} + [lac_c]}$	0.5	none
[AMP] <sub>n</sub>	_AMPn	$\frac{K_{eqADPATP} [ADP]_n^2}{[ATP]_n}$	0.0001822	mM
[CCO] <sub>mit</sub>	cytox_tot	$\frac{[CCO]_{tis}}{V_{mit}}$	0.03284	mM

Name	Model Name	Expression	Value	Units
$[\text{Cr}]_n$	_Crn	$\frac{K_{\text{eq,PCr}}[\text{ADP}]_n[\text{PCr}]_n}{[\text{ATP}]_n}$	2.354	mM
$[\text{HHb}_a]_n$	Xa_n	$[\text{Hbtot}]_n (1 - \text{SaO}_2)_n$	0.216	mM
$[\text{HHb}_v]_n$	Xv_n	$[\text{Hbtot}]_n - [\text{HbO}_{2,v}]_n$	2.716	mM
$[\text{H}^+]_n$	_Hyn	$1000 \times 10^{-\text{pH}_{o,n}}$	0.0001	mM
$[\text{H}^+]$	_Hy	$1000 \times 10^{-\text{pH}_o}$	0.0001	mM
$[\text{HbO}_{2,a}]_n$	X0a_n	$[\text{Hbtot}]_n \text{SaO}_2_n$	5.184	mM
$[\text{HbO}_{2,a}]$	X0a	$[\text{Hbtot}] \text{SaO}_2$	5.184	mM
$[\text{HbO}_{2,v}]_n$	X0v_n	$\frac{\text{CBF}_n[\text{HbO}_{2,a}]_n - J_{\text{O}_2,n}}{\text{CBF}_n}$	2.684	mM
$[\text{HbO}_{2,v}]_{\text{init}}$	X0v_init	$[\text{HbO}_{2,v}]_n$	2.684	mM
$[\text{Hbtot}]$	Xtot	$[\text{Hbtot}]_n$	5.4	mM
$[\text{NAD}]_n$	NADn	$\frac{N_t}{1 + \frac{[\text{NAD}]_n}{[\text{NADH}]_n}}$	1.8	mM
$[\text{O}_2]_{\text{init}}$	O2_init	$[\text{O}_2]_n$	0.024	mM
$[\text{O}_{2,c}]_n$	O2c_n	$\phi \left( \frac{\text{ScO}_2}_n}{1 - \text{ScO}_2}_n \right)^{\frac{1}{n_h}}$	0.05343	mM
$[\text{O}_{2,c}]_{\text{init}}$	O2c_init	$[\text{O}_{2,c}]_n$	0.05343	mM
$[\text{P}]_n$	_Pn	$\frac{[\text{PCr}]_n}{[\text{PCr}]_n / [\text{P}]_n}$	0.9524	mM
$[\text{a3r}]_n$	bred_n	$\frac{f_n (1 + \exp(-c_3(\Delta p_n - \Delta p_{30})))}{k_3 [\text{O}_2]_n \exp(-c_3(\Delta p_n - \Delta p_{30}))}$	0.000828	mM

Name	Model Name	Expression	Value	Units
$[a3r]_{\text{init}}$	<b>bred_init</b>	$[a3r]_n$	0.000828	mM
$\Delta G_n$	DGpn	$\Delta G^\circ + ZF \log(g_{p,n})$	-6.06e+04	J mol <sup>-1</sup>
$\Delta pH_n$	DpH_n	$pH_{m,n} - pH_{o,n}$	0.4	none
$\Delta p_n$	Dp_n	$\Delta \Psi_n + Z \Delta pH_n$	168.6	mV
$\Delta p_{CV0}$	Dp_CV0	$\frac{-\Delta G_n}{n_a F}$	145	mV
$\Delta p_{30}$	Dp_30	$\Delta p_n + \Delta p_{3,\text{corr}}$	143.6	mV
$a3_{\text{frac},n}$	<b>b_frac_n</b>	$1 - \frac{[a3r]_n}{[CCO]_{\text{mit}}}$	0.9748	none
$a3_{o,n}$	<b>b_n</b>	$[CCO]_{\text{mit}} - [a3r]_n$	0.03201	mM
$\text{glyc}_{a,n}$	<b>glyc_an</b>	$\frac{[ADP]_n^2}{k_{m,\text{glycA}} + [ADP]_n^2}$	0.9615	none
$\text{glyc}_{g,n}$	<b>glyc_gn</b>	$\frac{[\text{gluc}]_n}{k_{m,\text{glycG}} + [\text{gluc}]_n}$	0.96	none
$\text{glyc}_{p,n}$	<b>glyc_pn</b>	$\frac{[P]_n^2}{k_{m,\text{glycP}} + [P]_n^2}$	0.9615	none
$k_{1,n}$	<b>k1_n</b>	$\frac{f_n}{C_{\text{UA},o,n} - \frac{1}{K_{\text{eq1},n}} C_{\text{UA},o,n}}$	13.62	s <sup>-1</sup>
$k_{2,n}$	<b>k2_n</b>	$\frac{f_n}{C_{\text{UA},o,n} a3_{o,n} - \frac{1}{K_{\text{eq2},n}} C_{\text{UA},o,n} [a3r]_n}$	2681	mM <sup>-1</sup> s <sup>-1</sup>
$\nu_{P_a,n}$	<b>v_pn</b>	$P_{a,n}$	50	mmHg
$\nu_{\text{CO}_2,n}$	<b>v_cn</b>	$P_a \text{CO}_{2,n}$	40	mmHg
$\nu_{\text{O}_2,n}$	<b>v_on</b>	$[\text{O}_{2,c}]_n$	0.05343	mM

