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MORTALITY AND AIR POLLUTION STUDIES:
THE CASE OF SANTIAGO

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Abstract

Most of the epidemiological literature on air pollution and mortality deals only with single or dual pollutant models whose results are hard to interpret and of questionable value from the policy perspective. In addition, much of the existing literature deals only with the very short-term effects of air pollution whereas policy makers need to know when, whether and to what extent pollution-induced increases in mortality counts are reversed. This involves modelling the infinite distributed lag effects of air pollution.

Borrowing from econometrics this paper presents a method by which the infinite distributed lag effects can be estimated parsimoniously but plausibly estimated. The paper presents a time series study into the relationship between ambient levels of air pollution and daily mortality counts for Santiago employing this technique which confirms that the infinite lag effects are highly significant.

It is also shown that day to day variations in NO_2 concentrations and in the concentrations of both fine and coarse particulates are associated with short-term variations in death rates. These findings are made in the context of a model that simultaneously includes six different pollutants. Evidence is found pointing to the operation of a very short term harvesting effect.

1. Introduction

A vast number of epidemiological studies have identified particulate matter and, less frequently, other air pollutants as being statistically related to daily mortality counts. Despite the fact that these studies have been undertaken in a variety of locations the methodology followed by these studies is generally same. The procedure is to use Poisson or Ordinary Least Squares regression analysis to control for seasonal variations in daily mortality counts along with variations in meteorological conditions, day-of-the-week effects, dummy variables for national holidays and one or two pollution variables[1].

Although these studies have alerted policy makers to the potential harm from ambient pollution concentrations the results provided by time-series studies into the mortality effects of air pollution are nonetheless turning out to be of surprisingly limited value from the policy perspective. One problem relates to the current emphasis on single and dual pollutant models in the epidemiological literature. Schwartz et al (1996) remark that "One occasionally sees studies that have fitted regression models using four or even more collinear pollutants in the same regression… Given the non-trivial correlation of the pollutant variables and the relatively low explanatory power of air pollution these for mortality or hospital admissions such procedures risk letting the noise in the data choose the pollutant".

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[1] Here and elsewhere we consider only the issue of life lost due to the acute effects of air pollution. For evidence on the chronic mortality impacts of air pollution see Pope et al (1995).

The authors of this paper believe that alternative procedures risk allowing the researcher to choose the pollutant. This frustrates attempts to determine which out of a range of air pollutants are responsible for the empirically observed mortality impacts. With the evidence as it is we cannot be certain of the extent to which lowering particle concentrations alone, without other reducing other combustion-related pollutants, would lower mortality. The importance to policy makers of being able to attribute health impacts to particular pollutants should be obvious. Policy makers have before them a range of policy and technology options some of which entail reducing emissions of one pollutant whilst leaving the emissions of other pollutants unchanged or even increased.

Current practice also prevents researchers from reaching any conclusions regarding the overall health burden imposed by pollution-generating activities. Given the non-zero correlation that often exists between different air pollutants, reliance on the results of single pollutant models risks explaining what are essentially the same deaths several times over. Conversely, to assume that one pollutant such as PM_{10} is responsible for all of the observed health impacts risks significantly understating the toll of air pollution on health. These problems are avoided by multiple pollutant studies.

Matters are admittedly more complicated when one recognises ambient concentrations recorded by monitors might be a poor representation of individual exposure to a particular pollutant. Furthermore many pollutants might need to be included in the same regression some of which will be precursors of others included in the same regression. But none of these observations justifies the almost complete reliance on single or dual pollutant

studies or removes the understandable need that policy makers have to be able to attribute health impacts to particular pollutants or to calculate the overall toll on health.

The other problem, which is in some ways the main focus of this paper, involves the way air-pollution variables are entered into the model. Typically air pollution is included either as a contemporaneous variable or with one or two lags. Although such a methodology may succeed in demonstrating that air pollution causes a short-run increase in mortality rates policy responses cannot be built only on the basis of knowledge concerning the short-run impact of air pollution on mortality. Policy needs to the rate at which air pollution-induced increases in mortality counts are reversed[2].

In the absence of evidence on the rate at which excess mortality counts attributable to air pollution are reversed researchers from other disciplines have been at a loss to know how to value such deaths from a societal point of view. Economists for example are accustomed to valuing small changes in the risk of mortality or even small changes in a sequence of risks in which future risks are discounted. An air pollution episode is likely to increase the number of deaths in the short term but lead to a reduction in the number of deaths in future time periods. But unless they know the sequence of changes in risk or equivalently the infinite lagged impact of air pollution on mortality economists cannot value the air pollution episode correctly. McMichael et al (1998) provides a telling

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[2] Being aware of this limitation to their work typically contributors to the epidemiological literature are very careful to specify that the empirical evidence does not say anything about the extent to which life has been foreshortened as a consequence of poor air quality. Indeed

summary assessment of early attempts to value the mortality impacts of air pollution.

Our paper introduces a simple modelling technique in which the entire infinite lagged-response of daily mortality to increases in air pollution is modelled in a plausible yet parsimonious fashion. In so doing the technique nests the kind of models that have so far been used to explore the links between air pollution and mortality as special cases. We argue that such methods provide a far superior description of variations in daily mortality rates. And for the reasons given yield insights of potentially far greater relevance to policy. This paper further provides a demonstration of the technique using data from Santiago[3].

Although the modifications to current practice presented in this paper are intended to make the evidence offered by epidemiological research more relevant to policy, there is no suggestion that the techniques in this paper offer anything approaching a 'get out of jail free'. The multicollinearity between different pollutants makes it difficult to ascertain their individual contribution as well as the lag effect meaning the results of individual analyses are too uncertain to base policy. Only when the results of many different studies are combined using meta-analytical procedures will any statistically significant effects emerge. Rather that refraining from such ambitious studies, the point is

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the epidemiological literature states in a number of places that it is impossible to measure the extent of life lost using time series studies (see for example Anderson et al 1996).

[3] It should be apparent that identical issues arise in the analysis of morbidity endpoints. The Committee on the Medical Effects of Air Pollution (1998) discusses the importance of determining whether additional cases of respiratory hospital admission are caused by air pollution or whether these are simply brought forward – in which case the cost to the public should not be attributed to air pollution. The same techniques described in this paper could in principle be used answer this question.

that unless researchers begin to publish such studies then the data for meta-analyses will never appear in the public domain. Meta-analysis of results obtained from conventional studies will, of course, never answer the question of the extent of the harvesting effect or the contribution of individual pollutants no matter how many studies are undertaken.

The following section offers a discussion and critique of current practice in modelling the distributed lag effects of air pollution on mortality. An alternative method of modelling the distributed lags is introduced and the relative advantages of the method are explained. The remainder of the paper describes the empirical implementation of the technique within the context of a multiple pollutant model. Section three discusses the data used to implement the model along with the econometric modelling techniques employed. Section four discusses the implications of the results and the final section concludes.

2. Modelling Lags in Time Series Air Pollution-Mortality Studies

The traditional approach to the statistical modelling of the relationship between daily mortality counts and ambient levels of air pollution is to include just contemporaneous, once or twice-lagged values for air pollution into a regression equation. In these cases the choice about which lag to select is seldom explained in detail but often it appears that the single most significant lag is chosen as for example in Katsouyanni et al (1996).

It is however improbable that the researchers who present such models in the literature intend them to be taken literally. For example, a researcher who seeks to explain variations in daily mortality rates by the value of a pollutant once lagged is not claiming that the totality of the effect is experienced precisely one day afterwards. Nevertheless what such investigators actually end up estimating is the 'transient' impact of air pollution. An extension of this approach would be to estimate the model using single lagged-values for air pollutants ever more distant in time. In this way one might suppose that the lagged impacts of air pollution on mortality would emerge if the results were plotted on a graph. The problem with this approach is that, to the extent that pollutant variables are auto-correlated over time, the effects of adjacent lag terms will also be picked up.