Name	Model Name	Expression	Value	Units
$\nu_{u,n}$	v_un	$u_n$	1	none
$\sigma_{e,n}$	sigma_en	$\sigma_{e0} \left( \exp \left( \frac{K_\sigma(r_n - r_0)}{r_0} \right) - 1 \right) - \sigma_{coll}$	-44.89	mmHg
$f_n$	f_n	$\frac{CMRO_{2,n}}{V_{mit}}$	0.2985	mM s <sup>-1</sup>
$g_{p,n}$	gp_n	$\frac{[ADP]_n [P]_n}{1000 [ATP]_n}$	5.195e-06	none
$h_n$	h_n	$-r_n + \sqrt{r_n^2 + 2r_0 h_0 + h_0^2}$	0.00214	cm
$k_{PCr}^-$	k_nPCrATP	$\frac{\ln(2)}{(K_{eq,PCr} [PCr]_n [ADP]_n + [Cr]_n + [ATP]_n) t_{1/2,PCr}}$	0.6691	mM <sup>-1</sup> s <sup>-1</sup>
$k_{pl}^-$	k_nPytoLac	$t_{1/2,pl}$	10	s <sup>-1</sup>
$k_3$	k3	$\frac{k_{3,0}(1 + \exp(-c3(0 - \Delta p_{30})))}{\exp(-c3(0 - \Delta p_{30}))}$	2.5e+05	mM <sup>-1</sup> s <sup>-1</sup>
$k_{PCr}$	k_PCcrATP	$\frac{\ln(2)}{([PCr]_n [ADP]_n + \frac{[Cr]_n + [ATP]_n}{K_{eq,PCr}}) t_{1/2,PCr}} [H^+]$	111.1	mM <sup>-1</sup> s <sup>-1</sup>
$k_m$	kmATP	$[ATP]_n k_{m,ATP}$	0.055	mM
$k_{CV}$	kCV	$\frac{-1}{\Delta p_n - \Delta p_{CV0}} \ln \left( \frac{1 - L_{CV,0}}{1 + r_{CV} L_{CV,0}} \right)$	0.06829	mV <sup>-1</sup>
$k_{TCA_n}$	k_TCA_n	$\frac{1}{3} \frac{CMRO_{2,n}}{V_{mit}}$	0.0995	mM s <sup>-1</sup>
$k_{pl}$	k_PytoLac	$\frac{(2CMR_{gluc,n} - \frac{CMRO_{2,n}}{3} + k_{pl}^- [lac]_n) [H^+]}{[Py]_n [H^+]_n}$	300	s <sup>-1</sup>
$k_{m,glycA}$	Km_glycNA	$k_{m,glycA,f} [ADP]_n$	0.0024	mM
$k_{m,glycP}$	Km_glycNP	$k_{m,glycP,f} [P]_n$	0.1905	mM

Name	Model Name	Expression	Value	Units
$k_{m,tcaN}$	Km_NAD	$k_{m,tcaN,f}[\text{NAD}]_n$	1.08	mM
$k_{m,tcaP}$	Km_Py	$k_{m,tcaP,f}[\text{Py}]_n$	0.0005	mM
$p_1$	p1	$p_{tot} - p_{23}$	10.4	none
$p_3$	p3	$p_{23} - p_2$	4	none
$r_{init}$	r_init	$r_n$	0.0187	cm
$v_{MCT}$	v_lac_trans	$\frac{2\text{CMR}_{\text{gluc},n} - \frac{\text{CMRO}_{2,n}}{3}}{\frac{[\text{lac}]_n}{[\text{lac}]_n + k_{\text{MCT}}} - V_{\text{lacin}}}$	0.02133	$\text{mM s}^{-1}$
$v_{\text{glut}}$	v_gluc_trans	$\frac{\text{CMR}_{\text{gluc},n}}{V_{\text{glucosein}} - \frac{[\text{gluc}]_n}{[\text{gluc}]_n + k_{\text{glut}}}}$	0.01473	$\text{mM s}^{-1}$
$v_{\text{TCA}}$	v_TCA	$\frac{k_{\text{TCA}_n}}{[\text{Py}]_n[\text{NAD}]_n} (k_{m,tcaN} + [\text{NAD}]_n) (k_{m,tcaP} + [\text{Py}]_n)$	0.16	$\text{mM s}^{-1}$
$v_{\text{glyc},n}$	Vmax_glucNn	$\frac{\text{CMR}_{\text{gluc},n}}{\text{glyc}_{g,n}\text{glyc}_{p,n}\text{glyc}_{a,n}}$	0.004957	$\text{mM s}^{-1}$

### 3 Model Variables

Name	Model Name	Expression	Initial Value	Units	Description
$[\text{HbO}_{2,v}]$	X0v	$\text{CBF} ([\text{HbO}_{2,a}] - [\text{HbO}_{2,v}]) - J_{\text{O}_2}$	2.684	mM	The concentration of bound oxygen in the veins.
$\Delta\Psi$	Dpsi	$\frac{d\Delta\Psi}{dt} = \frac{p_2 f_2 + p_1 f_1 + p_3 f_3 - L}{C_{im}}$	145	mV	mitochondrial inner membrane potential

Name	Model Name	Expression	Initial Value	Units	Description
$\text{Cu}_{\text{A,o}}$	a	$\frac{d\text{Cu}_{\text{A,o}}}{dt} = 4T_{\text{a,ox}} - 4T_{\text{a,red}}$	0.022	mM	The concentration of oxidised cytochrome-c-oxidase
$\text{H}_{\text{m}}^+$	H	$\frac{d\text{H}_{\text{m}}^+}{dt} = \frac{-p_2 T_{\text{a,ox}}}{R_{\text{Hi}}} - \frac{p_1 T_{\text{a,red}}}{R_{\text{Hi}}} - \frac{p_3 T_{\text{b,ox}}}{R_{\text{Hi}}} + \frac{T_{\text{psi,out}}}{R_{\text{Hi}}}$	3.981e-05	mM	concentration of hydrogen ions in mitochondria
[ADP]	_ADP	$\frac{d[\text{ADP}]}{dt} = -T_{\text{PCrtoATP}} - T_{\text{ADPtoATP}} + T_{\text{ATPtoADP}} - 2T_{\text{aden1}} - 2T_{\text{glycol}}$	0.012	mM	ADP concentration in cytoplasm and mitochondria [2]
[AMP]	_AMP	$\frac{d[\text{AMP}]}{dt} = T_{\text{aden1}}$	0.0001822	mM	AMP concentration in cytoplasm
[ATP]	_ATP	$\frac{d[\text{ATP}]}{dt} = T_{\text{PCrtoATP}} + T_{\text{ADPtoATP}} - T_{\text{ATPtoADP}} + T_{\text{aden1}} + 2T_{\text{glycol}}$	2.2	mM	ATP concentration in cytoplasm and mitochondria
[Cr]	_Cr	$\frac{d[\text{Cr}]}{dt} = T_{\text{PCrtoATP}}$	2.354	mM	creatine concentration in cytoplasm
[NAD]	NAD	$\frac{d[\text{NAD}]}{dt} = 2T_{\text{a,red}} - 6T_{\text{TCA}}$	1.8	mM	Concentration of NAD in the mitochondria
$[\text{O}_{2,\text{c}}]$	02c	$\phi \left( \frac{\text{ScO}_2}{1 - \text{ScO}_2} \right)^{\frac{1}{n_h}} - [\text{O}_{2,\text{c}}]$	0.05343	mM	The concentration of oxygen in the capillary.
$[\text{O}_2]$	02	$\frac{d[\text{O}_2]}{dt} = -T_{\text{b,ox}} + \frac{T_{\text{O}_2,\text{in}}}{V_{\text{mit}}}$	0.024	mM	The concentration of oxygen in the mitochondria
[PCr]	_PCr	$\frac{d[\text{PCr}]}{dt} = -T_{\text{PCrtoATP}}$	2.6	mM	phosphocreatine concentration in cytoplasm