Regression on a moving average of air pollution levels is perhaps a small improvement on including just single lags (e.g. Schwartz 1994). But since it impels the lagged effects of pollutants to be exactly equal on consecutive days and thereafter constrains them to be zero it cannot be very realistic. In other papers researchers estimate the coefficients on two or more consecutive

pollution-levels and present the cumulated impact of air pollution (e.g. Dab et al 1996). These represent a further improvement but once again require that the impact of air pollution on mortality is zero after two or three days. A more realistic model would allow for the lagged effects of pollutants gradually to decay and perhaps turn negative if the deaths of susceptible individuals were being brought forward.

In theory the means to explore such a possibility would be to estimate a model containing many lagged terms for each of the pollutants. In practice however analysts have avoided adding a large number of additional regressor variables to their models. They quite rightly claim that estimation of the unrestricted regression will not be able to locate the lag structure because it will be beset by multicollinearity between the lagged regressors.

These reflections on current practice raise the following questions. First, how can a distributed lag structure be modelled parsimoniously in the context of air pollution-mortality studies (or indeed any study)? Secondly, how sensitive are the estimated relative risk ratios to seemingly arbitrary decisions regarding the period of time over which to cumulate the lagged impacts of air pollution? Thirdly, to what extent can adding a more realistic lag structure reduce the unexplained variance in a model?

A number of techniques to approximate lag structures have been proposed in econometrics and these may be helpful in the context of epidemiological studies too. This is a view shared by Schwartz et al (1996) who argue that the epidemiological literature needs to pay greater heed to econometric approaches

to modelling distributed lags. It is also plausible that a more systematic approach to specifying lags would allow better comparison between sites. However, the main reason for being interested in modelling distributed lags is in order to shed light on the question of the amount of life lost per case of premature mortality.

One method of estimating lagged impacts is the polynomial approach of Almon (1965). The technique involves making the assumption that the distribution of lag coefficients can be represented by a polynomial of suitably high order. The coefficients of the polynomial are estimated absorbing the order of the polynomial plus one degrees of freedom.

In one of the first epidemiological studies to take advantage of this technique, Schwartz (2000) employs a quadratic polynomial lag with a maximum lag of five days in an analysis of the link between ambient concentrations of particulate matter and the deaths of over-65s based on United States data[4]. He finds that the use of the technique increases the measured relative risk ratios associated with particulate matter compared to those associated with a one-day lag or a two-day moving average. Schwartz argues that this method should become standard practice in the epidemiological time-series studies. For a number of reasons we do not agree with this view.

The method of polynomial lags suffers from the handicap that it is necessary to specify a finite endpoint prior to estimation. There has, in the econometrics literature, been an extensive analysis of the consequences of miss-specifying

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[4] Ostro et al (1996) fit a polynomial distributed lag over the period t = 0-3 to their analysis of daily mortality counts in Santiago but provide no further details.

the lag length (as well as the order of the polynomial; see for example Hendry et al 1984). Simply assuming a maximum lag length is hazardous as the Almon lags technique will genially distribute the effects over the entire lag whether this is appropriate or not[5]. Finally, the technique has extreme difficulty in capturing any long-tailed lag distribution of the type that might well be expected in epidemiological time-series studies (see for example Maddala 1977).

In the opinion of the authors these features serve to make the polynomial lags technique unsuitable for use in epidemiological time-series studies. Partly because of these shortcomings the polynomial lags technique has seen relatively few recent applications in the field of applied econometrics. Most econometricians take recourse in the method of 'rational lags' (Jorgenson, 1966) in situations in which the modelling of distributed lags is required.