Name	Model Name	Expression	Initial Value	Units	Description
[Pi]	_P	$\frac{d[\text{Pi}]}{dt} = -T_{\text{ADPtoATP}} + T_{\text{ATPtoADP}} - 2T_{\text{glycol}}$	0.9524	mM	Inorganic phosphate concentration in cytoplasm and mitochondria
[Py]	_Py0	$\frac{d[\text{Py}]}{dt} = 2T_{\text{glycol}} - T_{\text{PytoLac}} - \frac{T_{\text{TCA}}V_{\text{mit}}}{1}$	0.1	mM	Concentration of pyruvate in the cytoplasm
[a3r]	bred	$\frac{d[\text{a3r}]}{dt} = 4T_{\text{a.ox}} - 4T_{\text{b.ox}}$	0.000828	mM	concentration of reduced cyt a3 in mitochondria
[gluc]	_gluc	$\frac{d[\text{gluc}]}{dt} = -T_{\text{glycol}} + T_{\text{glucose.in}} - T_{\text{glucose.out}}$	1.2	mM	Concentration of glucose in the cytoplasm
[lac]	_L0	$\frac{d[\text{lac}]}{dt} = T_{\text{PytoLac}} + T_{\text{lactate.in}} - T_{\text{lactate.out}}$	3	mM	Concentration of lactate in the cytoplasm
$\nu_u$	v_u	$\frac{d\nu_u}{dt} = \frac{1}{\tau_u} (u - \nu_u)$	1	none	The demand parameter u passed through a first order filter.
$\nu_{P_a}$	v_p	$\frac{d\nu_{P_a}}{dt} = \frac{1}{\tau_{P_a}} (P_a - \nu_{P_a})$	50	mmHg	ABP passed through a first order filter.
$\nu_{\text{CO}_2}$	v_c	$\frac{d\nu_{\text{CO}_2}}{dt} = \frac{1}{\tau_{\text{CO}_2}} (P_a \text{CO}_2 - \nu_{\text{CO}_2})$	40	mmHg	CO2 passed through a first order filter.
$\nu_{\text{O}_2}$	v_o	$\frac{d\nu_{\text{O}_2}}{dt} = \frac{1}{\tau_{\text{O}_2}} ([\text{O}_{2,c}] - \nu_{\text{O}_2})$	0.05343	mM	capillary O2 passed through a first order filter.
$r$	r	$T_e + T_m - (P_1 - P_{ic}) r$	0.0187	cm	typical radius of cerebral vessels

## 4 Temporary Variables

Name	Model Name	Expression	Initial Value	Units
$C_{0i}$	C_0i	$\frac{10^{-\text{pH}_m} - 10^{-\text{pH}_m - \text{dpH}}}{\text{dpH}}$	9.156e-08	none
$C_{\text{NADH}}$	C_NADH	$\frac{Z}{2} \log \left( \frac{1}{[\text{NAD}]/[\text{NADH}]} \right)$	-5.197	mV
$E_1$	E_1	$E_{1,\text{NADH}}$	561.8	mV
$E_{1,\text{NADH}}$	E1NADH	$\mathcal{E}_0(\text{Cu}_A) - \mathcal{E}_0(\text{NADH}) + C_{\text{NADH}}$	561.8	mV
$G$	G	$K_G r^4$	0.0002062	mmHg <sup>-1</sup> s <sup>-1</sup>
$J_{\text{O}_2, \text{min}}$	JO2	$\min(D_{\text{O}_2} ([\text{O}_{2,c}] - [\text{O}_2]), \text{CBF}[\text{HbO}_{2,a}])$	0.02	mM s <sup>-1</sup>
$J_{\text{O}_2}$	J_O2	$J_{\text{O}_2, \text{min}}$	0.02	mM s <sup>-1</sup>
$L$	L	$L_{\text{CV}} + L_{\text{lk}}$	5.494	mM s <sup>-1</sup>
$L_{\text{CV}}$	L_CV	$\frac{CV_{\text{inh}} L_{\text{CV}, \text{max}} (1 - e^{-\theta})}{1 + r_{\text{CV}} e^{-\theta}}$	4.12	mM s <sup>-1</sup>
$L_{\text{lk}}$	L_lk	$k_{\text{unc}} L_{\text{lk}0} (\exp(\Delta p k_{\text{lk}2}) - 1)$	1.373	mM s <sup>-1</sup>
$P_1$	P_1	$\frac{P_a + P_v}{2}$	30.6	mmHg
$P_v$	P_v	$\frac{G_v P_{vs} + G P_a}{G + G_v}$	11.2	mmHg
$R_{\text{ATPtoADP}}$	R_ATPtoADP	$\frac{[\text{ATP}]}{k_m + [\text{ATP}]}$	0.9756	none
$R_{\text{glucose\_in}}$	R_glucose_in	$V_{\text{glucosein}}$	0.4609	none
$R_{\text{glucose\_out}}$	R_glucose_out	$\frac{[\text{gluc}]}{k_{\text{glut}} + [\text{gluc}]}$	0.1622	none

Name	Model Name	Expression	Initial Value	Units
$R_{\text{glycol}}$	R_glycol	$\frac{[\text{ADP}]^2[\text{P}_i]^2[\text{gluc}]}{(k_{m,\text{glycA}}^2 + [\text{ADP}]^2)(k_{m,\text{glycP}}^2 + [\text{P}_i]^2)(k_{m,\text{glycG}} + [\text{gluc}])}$	0.8876	none
$R_{\text{lactate.in}}$	R_lactate_in	$V_{\text{lacin}}$	0.5	none
$R_{\text{lactate.out}}$	R_lactate_out	$\frac{[\text{lac}]}{k_{\text{MCT}} + [\text{lac}]}$	0.6	none
$T_e$	T_e	$\sigma_e h$	-0.09604	mmHg cm
$T_m$	T_m	$T_{\text{max}} \exp\left(-\left(\left \frac{r-r_m}{r_t-r_m}\right \right)^{n_m}\right)$	0.5841	mmHg cm
$T_{\text{ADPtoATP}}$	T_ADPToATP	$k_{\text{ATP,Cv}}$	0.06376	$\text{mM s}^{-1}$
$T_{\text{ATPtoADP}}$	T_ATPtoADP	$\frac{V_{\text{max,ATP}}[\text{ATP}]}{k_m + [\text{ATP}]}$	0.07254	$\text{mM s}^{-1}$
$T_{\text{O2.in}}$	T_O2_in	$J_{\text{O2}}$	0.02	$\text{mM s}^{-1}$
$T_{\text{PCrtoATP}}$	T_PCrtoATP	$k_{\text{PCr}}[\text{PCr}][\text{ADP}] - k_{\text{PCr}}^-[\text{ATP}][\text{Cr}]$	-9.728e-05	$\text{mM s}^{-1}$
$T_{\text{PytoLac}}$	T_PytoLac	$k_{\text{pl}}[\text{Py}] - k_{\text{pl}}^-[\text{lac}]$	0.002	$\text{mM s}^{-1}$
$T_{\text{TCA}}$	T_TCA	$k_{\text{TCA}}$	0.0995	$\text{mM s}^{-1}$
$T_{\text{a.ox}}$	T_a_ox	$f_2$	0.2985	$\text{mM s}^{-1}$
$T_{\text{a.red}}$	T_a_red	$f_1$	0.2985	$\text{mM s}^{-1}$
$T_{\text{aden1}}$	T_aden1	$k_{\text{AK}}[\text{ADP}]^2 - k_{\text{AK}}^-[\text{ATP}][\text{AMP}]$	1.64e-06	$\text{mM s}^{-1}$
$T_{\text{b.ox}}$	T_b_ox	$f_3$	0.2985	$\text{mM s}^{-1}$
$T_{\text{glucose.in}}$	T_glucose_in	$v_{\text{glut}} V_{\text{glucosein}}$	0.006789	$\text{mM s}^{-1}$

Name	Model Name	Expression	Initial Value	Units
$T_{\text{glucose\_out}}$	T_glucose_out	$\frac{v_{\text{glut}}[\text{gluc}]}{k_{\text{glut}} + [\text{gluc}]}$	0.002389	$\text{mM s}^{-1}$
$T_{\text{glycol}}$	T_glycol	$\frac{v_{\text{glyc}}[\text{ADP}]^2[\text{P}_i]^2[\text{gluc}]}{(k_{m,\text{glycA}} + [\text{ADP}]^2)(k_{m,\text{glycP}} + [\text{P}_i]^2)(k_{m,\text{glycG}} + [\text{gluc}])}$	0.0044	$\text{mM s}^{-1}$
$T_{\text{lactate\_in}}$	T_lactate_in	$v_{\text{MCT}} V_{\text{lacin}}$	0.01067	$\text{mM s}^{-1}$
$T_{\text{lactate\_out}}$	T_lactate_out	$\frac{v_{\text{MCT}}[\text{lac}]}{k_{\text{MCT}} + [\text{lac}]}$	0.0128	$\text{mM s}^{-1}$
$T_{\text{max}}$	T_max	$T_{\text{max0}} (1 + k_{\text{aut}}\mu)$	1.383	$\text{mmHg cm}$
$T_{\text{psi\_out}}$	T_psi_out	$L$	5.494	$\text{mM s}^{-1}$
$V_{\text{a}}$	Vol_art	$V_{\text{a,n}} \left(\frac{r}{r_n}\right)^2$	0.25	none
$V_{\text{t}}$	Vol_tot	$V_{\text{a}} + V_{\text{v}}$	1	none
$V_{\text{v}}$	Vol_ven	$V_{\text{v,n}} + C_v (P_v - P_{\text{v,n}})$	0.75	none
$V_{\text{mca}}$	Vmca	CBFCBFscale	40	$\text{cm s}^{-1}$
[HHb <sub>v</sub> ]	Xv	[Hbtot] - [HbO <sub>2,v</sub> ]	2.716	mM
$\Delta G_1$	DG1	$-4 \left( E_1 + Z \log \left( \frac{C_{\text{uA,o}}}{C_{\text{uA,o}}} \right) \right) + p_1 \Delta p$	-566.3	mV
$\Delta G_2$	DG2	$-4 \left( E_2 + Z \left( \log \left( \frac{C_{\text{uA,o}}}{C_{\text{uA,o}}} \right) - \log \left( \frac{[\text{a3r}]}{[\text{a3o}]} \right) \right) \right) + p_2 \Delta p$	-39.7	mV
$\Delta \text{Hbt}$	DHbT	$\Delta \text{HbT}_{\text{offset}} + \text{Hbt} - \text{Hbt}_n$	-0.0002694	$\mu\text{M}$