The idea behind rational lags is that *any* infinite distributed lag function can be approximated by the ratio of two finite polynomials in the lag operator and as such the rational lags technique involves only the inclusion of additional explanatory variables. The lag operator L is defined by $LX_t = X_{t-1}$. The lag operator may be applied more than once so that $L^2X_t = X_{t-2}$. It may also be handled algebraically like an ordinary variable such that $L^1L^2X_t = X_{t-3}$. Consider now the following infinite distributed lag model:

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[5] The Schwartz (2000) study might be criticised for simply assuming a maximum lag of five days and the appropriateness of a polynomial of degree two. There are protocols for selecting the appropriate lag lengths and order of the polynomial but these do not appear to have been followed.

$$Y_t = \alpha + \sum_{i=0}^{i=\infty} \beta_i L^i X_{t-i} + e_t$$

Rather than estimating the unrestricted model Jorgenson's Rational Lag technique involves estimating the following equation by means of non-linear least squares:

$$Y_t = \alpha + \frac{\gamma_0 + \gamma_1 L X_t + \gamma_2 L^2 X_t + \ldots + \gamma_j L^j X_t}{1 + \omega_1 L X_t + \omega_2 L^2 X_t + \ldots + \omega_k L^k X_t} + e_t$$

It is possible to retrieve the implied parameters of distributed lag function in a relatively straightforward manner enabling the analyst to observe the lagged impact of a pulse change in the independent variable. Given the equivalence between the parameters of the distributed lag and the parameters of the rational lag function one can rewrite the equation in the following way:

$$\left(\beta_0 + \beta_1 L + \beta_2 L^2 + \beta_3 +^3 \ldots\right)\left(1 + \omega_1 L + \omega_2 L^2 + \omega_3 L^3\right) = \left(\gamma_0 + \gamma_1 L + \gamma_2 L^2 + \gamma_3 L^3\right)$$

By comparing coefficients of the various powers of L one obtains the following:

$$\beta_0 = \gamma_0$$
$$\beta_1 = \gamma_1 - \beta_0 \omega_1$$
$$\beta_2 = \gamma_2 - \beta_0 \omega_2 - \beta_1 \omega_1$$
$$\beta_3 = \gamma_3 - \beta_0 \omega_3 - \beta_1 \omega_2 - \beta_2 \omega_1$$
$$\beta_4 = -\beta_1 \omega_3 - \beta_2 \omega_2 - \beta_3 \omega_1$$

Notice that after the fourth term the series follows the simple recursion:

$$\beta_k = -\beta_{k-3}\omega_3 - \beta_{k-2}\omega_2 - \beta_{k-1}\omega_1$$

These equations may now be solved recursively for each β.

The rational lag technique seems well suited to dealing with issues that arise in epidemiological time-series studies. But to the best knowledge of the authors this is first occasion on which its use has been seriously proposed in such a context. Schwarz et al (1996) does however suggest the use of a geometric lag for use in air pollution studies. Such a lag function is in fact the simplest possible example of a rational lag formulation. The use of the geometric lag is however deeply unappealing in this context since it assumes that the lag coefficients decline monotonically. We have argued that a more reasonable formulation would allow the lag coefficients to first increase and then decrease perhaps becoming negative if the deaths of vulnerable people are being brought forward. In the next section we illustrate the use of the technique of rational lags using data from Santiago.

3. The Empirical Analysis

Santiago is a city with very high levels of particulate air pollution, related in part to its geographic situation and climatic conditions. One study showing the relationship between levels of particulate air pollution and mortality in Santiago has already been published (Ostro et al 1996). Using a single pollutant model this paper shows a strong association between PM_{10} and daily deaths.

Daily data on non-accidental (ICD9 $\geq$ 800) mortality for all ages was taken from the metropolitan area of Santiago from the start of 1988 to the end of 1996 – a period of some 3,288 days[6]. Air pollution and temperature data were obtained from the records of the urban air pollution monitoring-network. From 1988 to 1996 this network operated five monitoring stations. Four of the monitors are closely located around downtown Santiago, and the fifth is in the far northeast of the city. Twenty-four hour averages were obtained for $PM_{2.5}$, PM_{10}, SO_2, NO_2, CO and O_3 concentrations from all five stations. Measures of mean temperature were obtained from four of the five monitoring stations. The data are described in tables 1 and 2. Note that some missing observations have been completed using first order regression techniques (see Maddala, 1977).