Name	Model Name	Expression	Initial Value	Units
$\eta$	eta	$R_P \left( \frac{\nu_{P_a}}{\nu_{P_a,n}} - 1 \right) + R_O \left( \frac{\nu_{O_2}}{\nu_{O_2,n}} - 1 \right) + R_u \left( 1 - \frac{\nu_u}{\nu_{u,n}} \right) + R_C \left( 1 - \frac{\nu_{CO_2}}{\nu_{CO_2,n}} \right)$	0	none
AVR	AVR	$\frac{V_a}{V_v}$	0.3333	none
CBF	CBF	$G(P_a - P_v)$	0.008	ml ml <sup>-1</sup> s <sup>-1</sup>
CMRO <sub>2</sub>	CMR02	$f_3 V_{mit}$	0.02	mM s <sup>-1</sup>
CMR <sub>gluc</sub>	CMRgluc	$T_{glucose.in} - T_{glucose.out}$	0.0044	mM s <sup>-1</sup>
CMR <sub>lac</sub>	CMRlac	$T_{lactate.in} - T_{lactate.out}$	-0.002133	mM s <sup>-1</sup>
Cu <sub>A,o</sub>	ared	$[CCO]_{mit} - Cu_{A,o}$	0.01084	mM
HHb	HHb	$1000 \frac{V_a[HHb_a] + V_v[HHb_v]}{4} V_{blood,n}$	16.99	μM
HbO <sub>2</sub>	Hb02	$1000 \frac{V_a[HbO_{2,a}] + V_v[HbO_{2,v}]}{4} V_{blood,n}$	26.89	μM
Hbt	HbT	$1000 \frac{(V_a + V_v)[Hbtot]}{4} V_{blood,n}$	43.87	μM
Keq <sub>1</sub>	Keq1	$10^{\frac{-1}{Z} \left( \frac{p_1 \Delta p}{4} - E_1 \right)}$	123.2	none
Keq <sub>2</sub>	Keq2	$10^{\frac{-1}{Z} \left( \frac{p_2 \Delta p}{4} - E_2 \right)}$	0.07735	none
R <sub>Hi</sub>	R_Hi	$\Gamma_{buffi}$	2.403e+05	none
ScO <sub>2</sub>	Sc02	$\frac{SaO_2 + SvO_2}{2}$	0.7285	none
SvO <sub>2</sub>	Sv02	$\frac{[HbO_{2,v}]}{[Hbtot]}$	0.497	none

Name	Model Name	Expression	Initial Value	Units
TOS	TOI	$100 \left( \frac{\left(\frac{r}{r_n}\right)^2}{\left(\frac{r}{r_n}\right)^2 + \frac{V_v}{V_{a,n}}} [\text{HbO}_{2,a}] + \frac{V_v}{V_{a,n} \left( \left(\frac{r}{r_n}\right)^2 + \frac{V_v}{V_{a,n}} \right)} [\text{HbO}_{2,v}] \right)$	61.28	none
$V_{\max, \text{ATP}}$	v_ATP	$\left( \frac{L_{CV,n} V_{\text{mit}}}{n_a} + 2\text{CMR}_{\text{gluc},n} \right) (1 + k_{m,\text{ATP}}) u$	0.07435	$\text{mM s}^{-1}$
[NADH]	NADH	$N_t - [\text{NAD}]$	1.2	mM
$[\text{NAD}]/[\text{NADH}]$	NADNADHrat	$\frac{[\text{NAD}]}{[\text{NADH}]}$	1.5	none
$\Delta G$	DGp	$\Delta G^\circ + ZF \log(g_p)$	-6.06e+04	$\text{J mol}^{-1}$
$\Delta \text{HHb}$	DHHb	$\Delta \text{HHb}_{\text{offset}} + \text{HHb} - \text{HHb}_n$	0.0002395	$\mu\text{M}$
$\Delta \text{HbO}_2$	DHbO2	$\Delta \text{HbO}_{2,\text{offset}} + \text{HbO}_2 - \text{HbO}_{2n}$	-0.0005089	$\mu\text{M}$
$\Delta \text{Hbdiff}$	DHbdiff	$\Delta \text{Hbdiff}_{\text{offset}} + \Delta \text{HbO}_2 - \Delta \text{HHb}$	-0.0007484	$\mu\text{M}$
$\Delta \text{oxCCO}$	CCO	$\Delta \text{oxCCO}_{\text{offset}} + 1000V_{\text{mit}} (\text{Cu}_{A,o} - \text{Cu}_{A,o,n})$	0	$\mu\text{M}$
$\Delta p$	Dp	$\Delta \Psi + Z (\text{pH}_m - \text{pH}_o)$	168.6	mV
a3 <sub>o</sub>	b	$[\text{CCO}]_{\text{mit}} - [\text{a3r}]$	0.03201	mM
k <sub>1</sub>	k1	$k_{1,0} \exp(-c_{k1} (\Delta p - \Delta p_n))$	13.62	$\text{s}^{-1}$
k <sub>2</sub>	k2	$k_{2,n} \exp(-c_{k2} (\Delta p - \Delta p_n))$	2681	$\text{mM}^{-1} \text{s}^{-1}$
k <sub>-1</sub>	kn1	$\frac{k_1}{K_{\text{eq1}}}$	0.1105	$\text{s}^{-1}$
k <sub>-2</sub>	kn2	$\frac{k_2}{K_{\text{eq2}}}$	3.466e+04	$\text{mM}^{-1} \text{s}^{-1}$
k <sub>1,0</sub>	k10	$\frac{k_{1,n} N_t}{1 + [\text{NAD}]/[\text{NADH}]}$	13.62	$\text{s}^{-1}$