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[6] The metropolitan area of Santiago includes 34 municipalities but only 32 of them were included in the analysis. Two were excluded for being mostly rural with low air pollution levels. Deaths of residents of Santiago that occurred outside of Santiago were also excluded.

Table 1:   Descriptive Statistics

Variables	Mean	Std. Deviation	Minimum	Maximum
MORT	56.6	12.4	22.0	116.0
TEMP (°C)	15.9	4.8	4.0	27.0
$PM_{2.5}$ ($\mu g/m^3$)	57.2	40.5	7.0	341.0
PM_{10} ($\mu g/m^3$)	102.4	52.3	16.0	438.0
CO (ppb)	2.5	1.8	0.2	12.8
SO_2 (ppb)	18.0	12.3	1.0	87.0
NO_2 (ppb)	41.0	26.7	9.0	299.0
O_3 (ppb)	90.2	63.0	3.0	963.0

Source: See text.

Table 2:   The Correlation Matrix

	MORT	TEMP	$PM_{2.5}$	PM_{10}	CO	SO_2	NO_2	O_3
MORT								
TEMP	-0.52							
$PM_{2.5}$	0.46	-0.51						
PM_{10}	0.41	-0.38	0.96					
CO	0.50	-0.49	0.82	0.81				
SO_2	0.24	-0.26	0.65	0.65	0.56			
NO_2	0.40	-0.26	0.62	0.70	0.64	0.45		
O_3	-0.22	0.46	-0.04	0.03	-0.05	0.21	0.04	

Source: See text.

The following regression equation was estimated in which L is the lag operator and μ_t represents the combined influence of cyclical components and the autonomous trend[7]:

$$\log(MORT_t) - \mu_t = \alpha + \frac{\sum_{i=0}^{i=3}\gamma_i L^i TEMP_t}{1+\sum_{i=1}^{i=3}\omega_i L^i TEMP_t} + \frac{\sum_{i=0}^{i=3}\psi_i L^i TEMP_t^2}{1+\sum_{i=1}^{i=3}\omega_i L^i TEMP_t^2} + \frac{\sum_{i=0}^{i=3}\lambda_i L^i PM_{2.5t}}{1+\sum_{i=1}^{i=3}\omega_i L^i PM_{2.5t}} +$$

$$\frac{\sum_{i=0}^{i=3}\sigma_i L^i PM_{10-2.5t}}{1+\sum_{i=1}^{i=3}\omega_i L^i PM_{10-2.5t}} + \frac{\sum_{i=0}^{i=3}\nu_i L^i CO_{2t}}{1+\sum_{i=1}^{i=3}\omega_i L^i CO_{2t}} + \frac{\sum_{i=0}^{i=3}\theta_i L^i SO_{2t}}{1+\sum_{i=1}^{i=3}\omega_i L^i SO_{2t}} + \frac{\sum_{i=0}^{i=3}\rho_i L^i NO_{2t}}{1+\sum_{i=1}^{i=3}\omega_i L^i NO_{2t}} +$$

$$\frac{\sum_{i=0}^{i=3}\delta_i L^i O_{3t}}{1+\sum_{i=1}^{i=3}\omega_i L^i O_{3t}} + e_t$$

This equation employs the rational lag technique to approximate an infinite distributed-lag on both the temperature and the pollution variables. Note that choosing i = 0-3 for both the numerator and denominator one is able to capture quite complicated lag patterns. Choosing i = 0-3 also has the advantage of encompassing the finite lag models typically encountered in epidemiological research (e.g. Katsouyanni et al, 1996). Note that the same parameters ω_1, ω_2 and ω_3 appear in the denominator of each term. This is sufficient to generate

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[7] The cyclical components and autonomous trends are the fitted values obtained by regressing the log of mortality on six dummy variables for different days of the week; a dummy variable for national holidays; a cubic time trend and sine and cosine terms of various frequencies. The coefficients on the sine and cosine terms were allowed to vary over the years. In this way the presence or absence of epidemics and changes in the timing of the seasonal peak and the size of the seasonal peak to trough ratio were accounted for.

infinite lagged effects for every variable but an even more flexible model would allow them to vary.