Name	Model Name	Expression	Initial Value	Units
$k_{\text{ATP},\text{CV}}$	kATP	$\frac{L_{\text{CV}}V_{\text{mit}}}{n_a}$	0.06376	$\text{mM s}^{-1}$
$\text{pH}_m$	pH_m	$-\log\left(\frac{\text{H}_m^+}{1000}\right)$	7.4	none
$r_{\text{buffi}}$	r_buffi	$\frac{C_{\text{buffi}}}{C_{\text{oi}}}$	2.403e+05	none
$\mu$	mu	$\frac{\mu_{\text{min}} + \mu_{\text{max}} e^\eta}{1 + e^\eta}$	0	none
$\sigma_e$	sigma_e	$\sigma_{e0} \left( \exp\left(\frac{K_\sigma(r-r_0)}{r_0}\right) - 1 \right) - \sigma_{\text{coll}}$	-44.89	mmHg
$\theta$	theta	$k_{\text{CV}} \left( \Delta p + \frac{Z}{n_a} \log\left(\frac{g_p}{g_{p,n}}\right) - \Delta p_{\text{CV}0} \right)$	1.61	none
$f_1$	f1	$k_1 \text{Cu}_{\text{A},\text{o}} - k_{-1} \text{Cu}_{\text{A},\text{o}}$	0.2985	$\text{mM s}^{-1}$
$f_2$	f2	$k_2 \text{Cu}_{\text{A},\text{o}} \text{a3}_\text{o} - k_{-2} \text{Cu}_{\text{A},\text{o}} [\text{a3r}]$	0.2985	$\text{mM s}^{-1}$
$f_3$	f3	$\frac{k_3 [\text{O}_2] [\text{a3r}] \exp(-c3(\Delta p - \Delta p_{30}))}{1 + \exp(-c3(\Delta p - \Delta p_{30}))}$	0.2985	$\text{mM s}^{-1}$
$g_p$	gP	$\frac{[\text{ADP}][\text{P}_i]}{1000[\text{ATP}]}$	5.195e-06	none
$h$	h	$-r + \sqrt{r^2 + 2r_0 h_0 + h_0 h_0}$	0.00214	cm
$k_{\text{TCA}}$	k_TCA	$\frac{v_{\text{TCA}} [\text{Py}] [\text{NAD}]}{(k_{m,\text{tcaN}} + [\text{NAD}])(k_{m,\text{tcaP}} + [\text{Py}])}$	0.0995	$\text{mM s}^{-1}$
$v_{\text{glyc}}$	Vmax_glucN	$\frac{v_{\text{glyc},n} (I+1)}{1 + I \frac{[\text{ATP}]_n}{[\text{ATP}]} \frac{[\text{AMP}]_n}{[\text{AMP}]}}$	0.004957	$\text{mM s}^{-1}$

## 5 Reactions

Model Name	Description	Reaction
ADPtoATP	Phosphorylation of ADP by Complex V	$\text{ADP} + \text{P}_i \rightarrow \text{ATP}$
ATPtoADP	Hydrolysis of ATP	$\text{ATP} \rightarrow \text{ADP} + \text{P}_i$
O2_in	The reaction in which $\text{O}_2$ is supplied to the mitochondria	$\rightarrow \text{O}_2$
PCrtoATP	A two way mass action reaction representing the interconversion of PCr + ADP to Cr + ATP.	$\text{PCr} + \text{ADP} \leftrightarrow \text{ATP} + \text{Cr}$
PytoLac	interconversion between pyruvate and lactate	$\text{Py} \leftrightarrow \text{lac}$
TCA	One step simple representation of pyruvate dehydrogenase and the TCA cycle	$\text{Py} + 6\text{NAD} \rightarrow$
a_ox	The reaction in which a3 oxidises $\text{Cu}_A$ and $p_2$ protons are pumped out of the matrix	$p2\text{H}_m^+ \rightarrow 4\text{Cu}_{A,o} + 4a3r$
a_red	The reaction in which a is reduced and $p_1$ protons are pumped out of the matrix	$4\text{Cu}_{A,o} + p1\text{H}_m^+ \rightarrow 2\text{NAD}$
aden1	a two way reaction in which two molecules of ADP are converted into one of ATP and one of AMP.	$2\text{ADP} \leftrightarrow \text{ATP} + \text{AMP}$
b_ox	The reaction in which $\text{O}_2$ oxidises a3 and $p_2$ protons are pumped out of the matrix	$\text{O}_2 + 4a3r + p3\text{H}_m^+ \rightarrow$
glucose_in	Transport of glucose from the blood to the cytoplasm (fixed rate)	$\rightarrow \text{gluc}$
glucose_out	Transport of glucose from the cytoplasm to the blood	$\text{gluc} \rightarrow$
glycol	a one way Michaelis Menten reaction which is assumed to capture the process of glycolysis	$2\text{ADP} + 2\text{P}_i + \text{gluc} \rightarrow 2\text{ATP} + 2\text{Py}$
lactate_in	Transport of lactate from the blood to the cytoplasm (fixed rate)	$\rightarrow \text{lac}$
lactate_out	Transport of lactate from the cytoplasm to the blood	$\text{lac} \rightarrow$
psi_out	The reaction in which protons re-enter the matrix (via leak and complex V)	$\rightarrow \text{H}_m^+$