The influence of temperature on mortality is well documented. The association is not linear, with some studies reporting a U-shaped relationship. We accommodate this by including a quadratic term for temperature with the mean subtracted. Rather than include PM_{10} and $PM_{2.5}$ as separate regressors we include $PM_{2.5}$ (fine particles) and $PM_{10-2.5}$ (coarse particles) in an attempt to reduce the level of multicollineary between these regressors.

The error term was assumed to be normally identically and independently-distributed and estimates of the parameters were obtained by using maximum likelihood estimation techniques[8]. Examination of the residuals yields no evidence of autocorrelation (the Durbin-Watson statistic is 2.02). This also suggests that the cyclical components and autonomous trends have been satisfactorily controlled for. The R^2 statistic was 0.04. Full details of the estimation results are available from the authors on request.

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[8] In many empirical analyses the error term is assumed to be a Poisson variable. In this analysis the daily number of deaths is typically very large and there is probably no discernible difference from modelling the error term as a Normal variable.

4. **Discussion**

The main point of interest is whether the exclusion of those additional terms that allow for infinite lagged impacts represents a statistically significant loss of fit. The alternative is a model, like those currently encountered in the literature, in which the effects of air pollution and meteorological variables can be satisfactorily represented by allowing for only three lagged terms. A likelihood-ratio test suggests that the loss of fit from setting parameters ω_1, ω_2 and ω_3 equal to zero is significant at the one-percent level[9]. This finding provides strong support for the use of the rational-lags technique in the context of air pollution mortality studies.

Turning to the question of whether individual air pollutants are statistically significant or not, the results of a suite of likelihood ratio tests are presented in table 3. This table suggests that when tested against a model containing all six air-pollutants three out of six air pollutants are statistically significant at the one-percent level of significance. The remaining air pollutants are not statistically significant even at the ten-percent level of significance. Beyond this it is difficult to compare these results to the existing literature. First and foremost this is because most researchers are measuring either the transient impact of air pollution at variety of lag lengths or the interim impact cumulated over an arbitrary number of days. The rational-lags technique by contrast calculates a different transient impact at each lag length. Secondly, unlike most other

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[9] The χ^2 Statistic is 11.56 against a critical value of 11.34 at the one-percent level of significance with 3 degrees of freedom.

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analyses, this study calculates the mortality effects of air pollution within the context of a multiple pollutant rather than a single pollutant model.

Table 4 presents the lag coefficients cumulated over different lag lengths. The first observation is that the lag coefficients cumulated over t = 0-7 differ from the coefficients at time t = 0. More specifically they are reduced not only in terms of their significance but also in terms of their absolute value. Furthermore the cumulative lag coefficients do not appear to change even to two significant figures when cumulated over periods between t = 0-7 and t = 0-∞. This is evidence consistent with the existence of a very short term harvesting effect.

Note that the cumulated coefficients over the period t = 0-∞ are not restricted to sum to zero even though common sense suggests that this restriction should hold. In fact, although it is easy to restrict the model such that the lag coefficients cumulated over the period t = 0-∞ sum to zero we prefer to test the hypothesis using a Wald test. The hypothesis is not rejected even at the 10 percent level of significance[10]. We do not however recommend imposing this restriction as a matter of course since it might sometimes interfere with the ability of the model to represent short-term lags.

There are a number of other interesting points that emerge from the current analysis. The first is that whereas the majority of attention has been focussed on particulate matter, an increased concentration of NO_2 is also seen to result in a significant variation in short term mortality rates. Other researchers have also

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[10] The statistic is 9.92 against a critical value of 10.64 at the ten-percent level of significance with 6 degrees of freedom.

identified NO_2 as a significant cause of premature mortality: for a survey and meta-analysis see Touloumi et al (1997). Secondly, whilst CO is associated with a significant effect at lag $t = 0$ according to the Likelihood Ratio test CO is statistically insignificant. As an empirical matter it is not unusual for a Wald test and a Likelihood Ratio test to give different results although here the difference is quite pronounced.