## References

- [1] A Aubert, R Costalat, and R Valabregue. Modelling of the coupling between brain electrical activity and metabolism. *Acta Biotheoretica*, 49(4):301–326, 2001. PMID: 11804241.
- [2] Murad Banaji, Alfred Mallet, Clare E Elwell, Peter Nicholls, and Chris E Cooper. A model of brain circulation and metabolism: NIRS signal changes during physiological challenges. *PLoS Comput Biol*, 4(11):–1000212, November 2008.



- [3] Murad Banaji, Ilias Tachtsidis, David Delpy, and Stephen Baigent. A physiological model of cerebral blood flow control. *Math Biosci*, 194(2):125–173, April 2005.
- [4] Martin D. Brand, Julian L. Pakay, Augustine Ocloo, Jason Kokoszka, Douglas C. Wallace, Paul S. Brookes, and Emma J. Cornwall. The basal proton conductance of mitochondria depends on adenine nucleotide translocase content. *Biochemical Journal*, 392(2):353, 2005.
- [5] R J Corbett, A R Laptok, D Garcia, and J I Ruley. Energy reserves and utilization rates in developing brain measured in vivo by <sup>31</sup>P and <sup>1</sup>H nuclear magnetic resonance spectroscopy. *Journal of Cerebral Blood Flow and Metabolism: Official Journal of the International Society of Cerebral Blood Flow and Metabolism*, 13(2):235–246, March 1993. PMID: 8436615.
- [6] Lars Edvinsson, Eric T Mackenzie, and James McCulloch. *Cerebral Blood Flow and Metabolism*. Raven Pr, December 1992.
- [7] Maria Erecinska, Shobha Cherian, and Ian A. Silver. Energy metabolism in mammalian brain during development. *Progress in Neurobiology*, 73(6):397–445, August 2004.
- [8] P A Flecknell, R Wootton, and M John. Cerebral blood flow and cerebral metabolism in normal and intrauterine growth retarded neonatal piglets. *Clinical Science (London, England: 1979)*, 64(2):161–165, February 1983. PMID: 6681598.
- [9] R Gruetter, E J Novotny, S D Boulware, D L Rothman, G F Mason, G I Shulman, R G Shulman, and W V Tamborlane. Direct measurement of brain glucose concentrations in humans by <sup>13</sup>C NMR spectroscopy. *Proceedings of the National Academy of Sciences of the United States of America*, 89(3):1109–1112, February 1992. PMID: 1736294 PMCID: 48395.
- [10] B. Korzeniewski and J. A Zoladz. A model of oxidative phosphorylation in mammalian skeletal muscle. *Biophys Chem*, 92(1-2):17–34, August 2001.
- [11] J W Lawson and R L Veech. Effects of pH and free mg<sup>2+</sup> on the keq of the creatine kinase reaction and other phosphate hydrolyses and phosphate transfer reactions. *Journal of Biological Chemistry*, 254(14):6528 –6537, July 1979.
- [12] M. Pourcyrous, C. W Leffler, H. S Bada, S. B Korones, and D. W Busija. Cerebral blood flow responses to indomethacin in awake newborn pigs. *Pediatric research*, 35(5):565, 1994.
- [13] Ted S. Rosenkrantz, Joanna Kubin, Om P. Mishra, Douglass Smith, and Maria Delivoria-Papadopoulos. Brain cell membrane Na<sup>+</sup>,K<sup>+</sup>-ATPase activity following severe hypoxic injury in the newborn piglet. *Brain Research*, 730(1-2):52–57, August 1996.
- [14] K. Roth and M. W Weiner. Determination of cytosolic ADP and AMP concentrations and the free energy of ATP hydrolysis in human muscle and brain tissues with <sup>31</sup>P NMR spectroscopy. *Magnetic Resonance in Medicine*, 22(2):505–511, 1991.
- [15] R. Springett, J. Newman, M. Cope, and D. T Delpy. Oxygen dependency and precision of cytochrome oxidase signal from full spectral NIRS of the piglet brain. *Am J Physiol Heart Circ Physiol*, 279(5):–2202, November 2000.
- [16] M. Ursino and C. A Lodi. Interaction among autoregulation, CO<sub>2</sub> reactivity, and intracranial pressure: a mathematical model. *Am J Physiol*, 274(5 Pt 2):–1715, May 1998.