Finally, even though they are to some extent collinear it nonetheless appears useful to distinguish between fine particles and coarse particles. More specifically it appears that whereas fine particles are significantly associated with short term increases in mortality, coarse particles are associated with a significant reduction in short term mortality. One interpretation might be that whilst fine particulate matter is harmful to health coarse particulate matter is not. Furthermore the fact that coarse particulate matter has a negative coefficient might indicate that only very fine particulate matter is an important cause of premature mortality.

Table 3:   The Individual Significance of Different Air Pollutants

Variables	Likelihood Ratio Test Statistic	Degrees of Freedom
$PM_{2.5}$	15.30***	4
$PM_{10\text{-}2.5}$	15.52***	4
CO	7.40	4
SO_2	5.36	4
NO_2	14.34***	4
O_3	4.46	4

Source: see text. Note that *** means significant at the one-percent level of significance, ** means significant at the five-percent level of significance and * means significant at the 10 percent level of significance.

Table 4:   Air Pollution as an Influence on Mortality Rates (All Ages)

Variables	Cumulated Over $t = 0$	Cumulated Over $t = 0\text{-}7$	Cumulated Over $t = 0\text{-}\infty$
$PM_{2.5}$	0.35E-03**	-0.13E-03	-0.13E-03
	(0.14E-03)	(0.16E-03)	(0.16E-03)
$PM_{10\text{-}2.5}$	-0.64E-03***	-0.26E-03	-0.26E-03
	(0.25E-03)	(0.30E-03)	(0.30E-03)
CO	0.62E-02**	0.51E-02	0.51E-02
	(0.31E-02)	(0.32E-02)	(0.32E-02)
SO_2	0.22E-03	0.11E-03	0.11E-03
	(0.38E-03)	(0.31E-03)	(0.31E-03)
NO_2	-0.35E-03**	0.30E-03*	0.30E-03*
	(0.17E-03)	(0.18E-03)	(0.18E-03)
O_3	0.38E-05	0.11E-03	0.11E-03
	(0.23E-04)	(0.86E-04)	(0.86E-04)

Source: see text. Figures relate to the estimated lag coefficients. Standard errors are in parentheses and have been calculated using the delta method. Note that *** means significant at the one-percent level of significance, ** means significant at the five-percent level of significance and * means significant at the 10 percent level of significance.

5. Conclusions

This paper has noted the problem of interpretation that the use of single pollutant models presents policy makers. The simple solution is for epidemiologists to present the results of multiple pollutant models and for policy makers to base their results exclusively upon them.

This paper has also noted that much of the existing epidemiological literature estimates only the very short-term transient or cumulative impacts of air pollution. But cumulating the impacts of air pollution over the very short term or presenting only the transient impacts at lags $t = 0$ or $t = 1$ could inadvertently give policy-makers or those from other disciplines a misleading impression of the health risks posed by the acute effects of air pollution. The most probable reason for the focus on the very short-term impacts is that epidemiologists have hitherto not known how to model infinite lags in a parsimonious manner.

Noting the deficiencies of alternative techniques, this paper has used the method of rational lags to approximate the infinite distributed lag impact of a change in air pollution. The method is straightforward and involves including additional terms that permit one to approximate the entire distributed lag. In the case of Santiago these are shown to dramatically improve the fit of the regression equation even in the context of a multiple pollutant model.

Because the results from any one study are too uncertain to be used as a basis for policy it would be interesting to reanalyse the data from existing studies using this technique. By computing the cumulated impact of air pollution at fixed

intervals (e.g. up to one day, one week and one month) and combining the results it may be possible to determine the speed with which excess mortality attributed to the acute impacts of air pollution is reversed. The standard errors of the parameters of interest in this study suggest that large numbers of studies would be required in order for statistically significant results to emerge. Fortunately there are many data sets available for analysis. But in order to be meaningful such comparisons must be careful to compare the impacts cumulated over identical periods of time and, if they intend to be policy relevant, should certainly avoid focussing solely on the very short-term impacts.

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